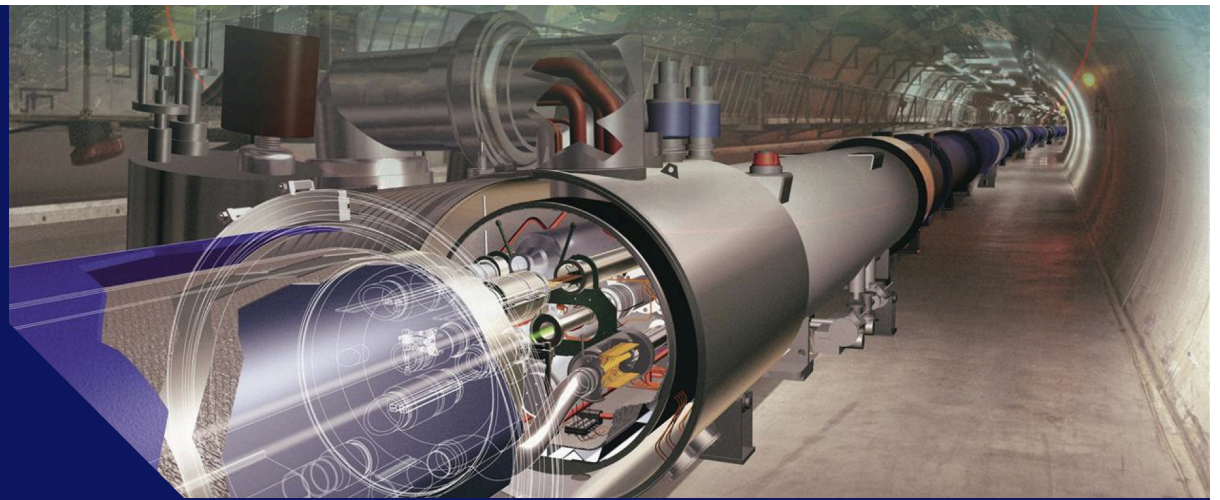


PDF4LHC

IPPP, Durham

17 – 18 Sept. 2019

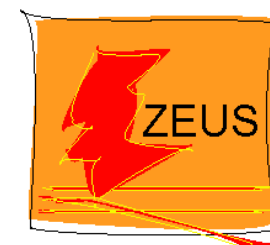


# HERAPDF2.0Jets NNLO

completion of the HERAPDF2.0 family of PDFs  
and extraction of  $\alpha_s(M_Z)$

Claire Gwenlan, Oxford

on behalf of the  
H1, ZEUS, NNLOJet and APPLfast  
collaborations



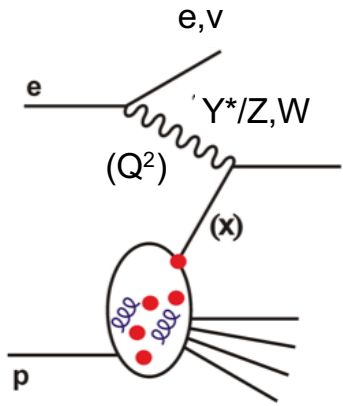
# overview

[H1prelim-19-041](#)

[ZEUS-prel-19-001](#)

- **completing the HERAPDF2.0 family of PDFs**
- previously produced (arXiv: [1506.06042](#)): HERAPDF2.0LO, NLO and NNLO;  
**HERAPDF2.0Jets were only at NLO**
- **HERAPDF2.0Jets updated here with NNLO jet predictions from NNLOJet, as implemented in APPLfast**
- plus addition of new H1 low  $Q^2$  jet data
- **NEW** PDFs at NNLO QCD for  $\alpha_s(M_Z)=0.118$  and  $0.115$
- **PLUS** free  $\alpha_s(M_Z)$  fit, with preferred value significantly lower at NNLO than at NLO
- **NNLO:**  
$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008 \text{ (exp)}_{-0.0005}^{+0.0002} \text{ (model/par.)} \pm 0.0006 \text{ (had)} \pm 0.0027 \text{ (scale)}$$
- **NLO result, as published:**  
$$\alpha_s(M_Z^2) = 0.1183 \pm 0.0009 \text{ (exp)} \pm 0.0005 \text{ (model/par.)} \pm 0.0012 \text{ (had)}_{-0.0030}^{+0.0037} \text{ (scale)}$$

# HERA and DIS



o Kinematic variables:  
 $Q^2 = -q^2 = -(k - k')^2$  Virtuality of the exchanged boson  
 $x = \frac{Q^2}{2p \cdot q}$  Bjorken scaling parameter  
 $y = \frac{p \cdot q}{p \cdot k}$  Inelasticity parameter  
 $s = (k + p)^2 = \frac{Q^2}{xy}$  Invariant c.o.m.

