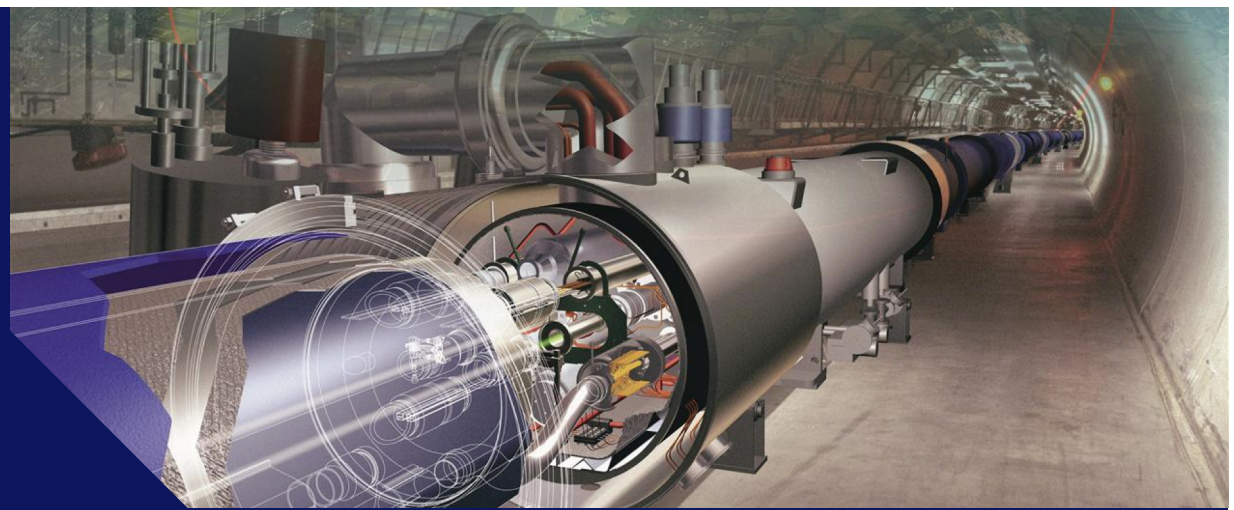




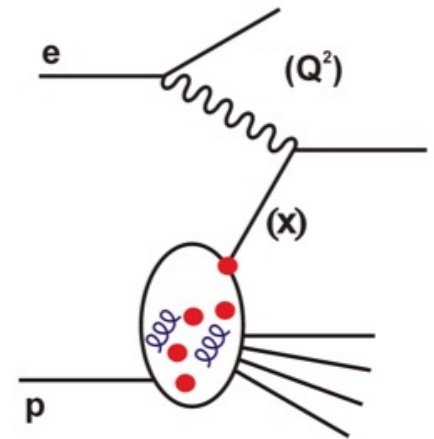
online conference
26 – 30 July 2021



Precision QCD and Small x Physics at the LHeC and FCC-eh

Claire Gwenlan, Oxford

on behalf of the LHeC and FCC-eh study groups

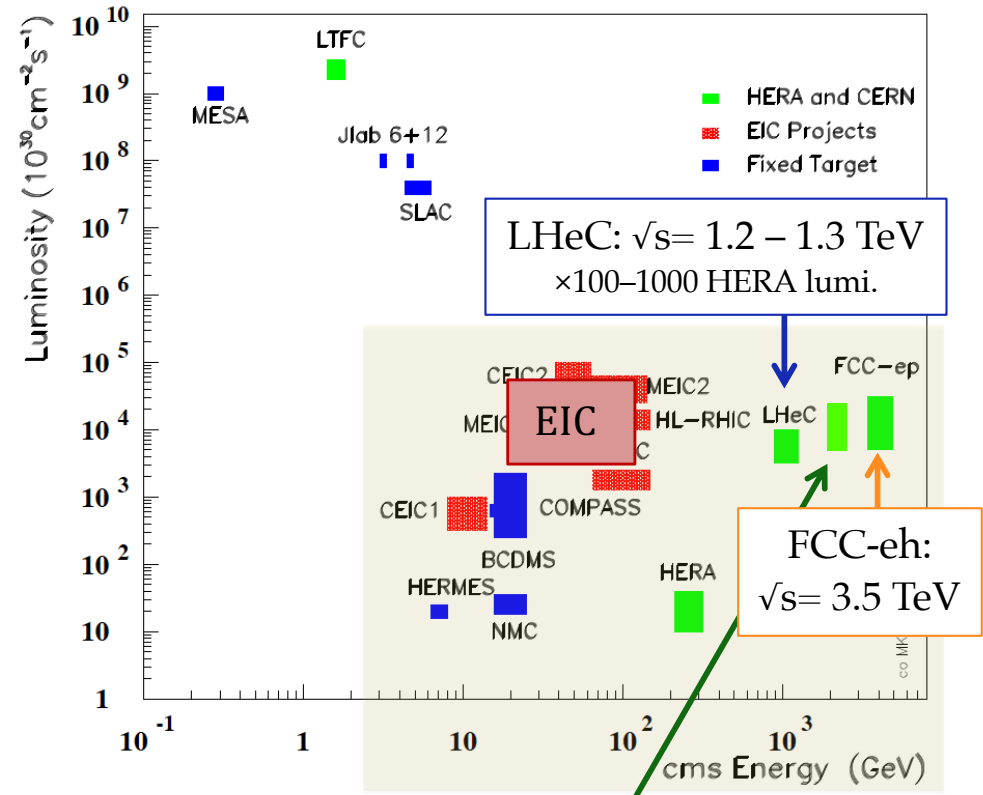
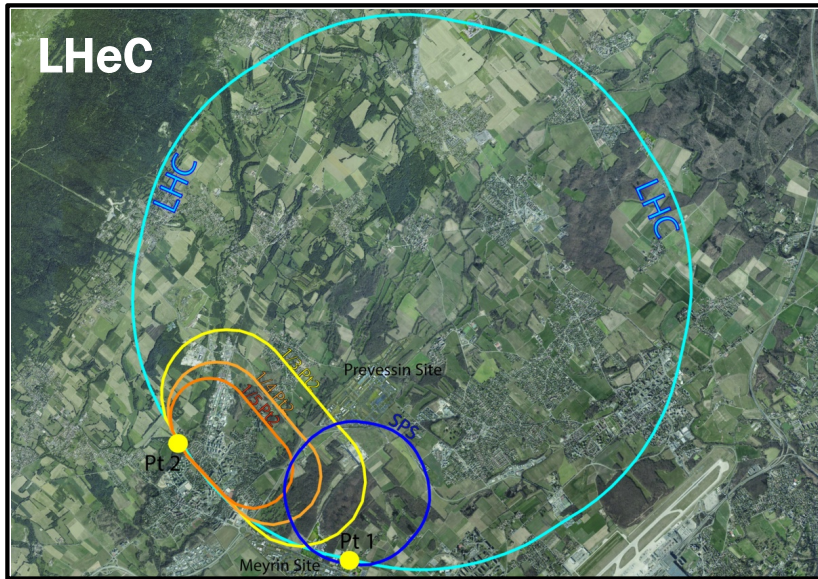


with focus on results from LHeC CDR update, arXiv:[2007.14491](https://arxiv.org/abs/2007.14491)



LHeC, FCC-eh and PERLE

CERN future colliders: arXiv:[1810.13022](https://arxiv.org/abs/1810.13022)



energy recovery LINAC (ERL)

attached to HL-LHC (or FCC)

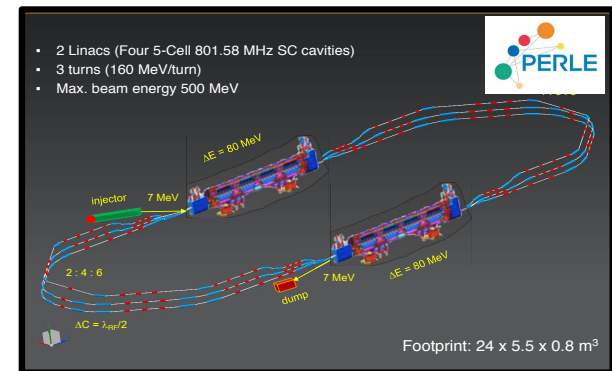
e beam: $\rightarrow 50$ or 60 GeV

e pol.: $P = \pm 0.8$

Lint $\rightarrow 1-2 \text{ ab}^{-1}$ (**1000 \times HERA!**)

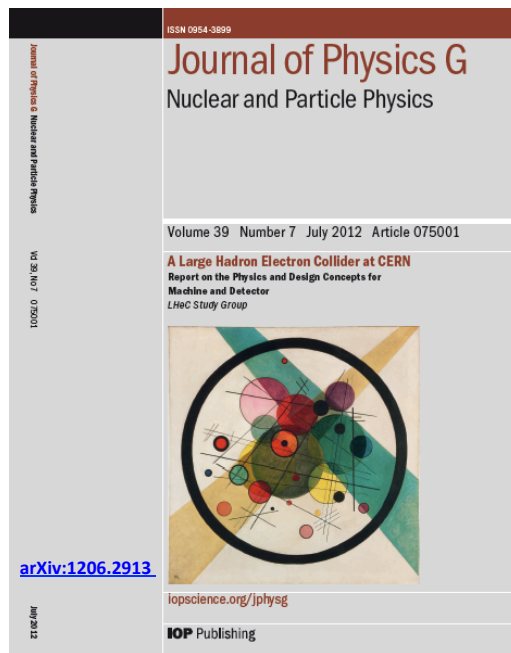
PERLE: international collaboration built to realise 500 MeV energy facility at Orsay, for development of ERL with LHeC conditions

ESPPU: ERL is a high-priority future initiative for CERN



LHeC Conceptual Design Report and Beyond

CDR 2012: commissioned by
CERN, ECFA, NuPECC
200 authors, 69 institutions



arXiv:[1206.2913](https://arxiv.org/abs/1206.2913)

see also, **FCC CDR**, vols 1 and 3:

physics, [EPJ C79 \(2019\), 6, 474](https://arxiv.org/abs/1907.04847)

FCC with eh integrated, [EPJ ST 228 \(2019\), 4, 755](https://arxiv.org/abs/1907.04847)

CDR update 2020
300 authors, 156 institutions

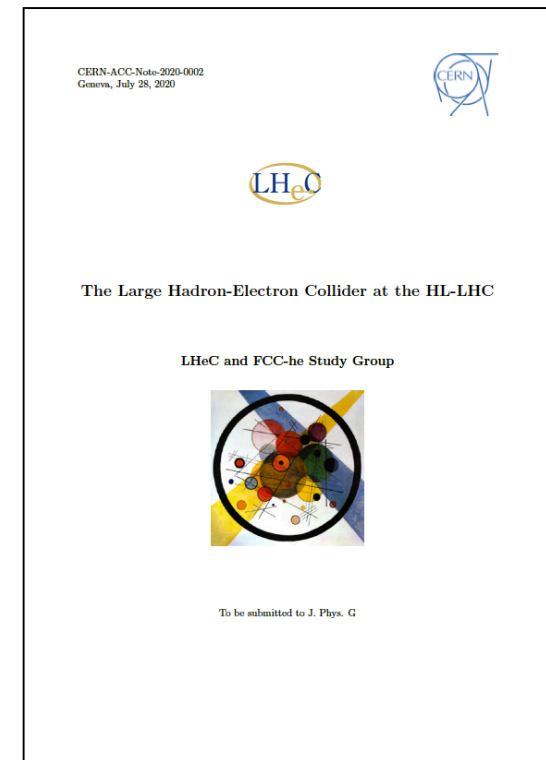
Further selected references:

On the relation of the LHeC and the LHC
arXiv:[1211.5102](https://arxiv.org/abs/1211.5102)

The Large Hadron Electron Collider
arXiv:[1305.2090](https://arxiv.org/abs/1305.2090)

Dig Deeper
Nature Physics 9 (2013) 448

Future Deep Inelastic Scattering with the LHeC
arXiv:[1802.04317](https://arxiv.org/abs/1802.04317)



arXiv:[2007.14491](https://arxiv.org/abs/2007.14491)

5 page summary: **ECFA newsletter No. 5, August 2020**

<https://cds.cern.ch/record/2729018/files/ECFA-Newsletter-5-Summer2020.pdf>

Physics with Energy Frontier DIS

see also, other **LHeC** / **FCC-eh** contributions to this conference:

BSM, O. Fischer

eA, G. Milhano

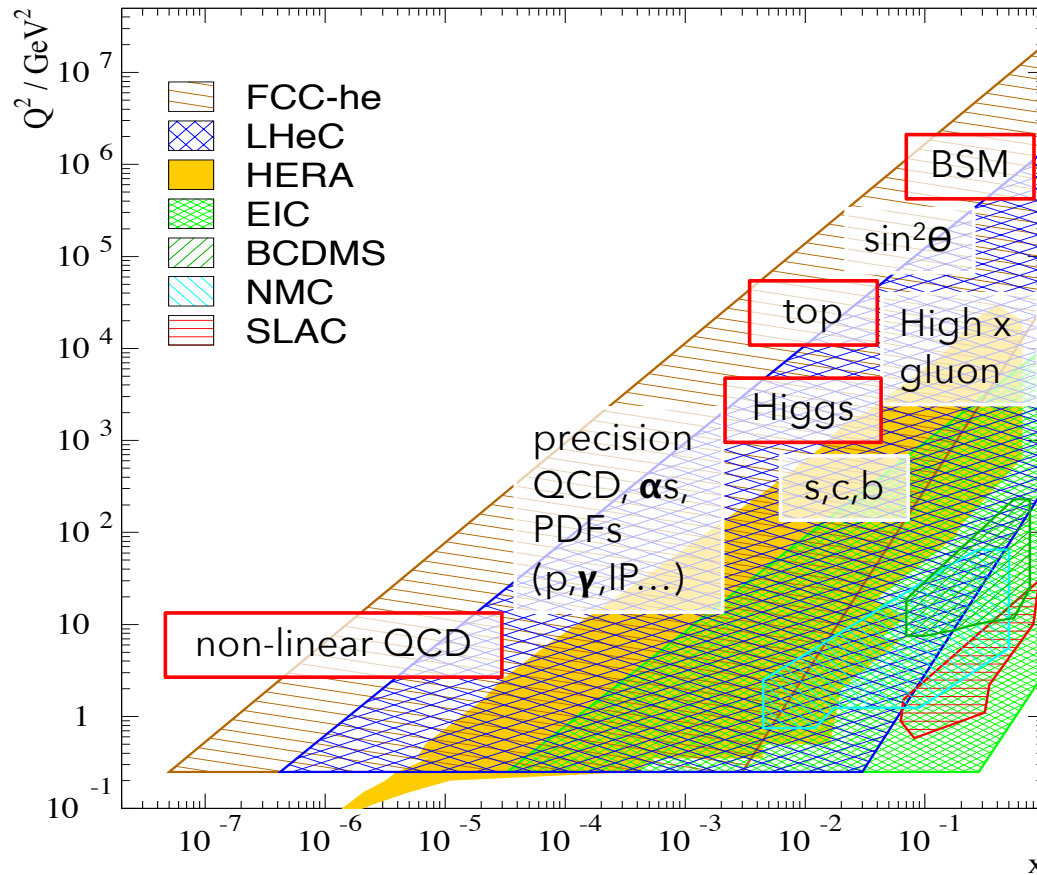
Higgs, U. Klein

EW, and LHeC as part of HL-LHC, D. Britzger

Top, S. Behera

LHeC status and plans, K. Andre (poster)

PERLE, B. Hounsell (poster)



opportunity for **unprecedented increase in DIS kinematic reach;**
×1000 increase in lumi.
 cf. HERA

no higher twist,
 no nuclear corrections,
 free of symmetry assumptions,
 N3LO theory, ...