Neutral Current:

LO expressions

$$\frac{d^2\sigma_{NC}^\pm}{dx dQ^2} = \frac{2\alpha\pi^2}{xQ^4} (Y_+ F_2 \mp Y_- xF_3 - y^2 F_L)$$

$$F_2 \sim \sum_i e_i^2 (xq_i + x\bar{q}_i) \quad xF_3 \sim \sum_i (xq_i - x\bar{q}_i) \quad F_L \sim \alpha_s \times g$$

quarks pdfs      valence quarks      gluon via  $\mathcal{O}(\alpha_s)$

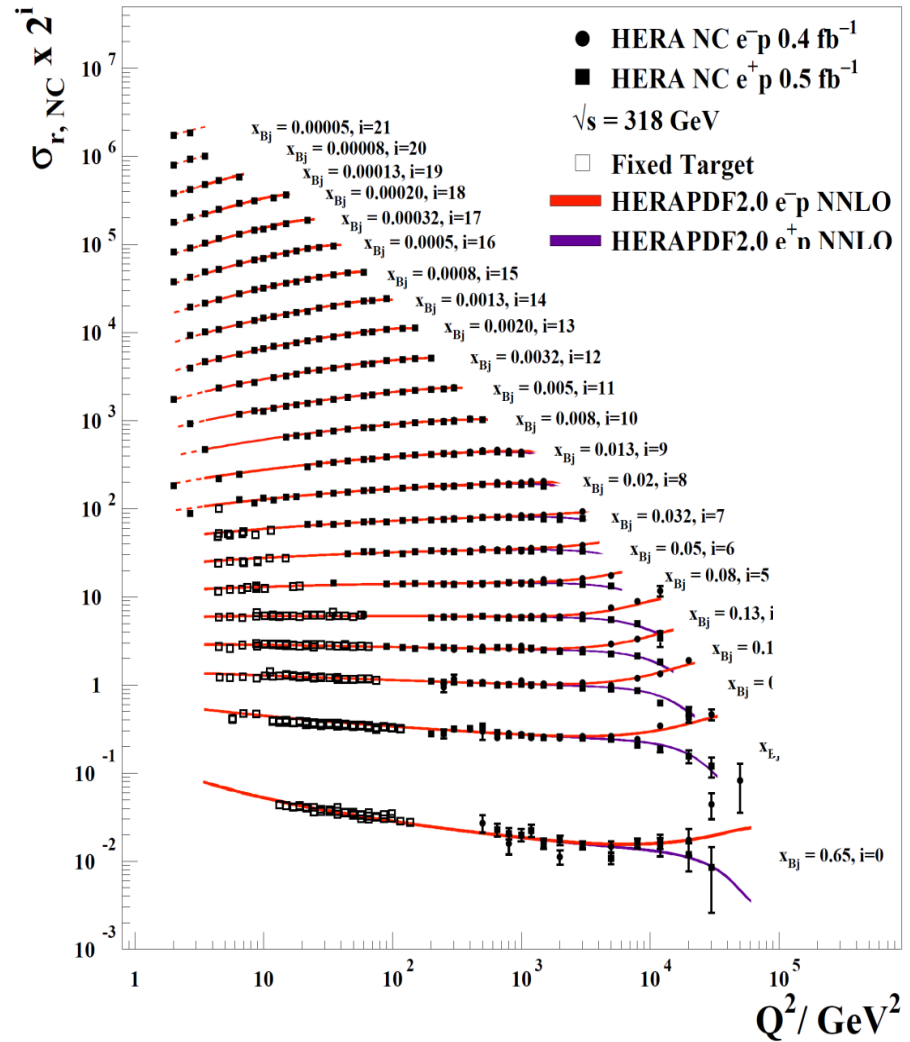
Charged Current:

$$\frac{d^2\sigma_{CC}^-}{dx dQ^2} = \frac{G_F^2}{2\pi} \frac{M_W^2}{M_W^2 + Q^2} (u + c + (1 - y^2)(\bar{d} + \bar{s}))$$

$$\frac{d^2\sigma_{CC}^+}{dx dQ^2} = \frac{G_F^2}{2\pi} \frac{M_W^2}{M_W^2 + Q^2} (\bar{u} + \bar{c} + (1 - y^2)(d + s))$$

flavour decomposition

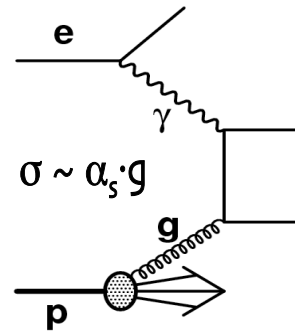
## H1 and ZEUS



arXiv: [1506.06042](https://arxiv.org/abs/1506.06042)

# why jet data?

simultaneous fit of DIS  
inclusive and jet cross  
sections **allows**  
**determination of**  
 **$\alpha_s(M_Z)$**