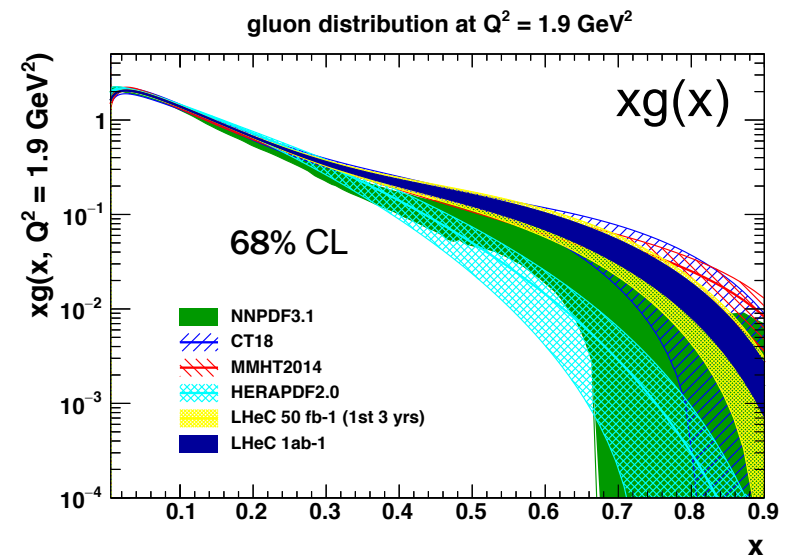
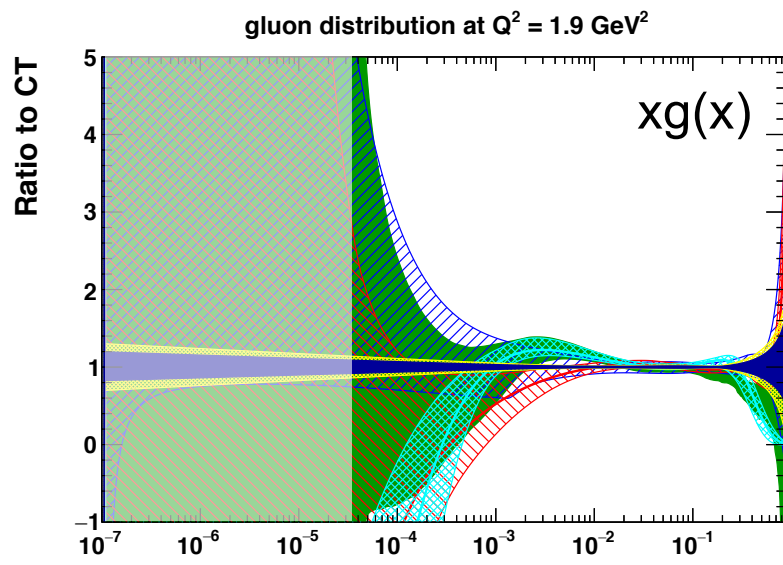
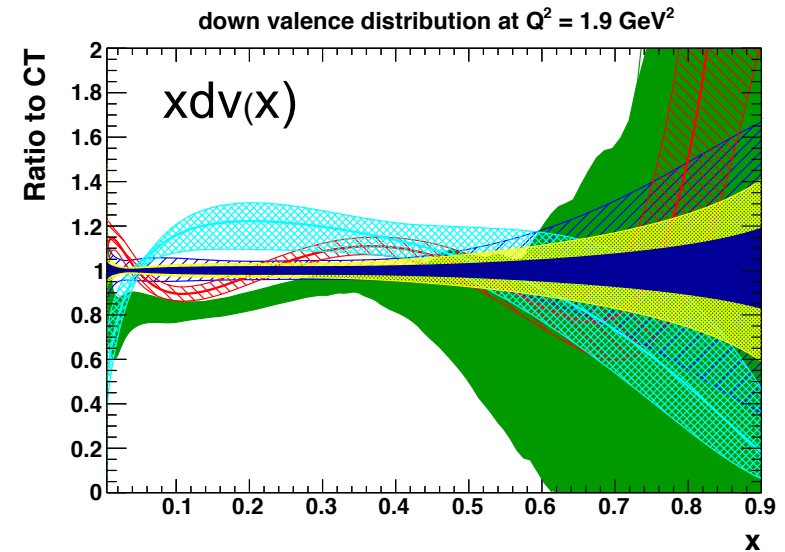
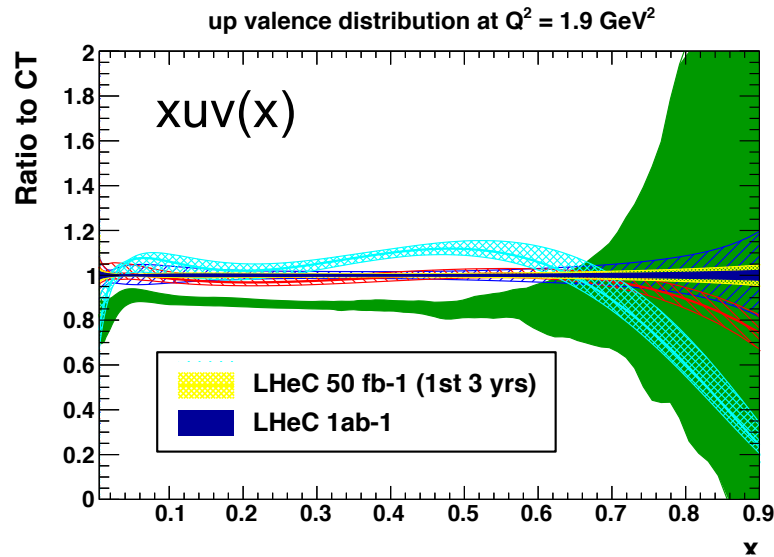
completely resolve **all proton pdfs,**
 sensitivity to **$x \rightarrow 1$,**
 and exploration of **small x regime;**

α_s to permille precision

×15/120 extension in $Q^2, 1/x$ reach vs **HERA**

(LHeC projected timeline, several years concurrent HL-LHC operation, plus dedicated run, arXiv:[1810.13022](https://arxiv.org/abs/1810.13022))

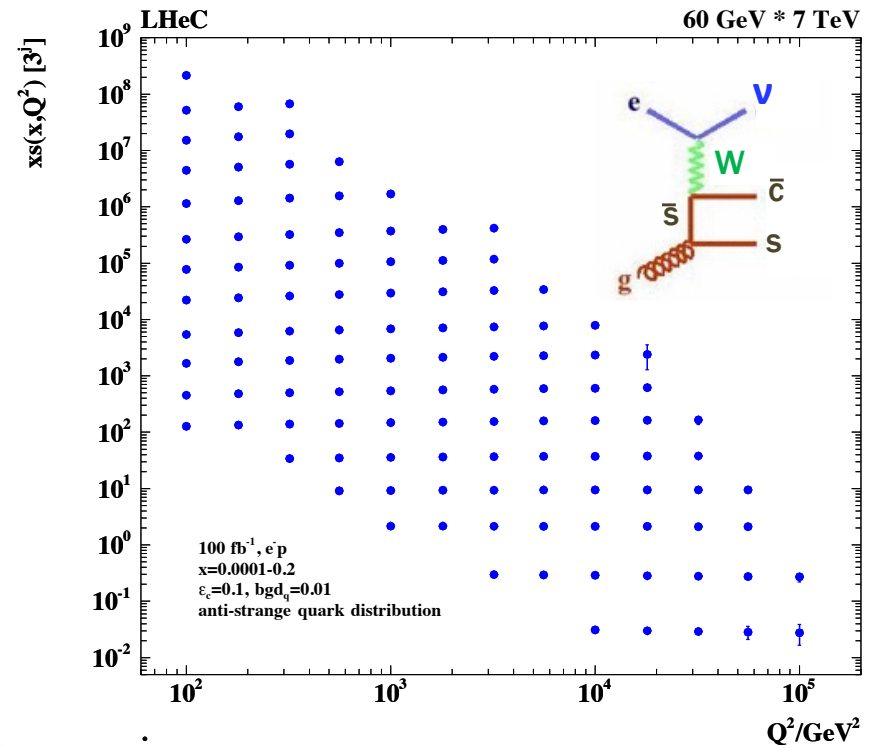
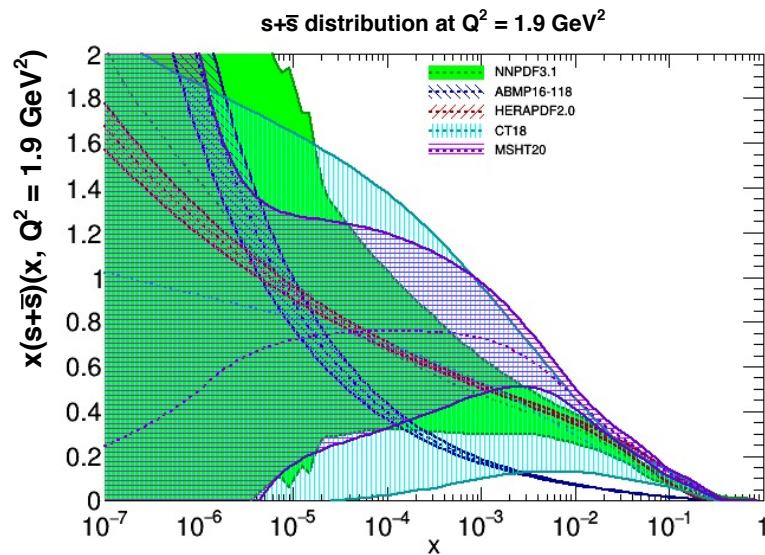
Quark and Gluon PDFs



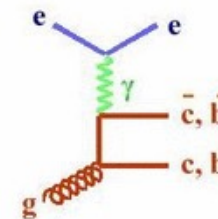
Strange, c, b

- **strange pdf** poorly known
- suppressed cf. other light quarks?
strange valence?

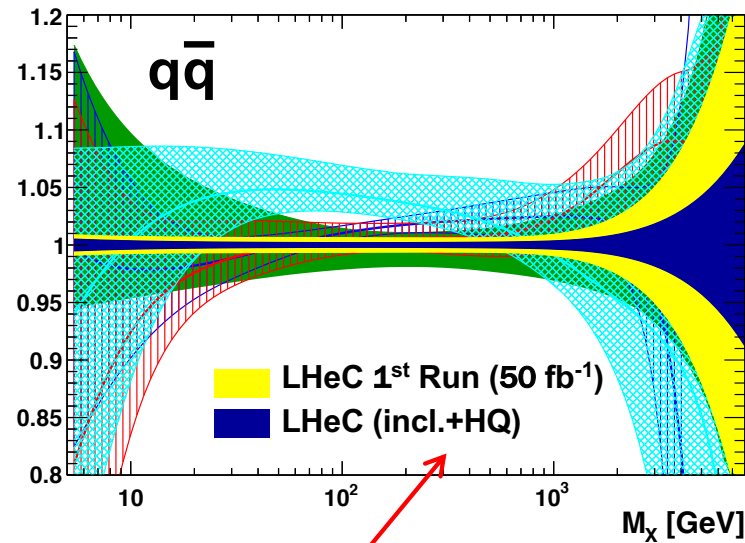
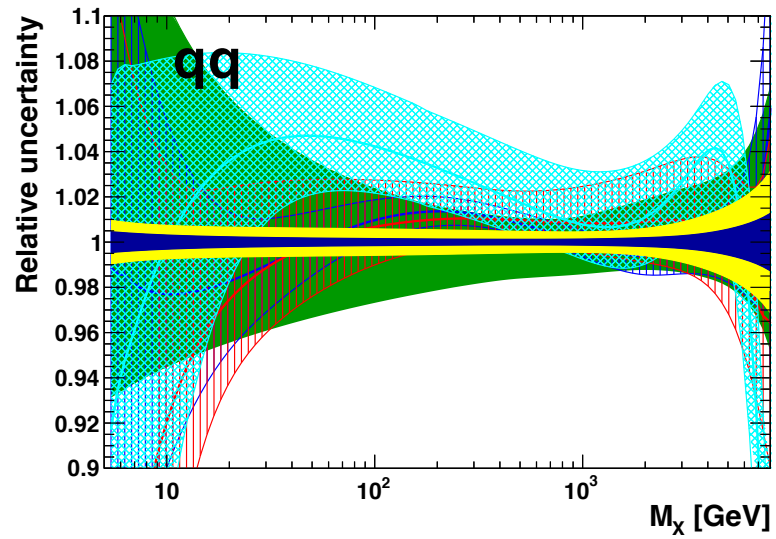
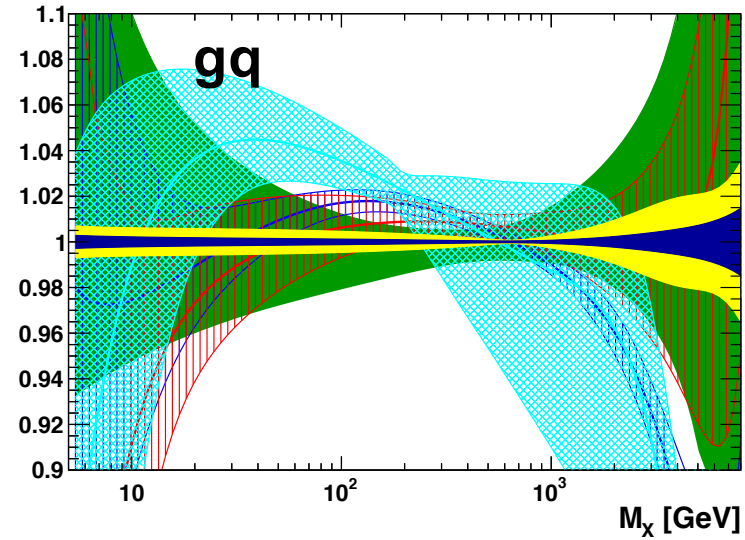
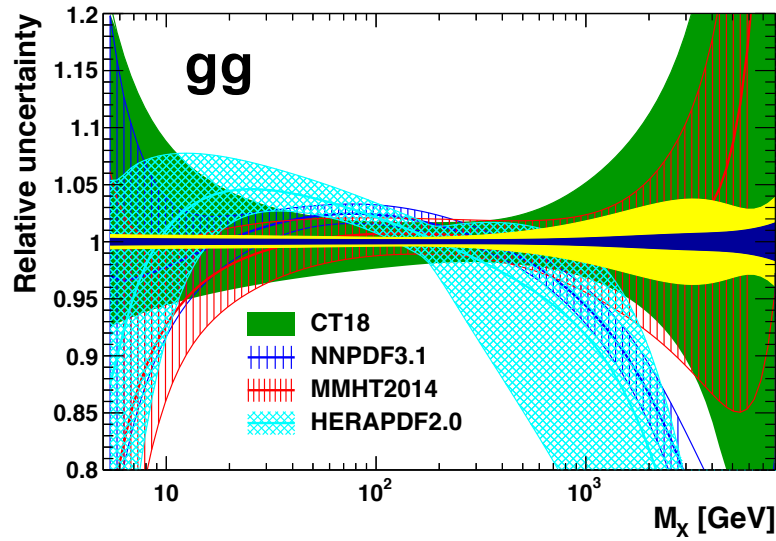
→ **LHeC**: direct sensitivity via charm tagging in $W_s \rightarrow c$
(x, Q^2) mapping of strange density for first time



- **c, b**: enormously extended range and much improved precision c.f. HERA
- **ΔMc = 50 (HERA) to 3 MeV**: impacts on α_s, regulates ratio of charm to light, crucial for precision t, H
- **ΔMb to 10 MeV**; MSSM: Higgs produced dominantly via $b\bar{b} \rightarrow A$



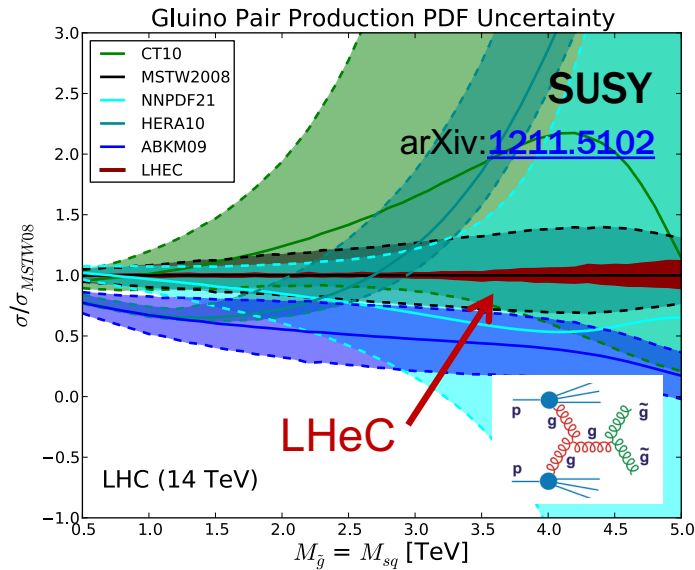
PDF luminosities @ 14 TeV



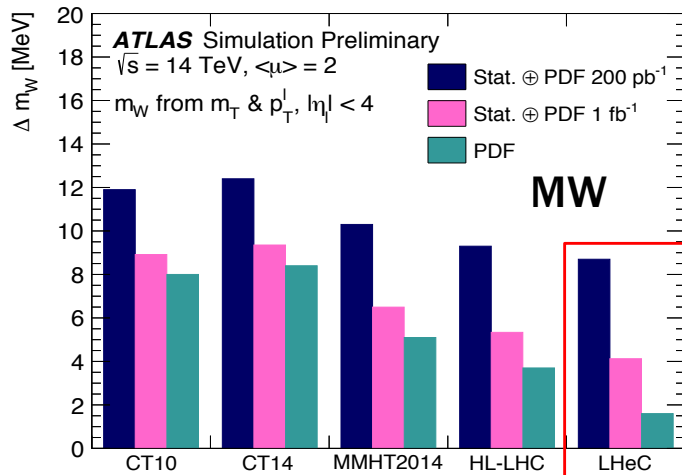
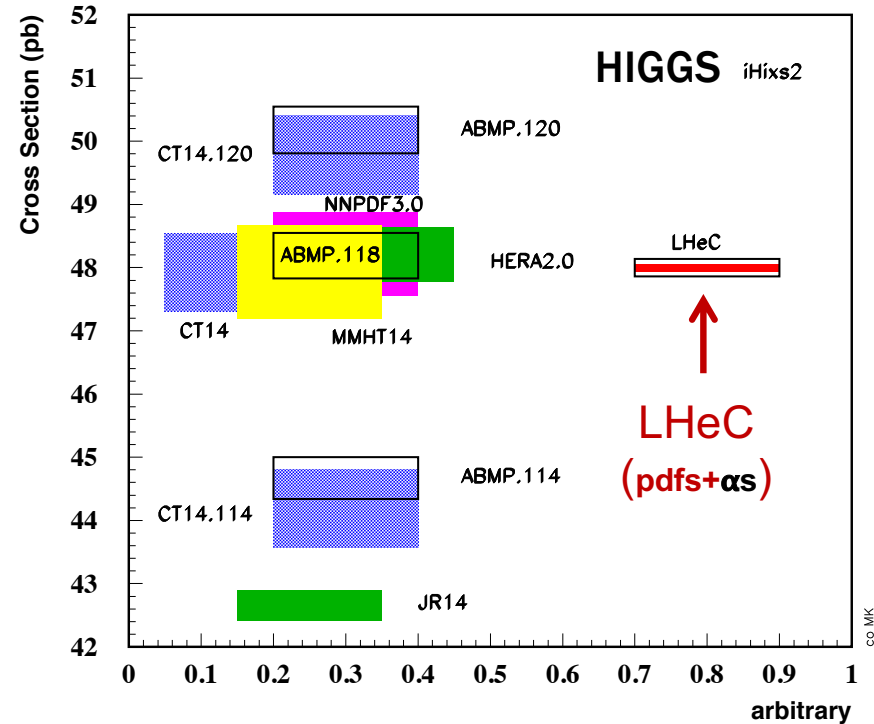
(s,c,b) also included

Empowering the LHC

external, reliable, precise **pdfs** needed for
range extension and interpretation



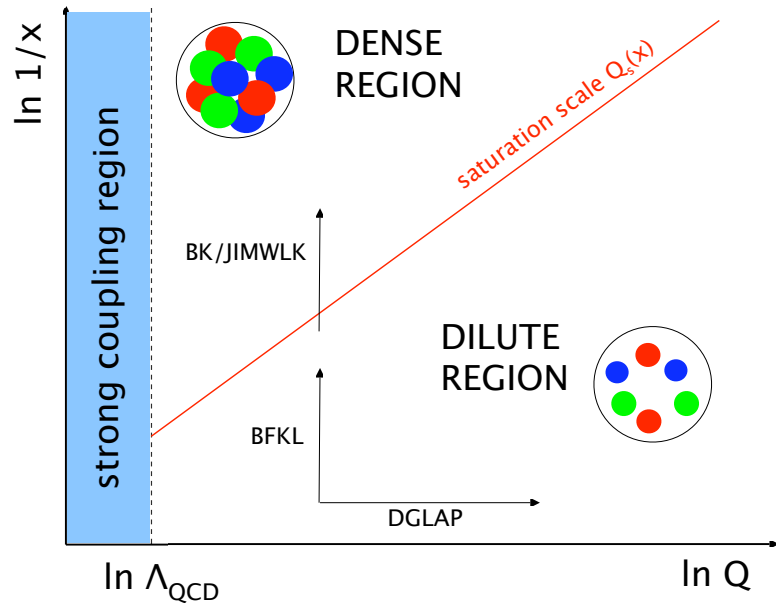
NNNLO pp-Higgs Cross Sections at 14 TeV



CONTACT INTERACTIONS: $\mathcal{L}_{CI} = \frac{g^2}{\Lambda^2} \eta_{ij} (\bar{q}_i \gamma_\mu q_i) (\bar{\ell}_i \gamma^\mu \ell_i)$

Model	ATLAS (Ref. [702])		HL-LHC	
	$\mathcal{L} = 36 \text{ fb}^{-1}$ (CT14nnlo)	$\mathcal{L} = 3 \text{ ab}^{-1}$ (CT14nnlo)	$\mathcal{L} = 3 \text{ ab}^{-1}$ (LHeC)	$\mathcal{L} = 3 \text{ ab}^{-1}$ (LHeC)
LL (constr.)	28 TeV	58 TeV	96 TeV	96 TeV
LL (destr.)	21 TeV	49 TeV	77 TeV	77 TeV
RR (constr.)	26 TeV	58 TeV	84 TeV	84 TeV
RR (destr.)	22 TeV	61 TeV	75 TeV	75 TeV
LR (constr.)	26 TeV	49 TeV	81 TeV	81 TeV
LR (destr.)	22 TeV	45 TeV	62 TeV	62 TeV

Novel small x dynamics



- **small x** – various phenomena may occur which go beyond standard DGLAP QCD evolution:
- **BFKL**, connected to small x resummation of $\log \frac{1}{x}$ terms
- **gluon recombination** → non-linear evolution, parton saturation

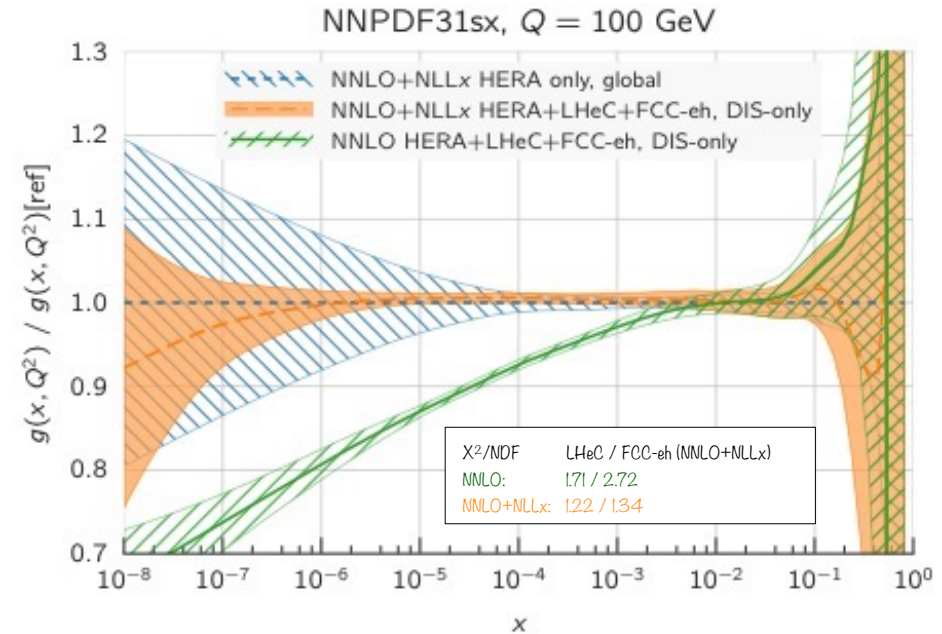
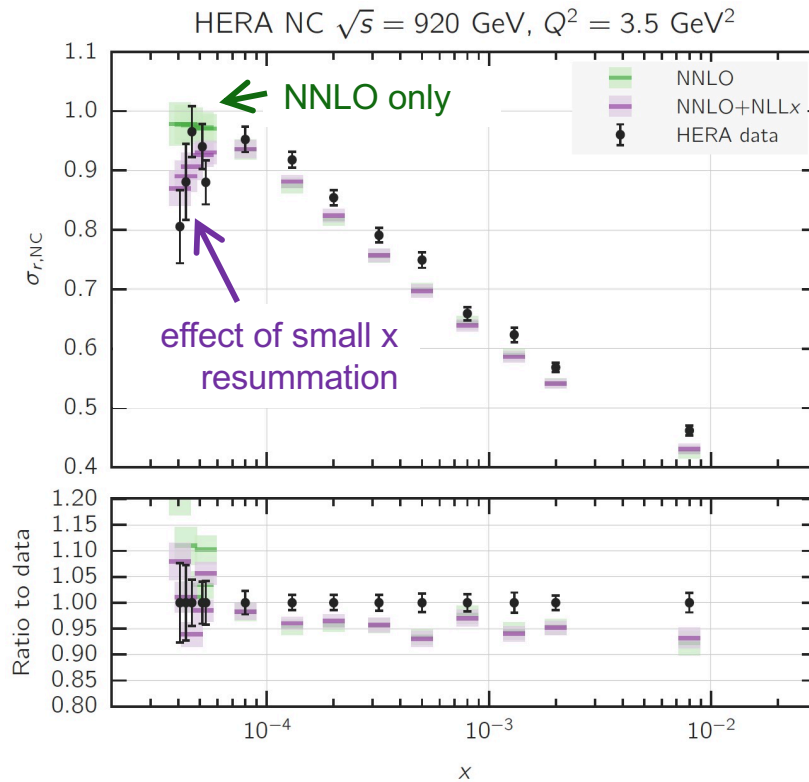
unprecedented opportunity to explore **small x** with **LHeC/FCC-eh**
 ×15/120 extension in 1/x cf. HERA