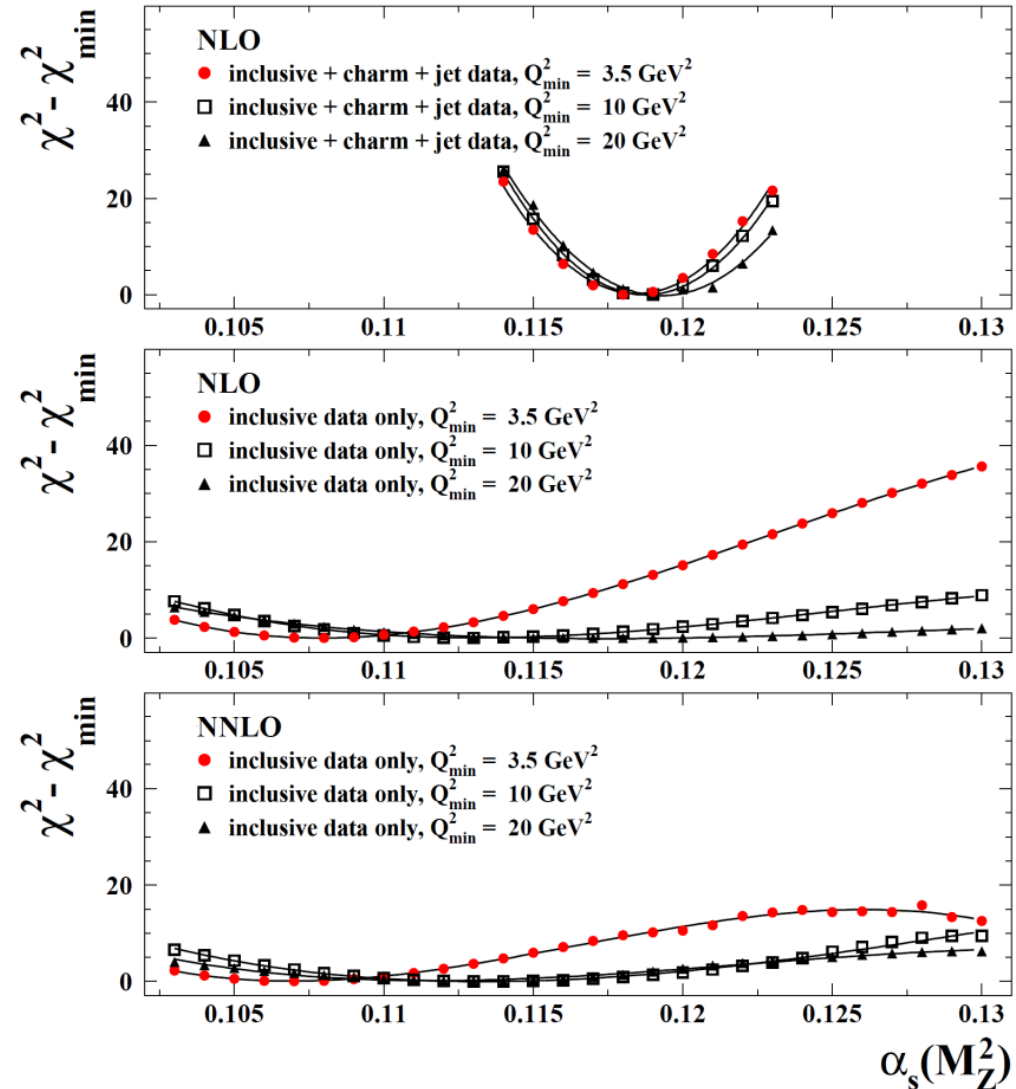
different dependencies on gluon and  $\alpha_s$   
gives improved constraints on both

previous result at NLO  $\rightarrow$   
arXiv: [1506.06042](https://arxiv.org/abs/1506.06042)

**NOW:**

**NNLO QCD calculations** for DIS  
jets available in **NNLOJet**  
(arXiv: [1606.03991](https://arxiv.org/abs/1606.03991), [1703.05977](https://arxiv.org/abs/1703.05977)), and  
implemented in **APPLfast**  
(arXiv: [1906.05303](https://arxiv.org/abs/1906.05303))