$\tau = \frac{Q^2}{s}$	Higgs	Z, W	low mass DY	$c\bar{c}$
LHC (13 TeV)	10^{-4}	5×10^{-5}	$\sim 10^{-6}$	$\sim 10^{-7}$
FCC-hh (100 TeV)	1.5×10^{-6}	8×10^{-7}	$\sim 10^{-8}$	$\sim 10^{-9}$

(note: typical values $x_1, x_2 \sim \sqrt{\tau}$)

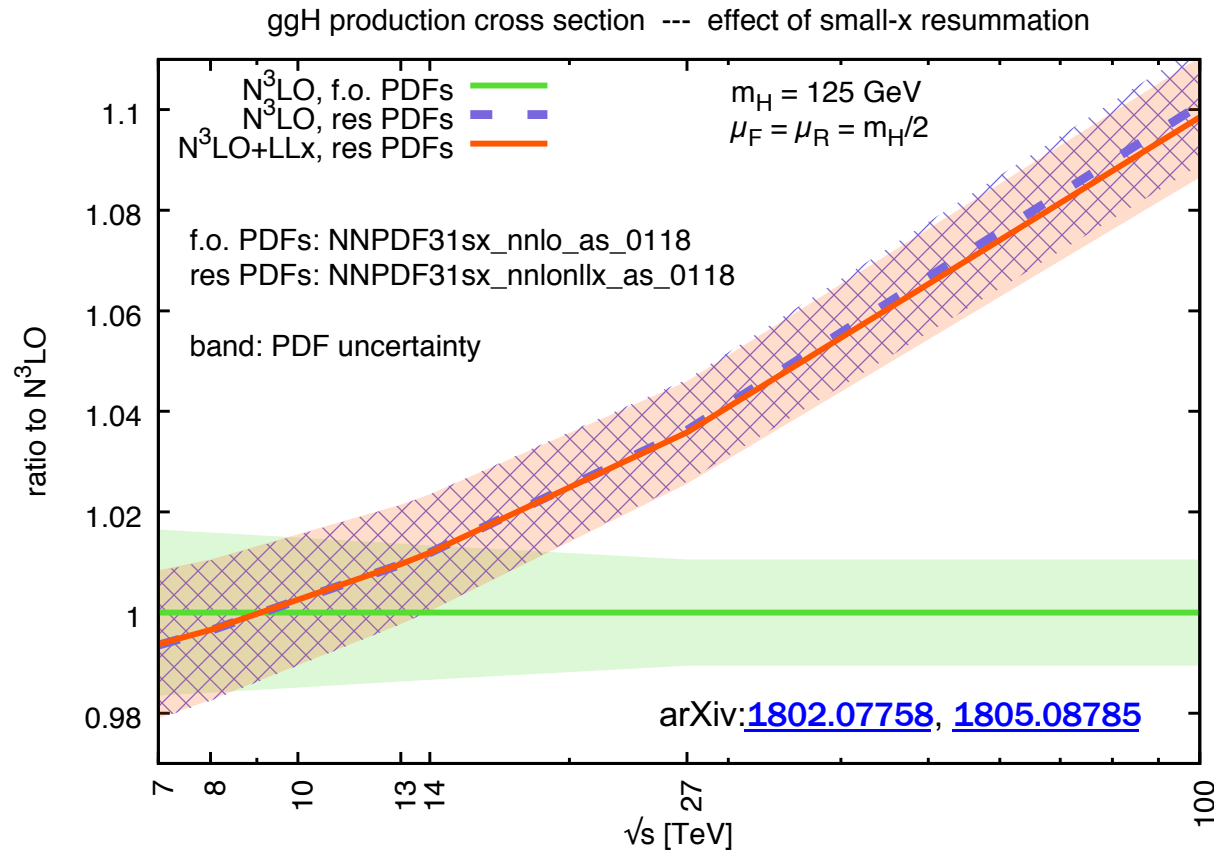
central rapidity ↑

Novel small x dynamics: resummation



- recent evidence for onset of BFKL dynamics in HERA inclusive data,
 - arXiv:[1710.05935](https://arxiv.org/abs/1710.05935); [1802.00064](https://arxiv.org/abs/1802.00064)
- (see also, arXiv:[1604.02299](https://arxiv.org/abs/1604.02299))
- small x resummation mainly affects **gluon pdf** – dramatic effect for $x \leq 10^{-3}$
 - **essential for LHeC and FCC-eh**
 - NB, gluon pdf obtained with small x resummation grows more quickly – **saturation** at some point!

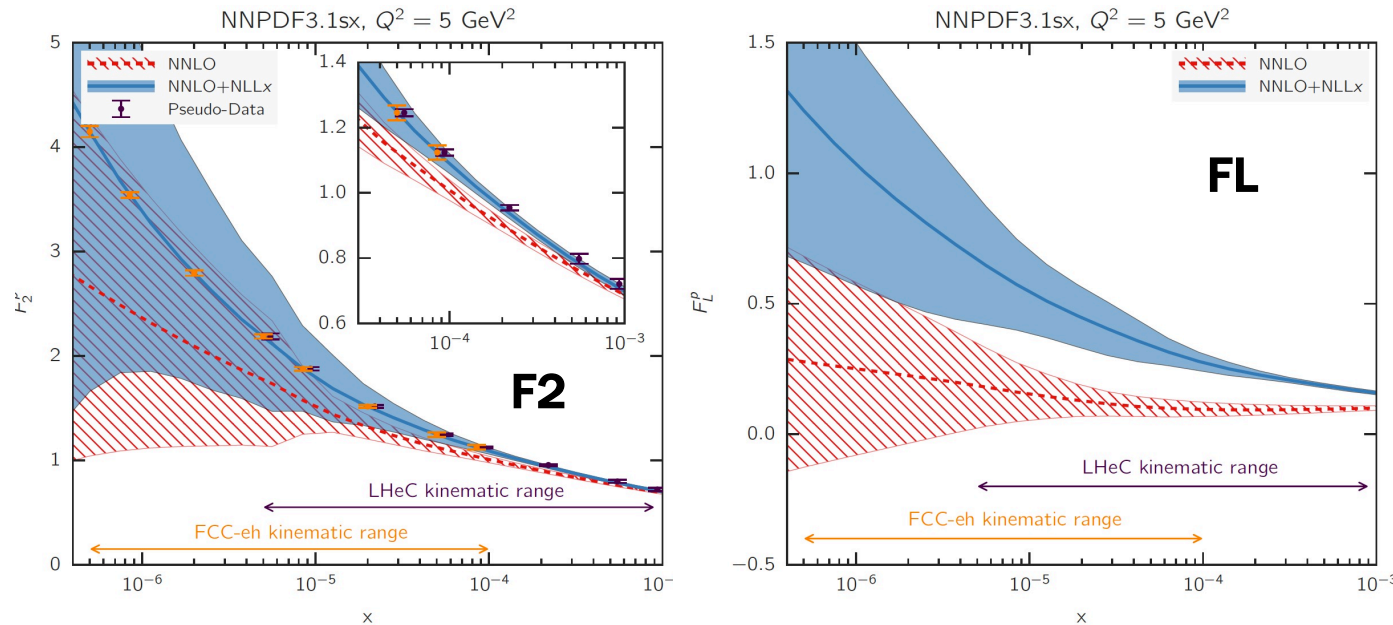
Impact on pp phenomenology



- effect of small x resummation on $gg \rightarrow H$ cross section for LHC, HE-LHC, FCC
- **significant impact, especially at ultra low x values probed at FCC**

(see also recent work on forward Higgs production, arXiv: [2011.03193](https://arxiv.org/abs/2011.03193); other processes in progress)

LHeC sensitivity to small x



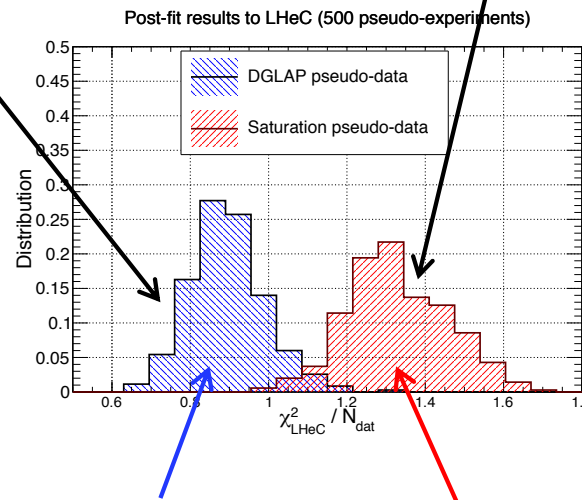
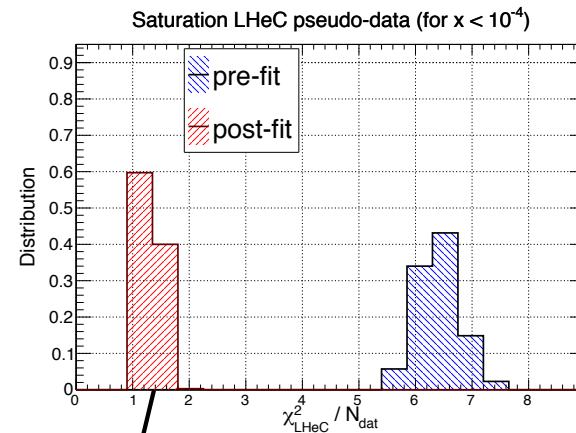
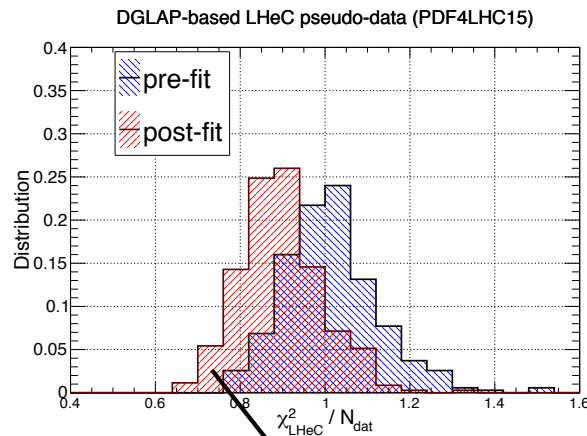
NC cross section:
$$\sigma_{r,\text{NC}} = F_2(x, Q^2) - \frac{y^2}{1 + (1 - y)^2} F_L(x, Q^2) \quad y = \frac{Q^2}{x s}$$

- LHeC and FCC-eh have unprecedented kinematic reach to **small x** ; very large sensitivity and discriminatory power to pin down details of **small x QCD dynamics**
- measurement of F_L has a significant role to play, arXiv:[1802.04317](https://arxiv.org/abs/1802.04317)

Novel dynamics at small x: saturation



- with the unprecedented small-x reach, **gluon recombination / parton saturation may also be expected**, manifesting as deviation from linear DGLAP



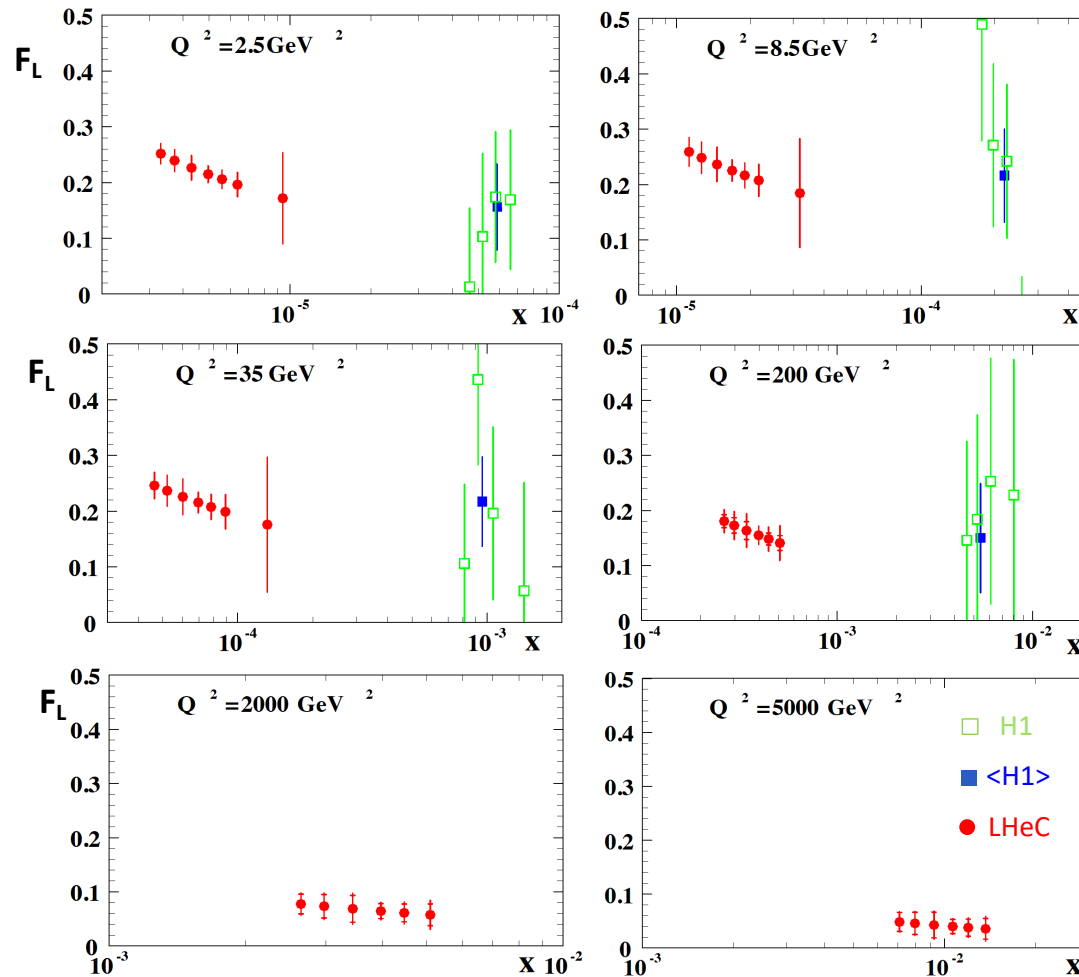
pre- and post-fit χ^2 distributions consistent for DGLAP pseudo-data fitted with DGLAP

pre- and post-fit distributions very different for DGLAP fit to saturation-based ($x \leq 10^{-4}$, GBW model) pseudo-data

DGLAP can not absorb all saturation effects

LHeC can distinguish between **DGLAP** and **saturation**

Longitudinal Structure Function



simulated for:
 $E_p = 7 \text{ TeV}$ and
 $E_e = 60, 30, 20 \text{ GeV}$

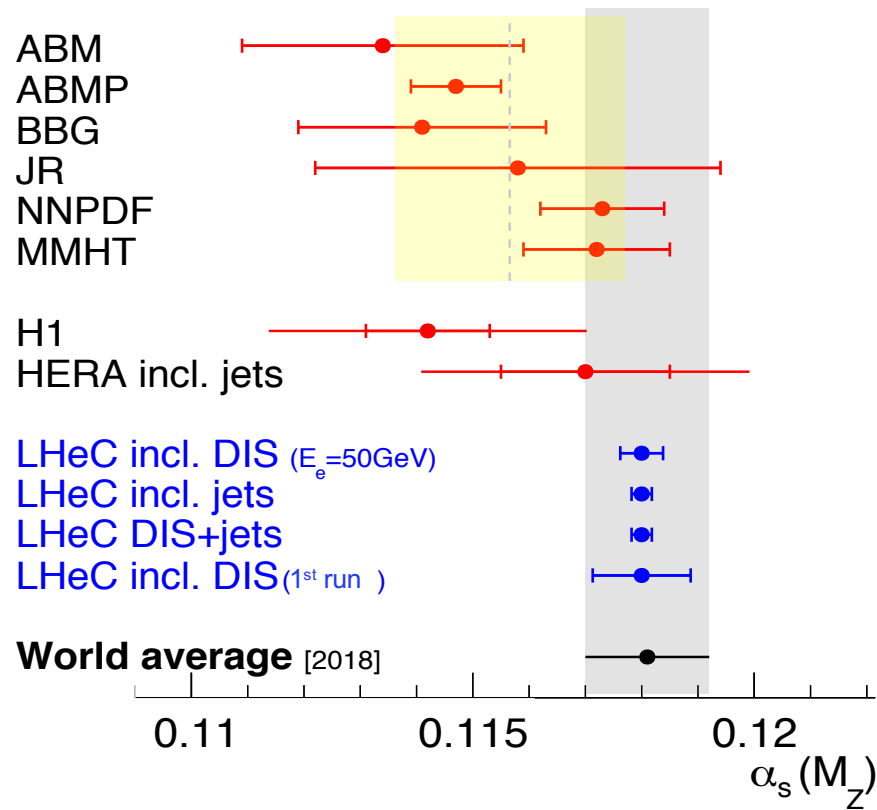
integrated luminosity:
 $10, 1, 1 \text{ fb}^{-1}$

measurement
dominated by
systematics

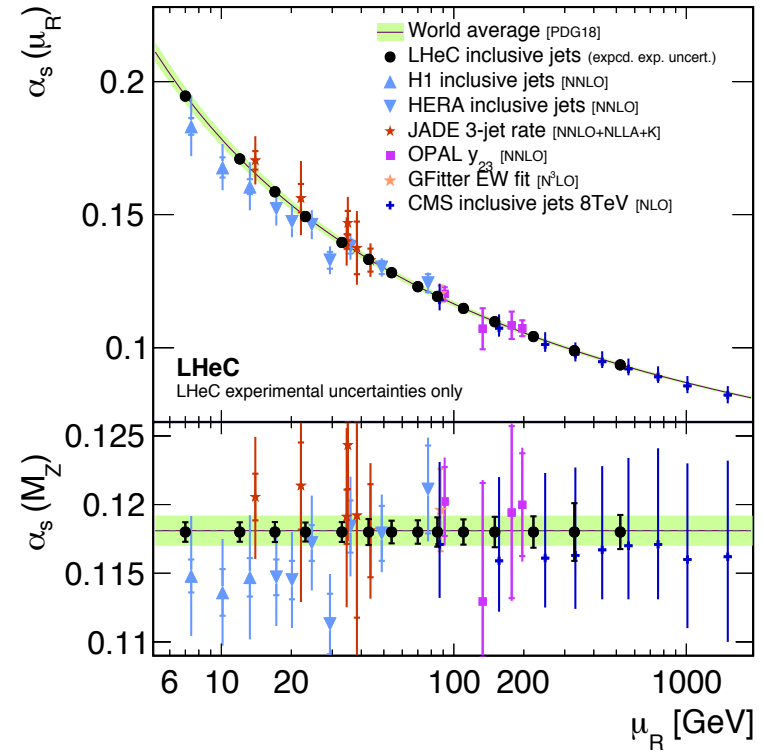
- simultaneous measurement of F_2 and F_L is clean way to pin down dynamics at small x

Strong Coupling

α_s determinations at NNLO QCD:



fit to subsets of ep jet data



- α_s is least known coupling constant
- current state-of-the-art: $\delta\alpha_s/\alpha_s = \mathcal{O}(1\%)$
- achievable precision at **LHeC** $\mathcal{O}(0.1\%)$

- α_s running testable over two orders of magnitude in scale

Summary

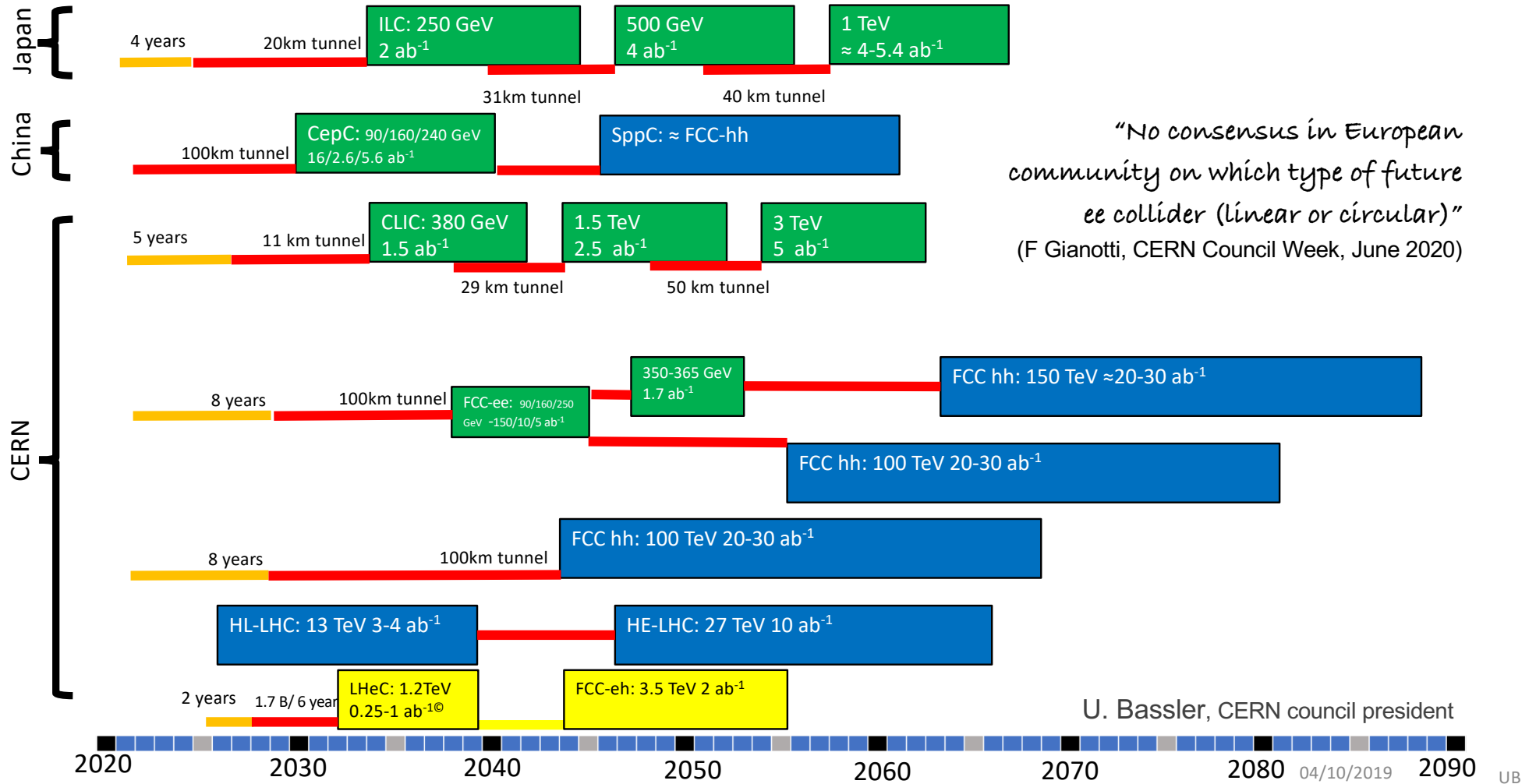
- energy frontier **electron-proton colliders** essential for full exploitation of current and future hadron colliders (Higgs, BSM, electroweak, ...)
 - **external precision pdf input**; complete q,g unfolding, high luminosity $x \rightarrow 1$, s, c, b, (t); N3LO; small x; strong coupling to permille precision; ...
 - LHeC CDR update (arXiv:[2007.14491](https://arxiv.org/abs/2007.14491)) summarises wealth of new and updated studies
 - enormously rich physics programme both in **own right**, and for **transformation of proton-proton machines** into precision facilities
 - **all critical pdf information can be obtained early** ($\sim 50 \text{ fb}^{-1} \equiv \times 50$ HERA), in parallel with HL-LHC operation
 - unprecedented access to novel kinematic regime, with **unique potential to explore small x phenomena**
 - **α_s to permille experimental precision** also achievable early, with use of inclusive DIS and/or jets
- ... and much more in realm of **QCD** and **small x** physics; EG. no time to cover **diffractive**, **vector meson**, **γp** , ...

Extras

Possible scenarios of future colliders

- Proton collider
- Electron collider
- Electron-Proton collider

- Construction/Transformation: heights of box construction cost/year
- Preparation



→ LHeC: installation during LS4;

concurrent operation through LHC Runs 5/6; and period of dedicated running, arXiv:1810.13022

LHeC simulated data

Source of uncertainty	Uncertainty
Scattered electron energy scale $\Delta E'_e/E'_e$	0.1 %
Scattered electron polar angle	0.1 mrad
Hadronic energy scale $\Delta E_h/E_h$	0.5 %
Radiative corrections	0.3 %
Photoproduction background (for $y > 0.5$)	1 %
Global efficiency error	0.5 %

Table 3.1: Assumptions used in the simulation of the NC cross sections on the size of uncertainties from various sources. The top three are uncertainties on the calibrations which are transported to provide correlated systematic cross section errors. The lower three values are uncertainties of the cross section caused by various sources.

Parameter	Unit	Data set								
		D1	D2	D3	D4	D5	D6	D7	D8	D9
Proton beam energy	TeV	7	7	7	7	1	7	7	7	7
Lepton charge		-1	-1	-1	-1	-1	+1	+1	-1	-1
Longitudinal lepton polarisation		-0.8	-0.8	0	-0.8	0	0	0	+0.8	+0.8
Integrated luminosity	fb ⁻¹	5	50	50	1000	1	1	10	10	50

Table 3.2: Summary of characteristic parameters of data sets used to simulate neutral and charged current e^\pm cross section data, for a lepton beam energy of $E_e = 50$ GeV. Sets D1-D4 are for $E_p = 7$ TeV and e^-p scattering, with varying assumptions on the integrated luminosity and the electron beam polarisation. The data set D1 corresponds to possibly the first year of LHeC data taking with the tenfold of luminosity which H1/ZEUS collected in their lifetime. Set D5 is a low Ep energy run, essential to extend the acceptance at large x and medium Q^2 . D6 and D7 are sets for smaller amounts of positron data. Finally, D8 and D9 are for high energy e^-p scattering with positive helicity as is important for electroweak NC physics. These variations of data taking are subsequently studied for their effect on PDF determinations.

LHeC pdf parameterisation

- QCD fit ansatz based on HERAPDF2.0, with following differences:
- no requirement that $\bar{u}=\bar{d}$ at small x
- no negative gluon term (only for the aesthetics of ratio plots – it has been checked that this does not impact size of projected uncertainties)

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} (1 + D_g x)$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2)$$

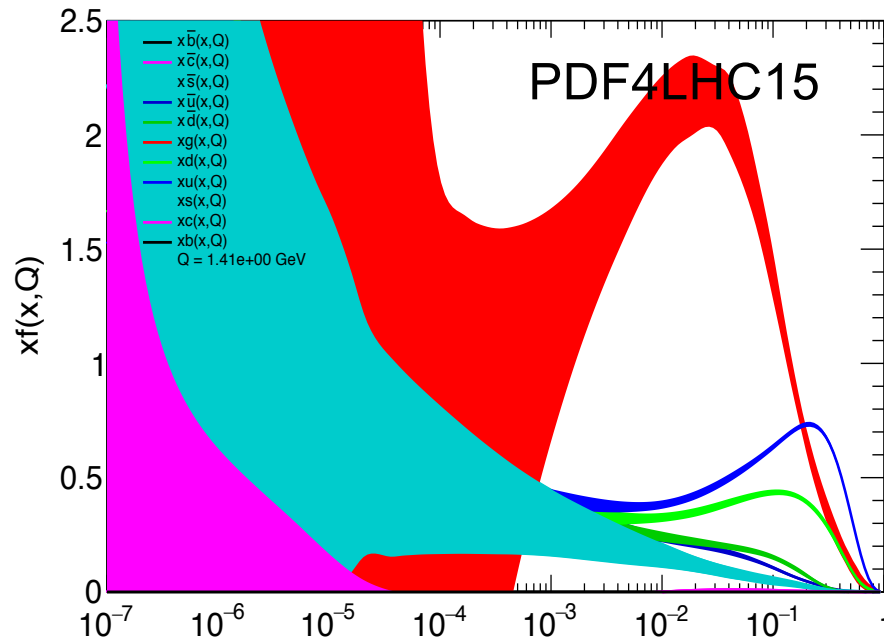
$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}}$$

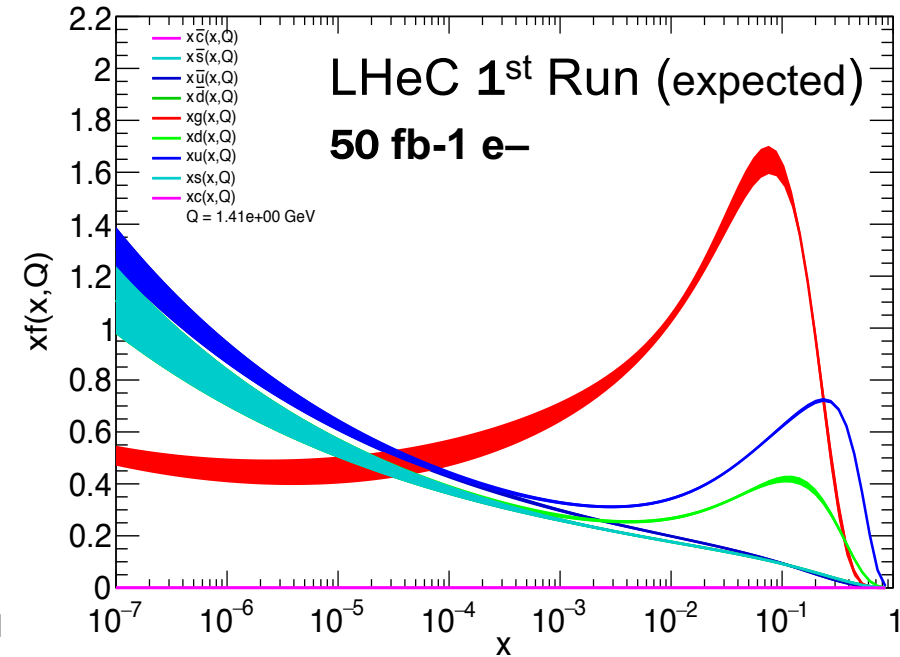
$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}$$

- **4+1 pdf fit (above) has 14 free parameters**
- **5+1 pdf fit for HQ studies parameterises \bar{d} and \bar{s} separately, 17 free parameters**

Summary of LHeC pdfs



situation today

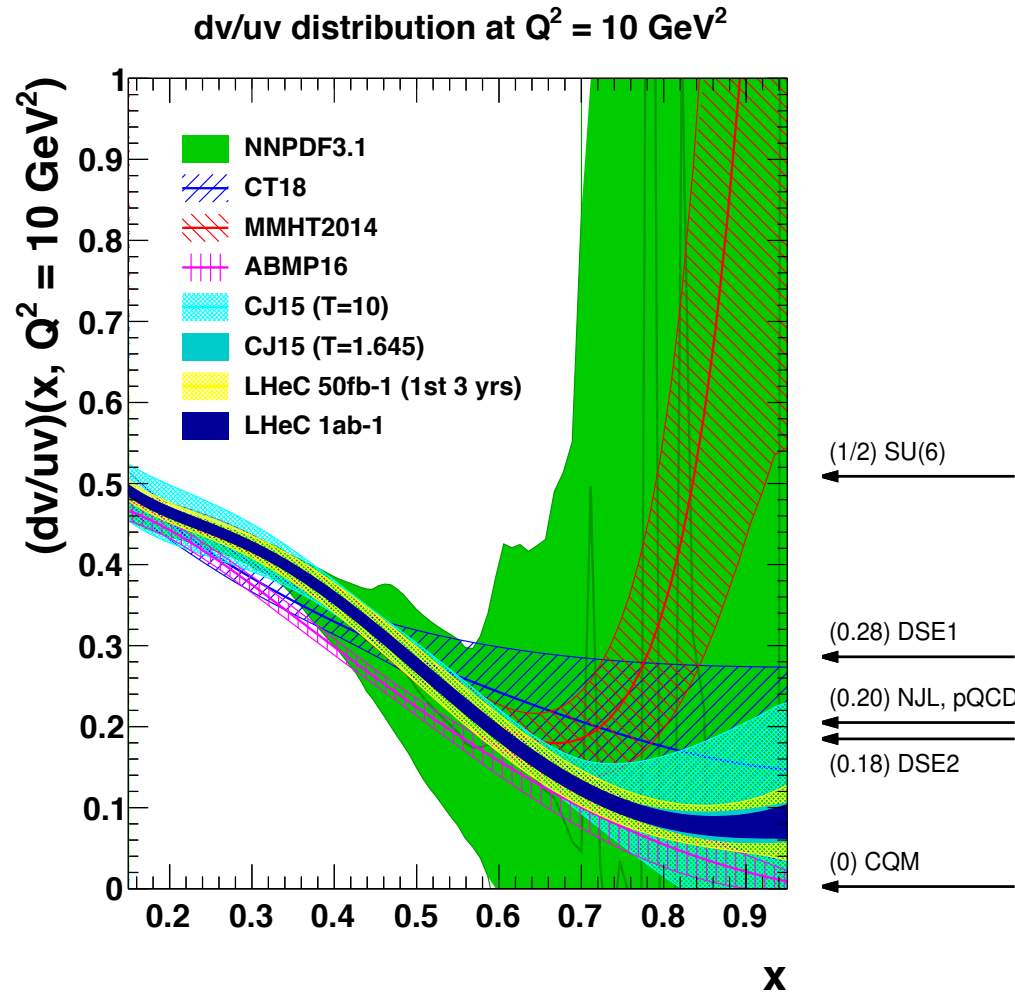


after 1st LHeC Run

with further improvements after full running period, plus HQs, (DIS jets, ...)

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d/u at large x

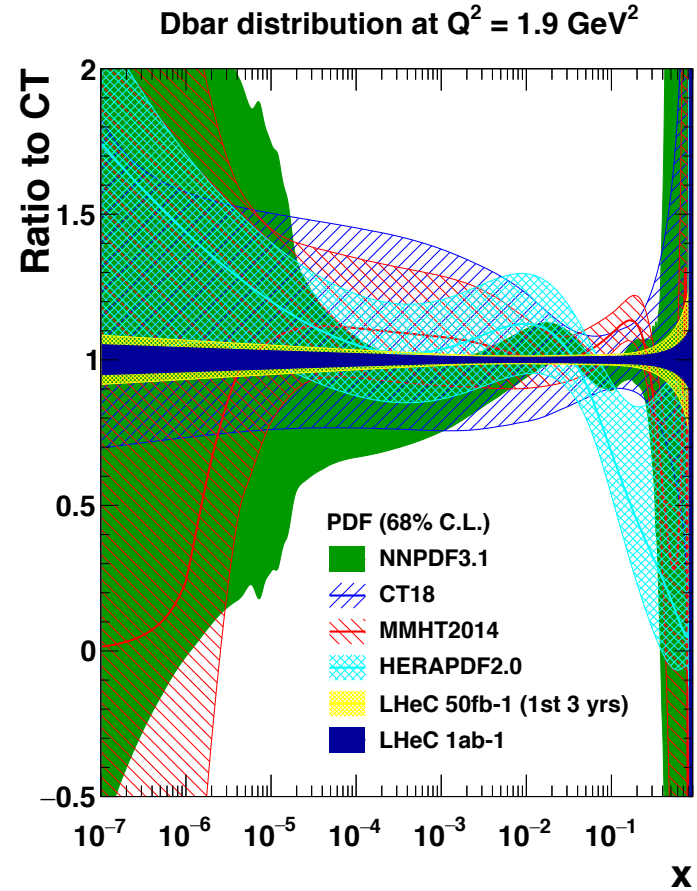
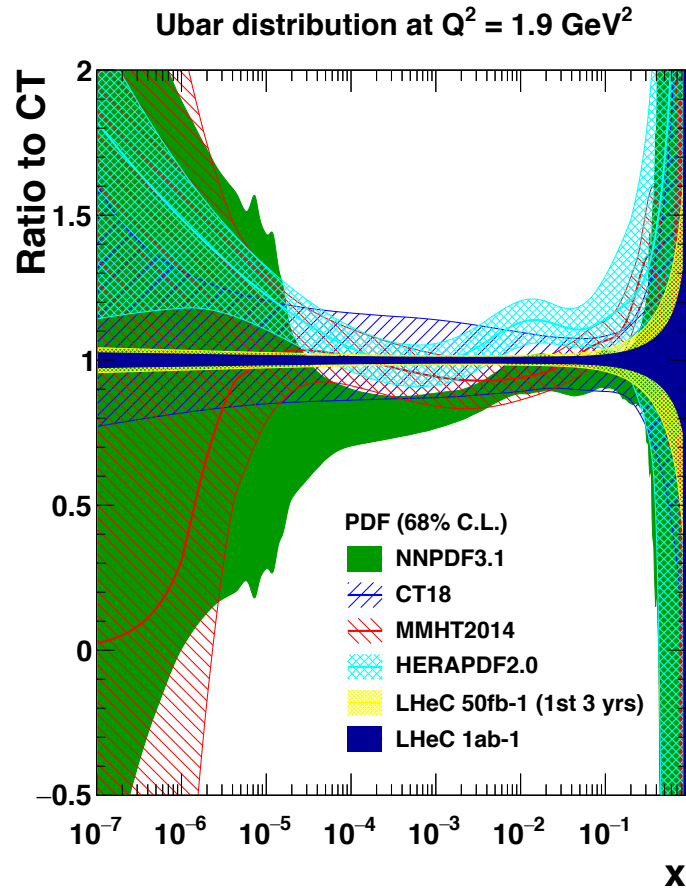


d/u essentially unknown at large x

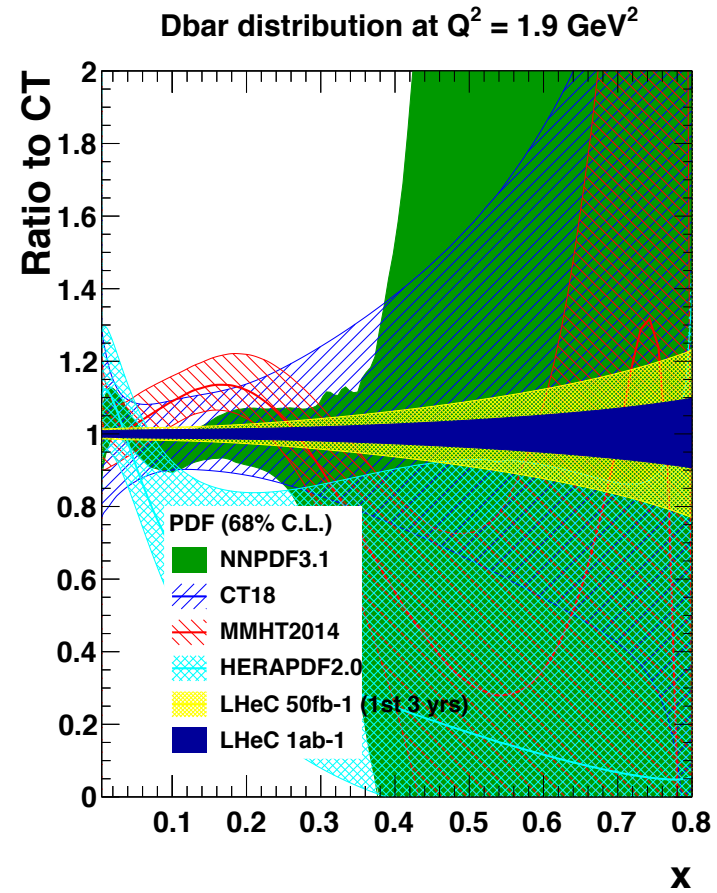
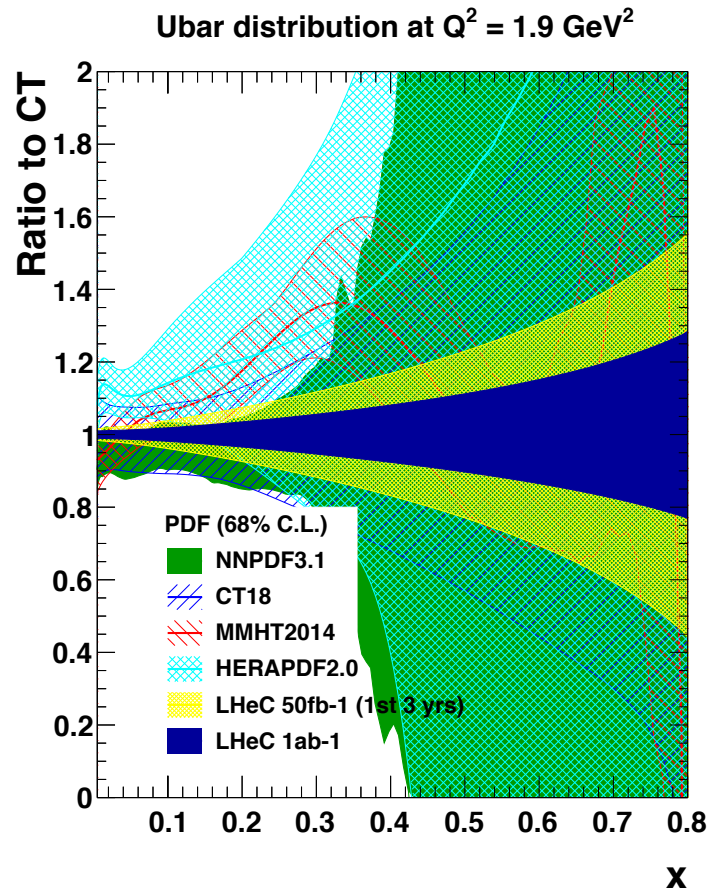
no predictive power from current pdfs;
conflicting theory pictures;
data inconclusive, large nuclear uncertainties

can resolve long-standing mystery of d/u ratio at large x

Sea quarks



Sea quarks



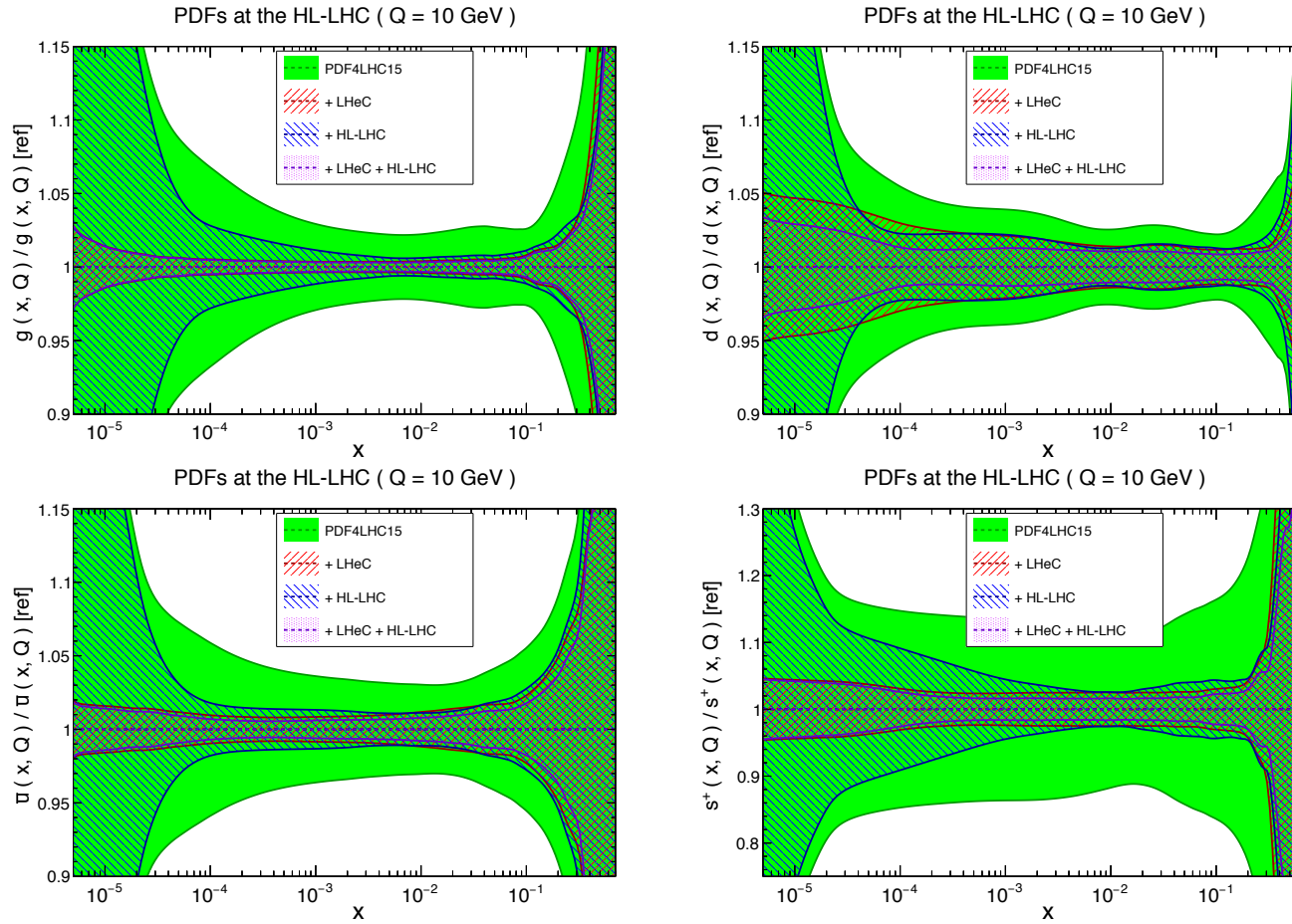


Figure 9.9: Impact of LHeC on the $1\text{-}\sigma$ relative PDF uncertainties of the gluon, down quark, anti-up quark and strangeness distributions, with respect to the PDF4LHC15 baseline set (green band). Results for the LHeC (red), the HL-LHC (blue) and their combination (violet) are shown.

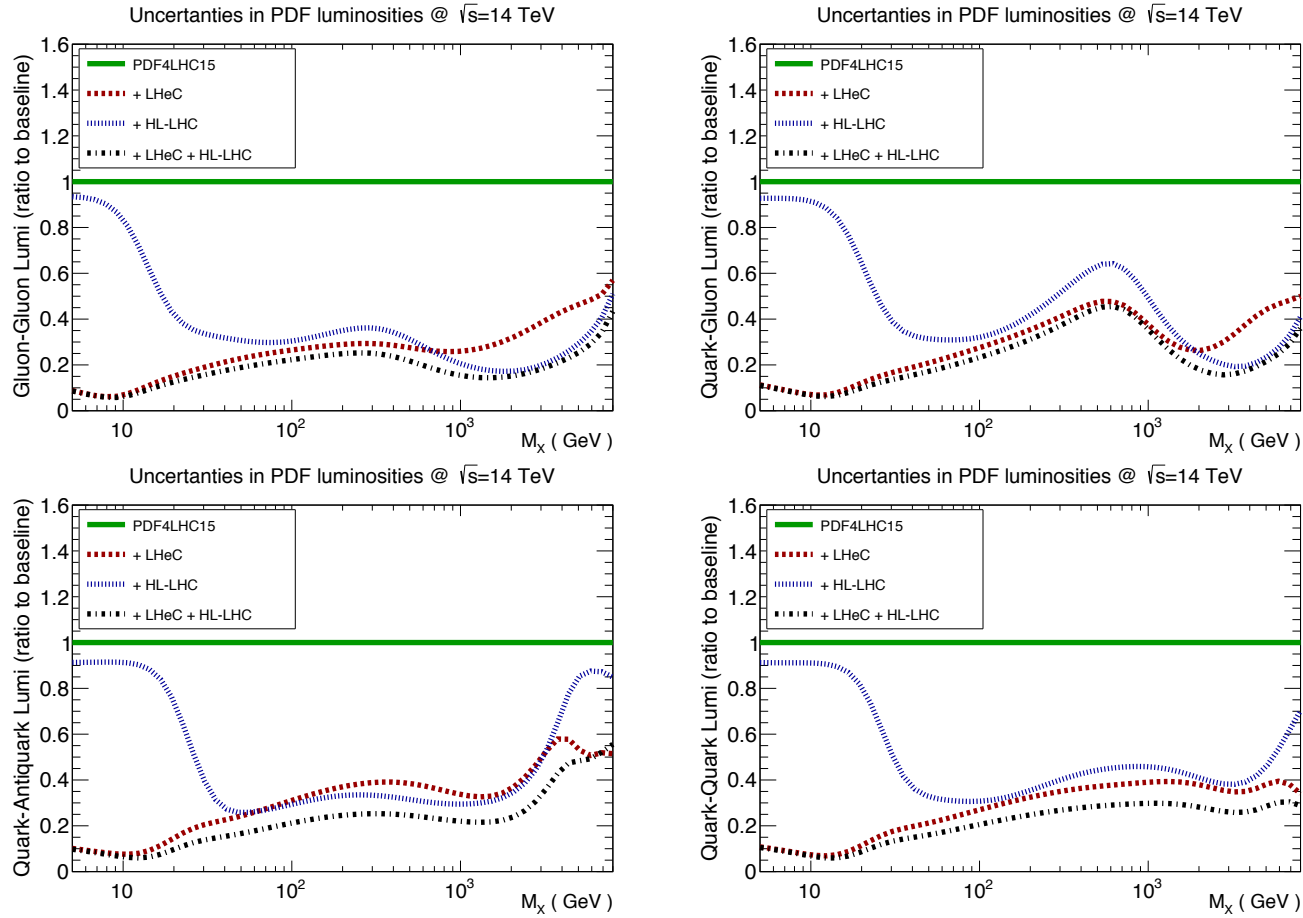
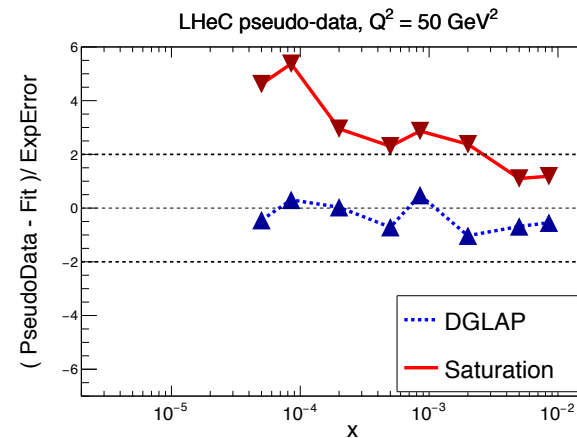
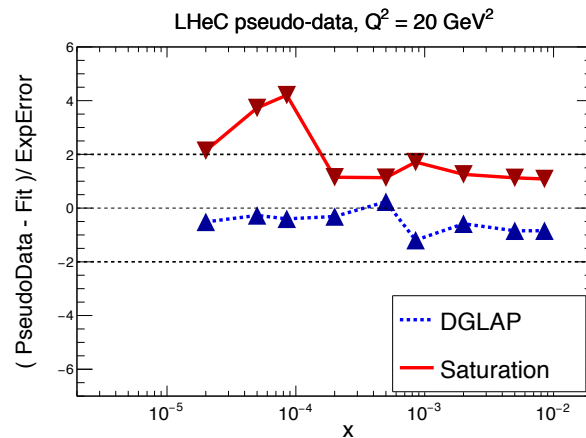
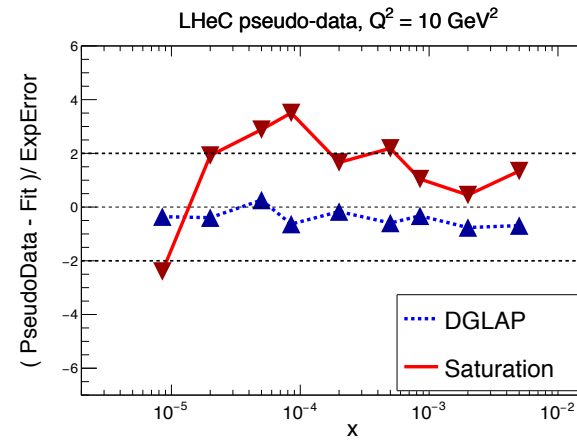
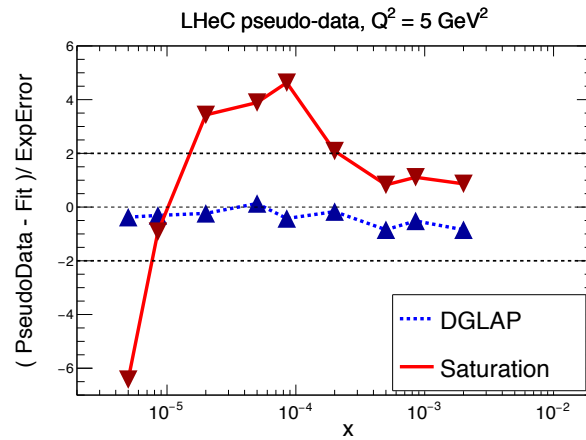


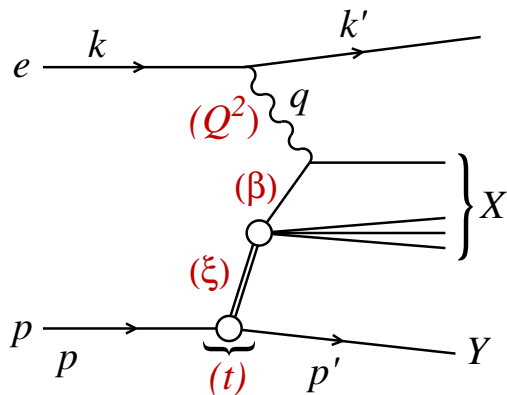
Figure 9.10: Impact of LHeC, HL-LHC and combined LHeC + HL-LHC pseudodata on the uncertainties of the gluon-gluon, quark-gluon, quark-antiquark and quark-quark luminosities, with respect to the PDF4LHC15 baseline set. In this comparison we display the relative reduction of the PDF uncertainty in the luminosities compared to the baseline.

Novel small x dynamics: saturation



- inspect **PULLS** to highlight origin of worse agreement: **in saturation case (fitted with DGLAP), theory wants to overshoot data at smallest x, and undershoot at higher x**
- while a different x dependence might be absorbed into PDFs at scale Q_0 , this is not possible with a Q^2 dependence – **large Q^2 lever arm crucial**

Diffraction



Longitudinal momentum fraction of the Pomeron w.r.t hadron

$$\xi \equiv x_{IP} = \frac{Q^2 + M_X^2 - t}{Q^2 + W^2}$$

Longitudinal momentum fraction of the parton w.r.t Pomeron

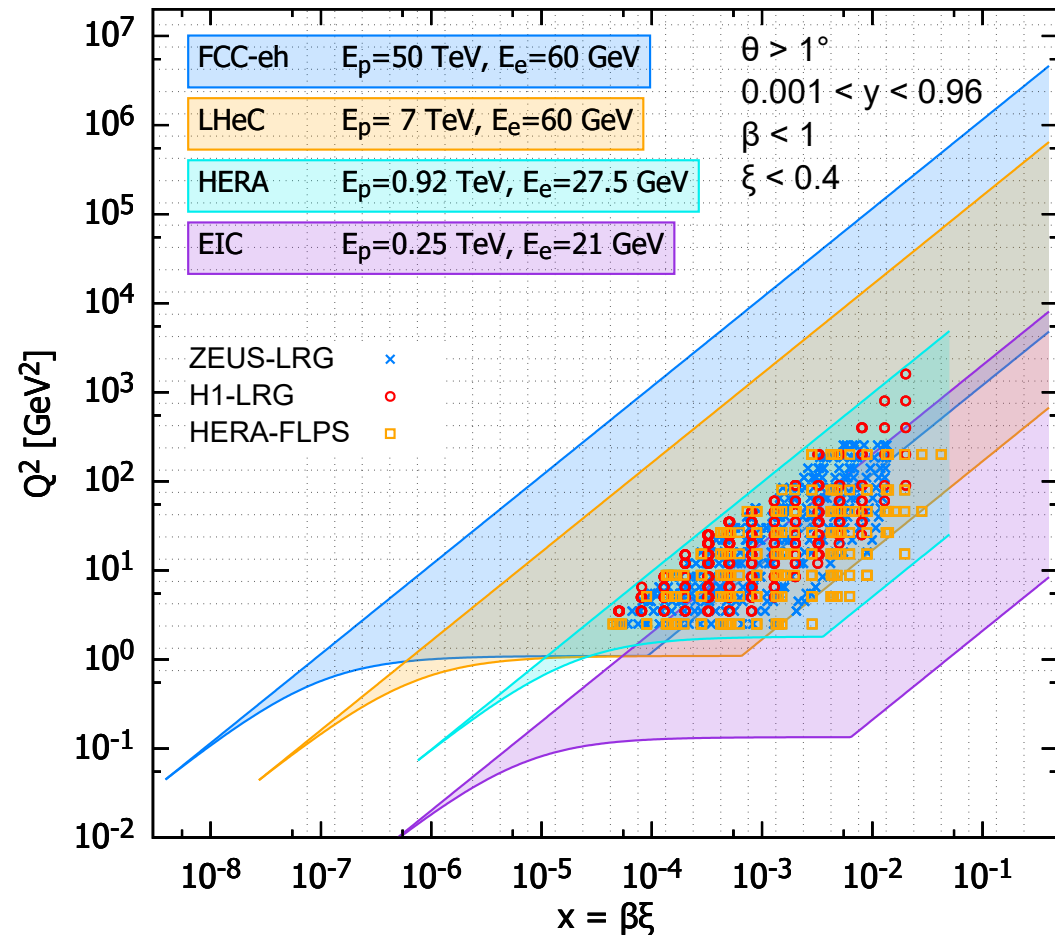
$$\beta = \frac{Q^2}{Q^2 + M_X^2 - t}$$

4-momentum transfer squared

$$t = (p - p')^2$$

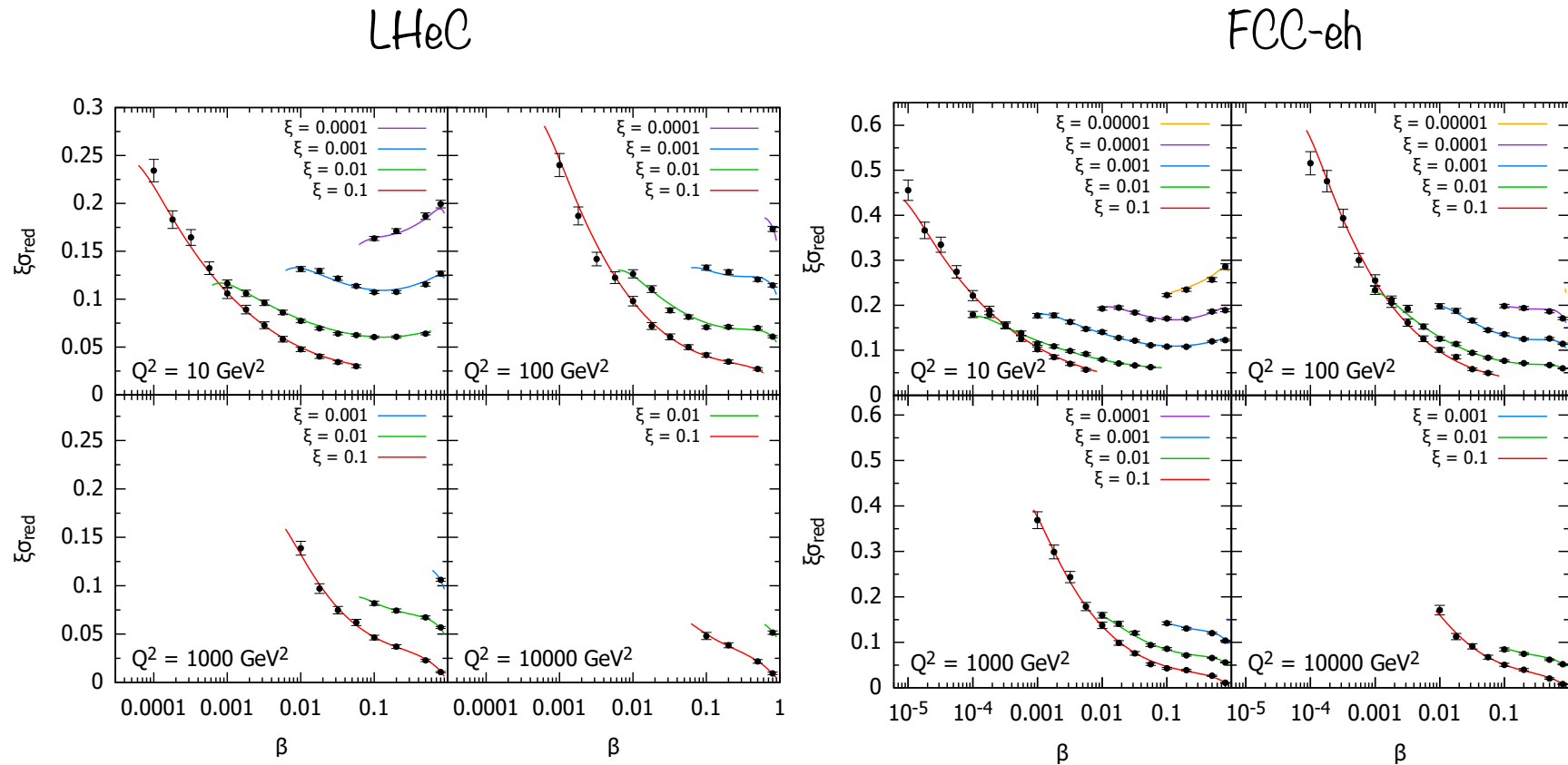
Bjorken x relation

$$x_{Bj} = x_{IP}\beta$$



- inclusive diffraction, constraints on diffractive pdfs, new final states in diffraction, also EW exchange

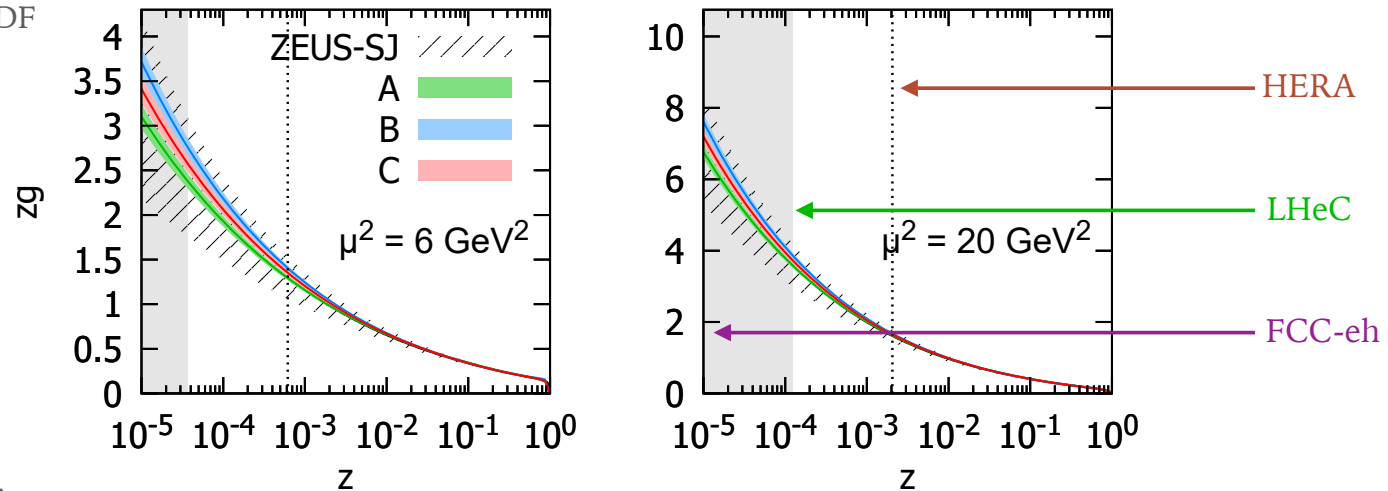
Diffraction σ_{red} pseudo-data



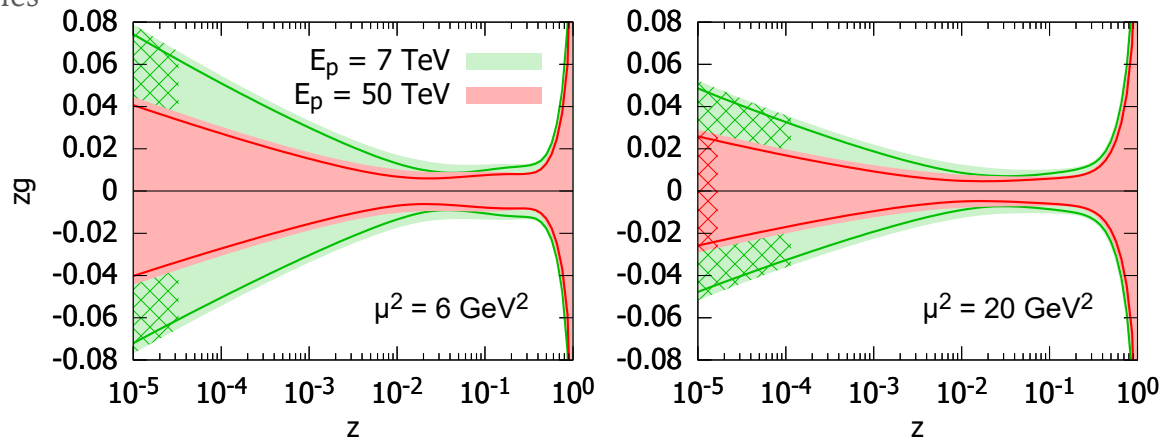
- potential for high quality data for inclusive diffraction at **LHeC/FCC-eh** (only small subset of simulated data shown)
- prospects for precise extraction of **diffraction pdfs, tests of factorisation breaking** (soft and collinear)

Diffractive PDFs from simulation

Diffractive gluon PDF

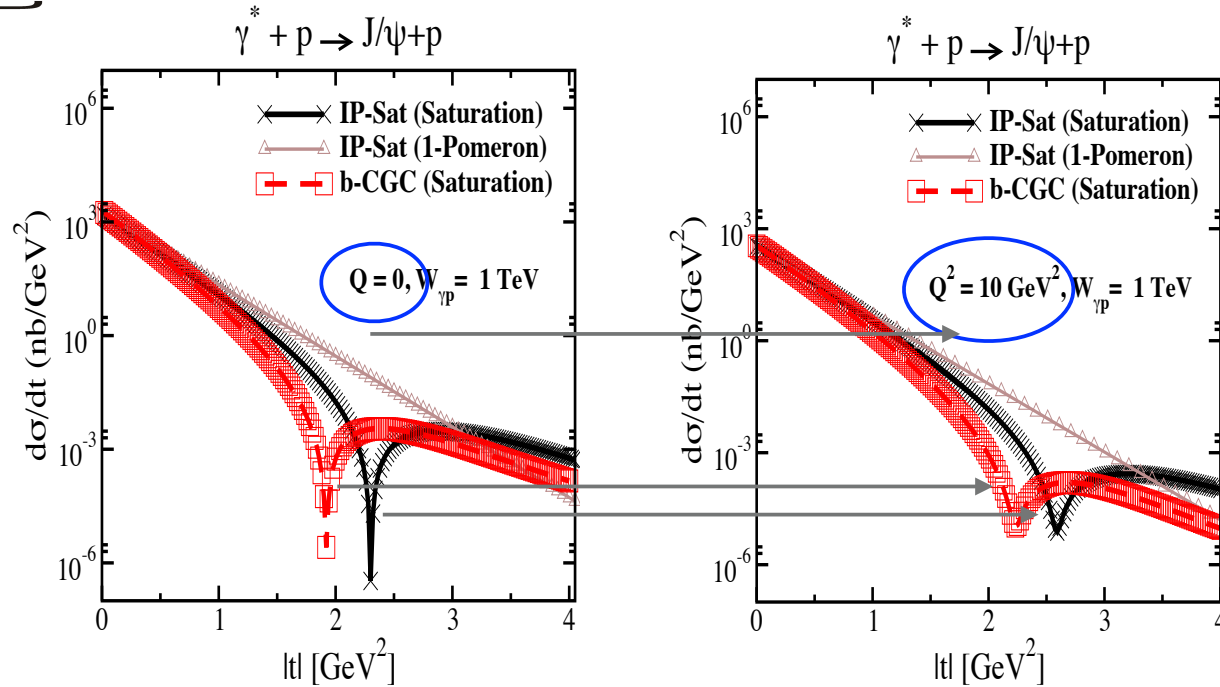
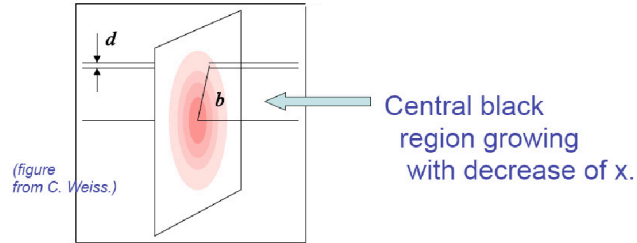
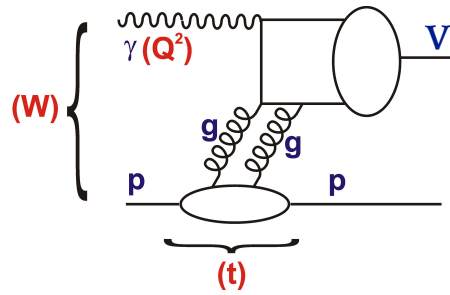


Relative uncertainties



Reduction of DPDF uncertainty by factor 5 — 7 at LHeC and 10 — 15 at FCC-eh with inclusive data alone
 Prospects for precise extraction of diffractive PDFs, tests of factorization breaking (collinear and soft)

Elastic diffraction of vector mesons



Advantage over UPC:

Q^2 dependence

- one of the best processes to test for novel small x dynamics