## H1 and ZEUS



# jet data used in the current NNLO analysis

strong overlap with those used in previous NLO QCD analysis

Data Set	taken		$Q^2[\text{GeV}^2]$ range		$\mathcal{L}$ pb <sup>-1</sup>	$e^+/e^-$	$\sqrt{s}$ GeV	norma- lised	all points	used points
	from	to	from	to						
H1 HERA I normalised jets	1999	2000	150	15000	65.4	$e^+p$	319	yes	24	24
H1 HERA I jets at low $Q^2$	1999	2000	5	100	43.5	$e^+p$	319	no	28	16
H1 normalised inclusive jets at high $Q^2$	2003	2007	150	15000	351	$e^+p/e^-p$	319	yes	30	24
H1 normalised dijets at high $Q^2$	2003	2007	150	15000	351	$e^+p/e^-p$	319	yes	24	24
H1 normalised inclusive jets at low $Q^2$	2005	2007	5.5	80	290	$e^+p/e^-p$	319	yes	48	32
H1 normalised dijets at low $Q^2$	2005	2007	5.5	80	290	$e^+p/e^-p$	319	yes	48	32
ZEUS inclusive jets	1996	1997	125	10000	38.6	$e^+p$	301	no	30	30
ZEUS dijets	1998–2000 &	2004–2007	125	20000	374	$e^+p/e^-p$	318	no	22	16

**low  $Q^2$  H1 datasets added (published 2016) that were not used in the previous NLO analysis**

## some other data sets removed cf. NLO analysis:

- trijet data, since no NNLO QCD calculations;
- 6 dijet data points at low pt, since predictions unreliable;
- low scale data  $\mu = \sqrt{(Q^2 + pt^2)} < 13.5$  GeV, for which scale variations large

all systematic and statistical correlations implemented

# scale choice for jet data

**factorisation scale choice is  $\mu_F^2=(Q^2+pt^2)$**

cf.  $\mu_F^2=Q^2$  in previous NLO analysis; updated since not a good choice for low  $Q^2$  jet data; change makes almost no difference for high  $Q^2$  jet data

**renormalisation scale choice is  $\mu_R^2=(Q^2+pt^2)$**

cf.  $\mu_R^2=(Q^2+pt^2)/2$  in previous NLO analysis

NB, optimal scale choice – where ‘optimal’ here means lower  $X^2$  – is different for NLO vs NNLO;

NNLO fit with  $\mu_R^2=(Q^2+pt^2)$  gives  $\Delta X^2= -15$  cf.  $\mu_R^2=(Q^2+pt^2)/2$  and vice versa for NLO fit

**consequences of scale changes also explored**

† pt denotes  $pt^{\text{jet}}$  in the case of inclusive jet cross sections and  $\langle pt \rangle$  for dijets

# HERA PDF approach

- **HERAPDF uses only HERA data**
- combination of HERA data yields very precise and consistent dataset for 4 different processes: **e+p** and **e-p neutral** and **charged current** reactions; also, for e+p, neutral current at 4 beam energies
- single consistent dataset; conventional  $\chi^2$  tolerance,  $\Delta\chi^2 = 1$
- use of proton target means no need for heavy target/deuterium corrections
- d-valence extracted from CC e+p without assuming d in proton = u in neutron
- all data at  $W > 15$  GeV, so high-x higher twist effects negligible
- **HERAPDF** evaluates model and parameterisation uncertainties in addition to experimental uncertainties
- **HERAPDF2.0** based on **FINAL combination of HERA I and HERA II data**, which supercedes the HERA I combination and all previous HERAPDFs
- **HERAPDF2.0Jets** add HERA jet data to this

# HERAPDF parameterisation

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g},$$

QCD sum rules constrain  
 $A_g, A_{uv}, A_{dv}$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2),$$

$x\bar{s} = f_s x\bar{D}$  : sets size of  
strange PDF

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x),$$

constraints  $B_{\bar{U}} = B_{\bar{D}}$  and  
 $A_{\bar{U}} = A_{\bar{D}}(1 - f_s)$  ensure  
 $x\bar{u} \rightarrow x\bar{d}$  as  $x \rightarrow 0$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$$

- **14 free parameters in central fit**, established by saturation of  $\mathbf{X}^2$
- extra D, E parameters added to all PDF flavours for parameterisation uncertainties,  $A_{g'}=0$  also checked
- QCDNUM used for QCD DGLAP evolution, within xFitter framework, and cross checked with independent code
- Thorne-Roberts Optimised Variable Flavour Number Scheme (RT-VFN)
- jet predictions from NNLOJet (arXiv:[1606.03991](https://arxiv.org/abs/1606.03991), [1703.05977](https://arxiv.org/abs/1703.05977)) interfaced to APPLfast (arXiv:[1906.05303](https://arxiv.org/abs/1906.05303))
- **$\alpha_s(M_Z)=0.118, 0.115$ ; plus free  $\alpha_s$  fit**



# HERAPDF sources of uncertainty

## experimental:

Hessian uncertainties: 14 eigenvector pairs evaluated with  $\Delta\chi^2=1$ ; cross checked uncertainties using rms of MC replicas

## model:

variation of input assumptions; and c,b masses

$$f_s = 0.4 \pm 0.1$$

$$M_c = 1.43 \pm 0.06 \text{ GeV}$$

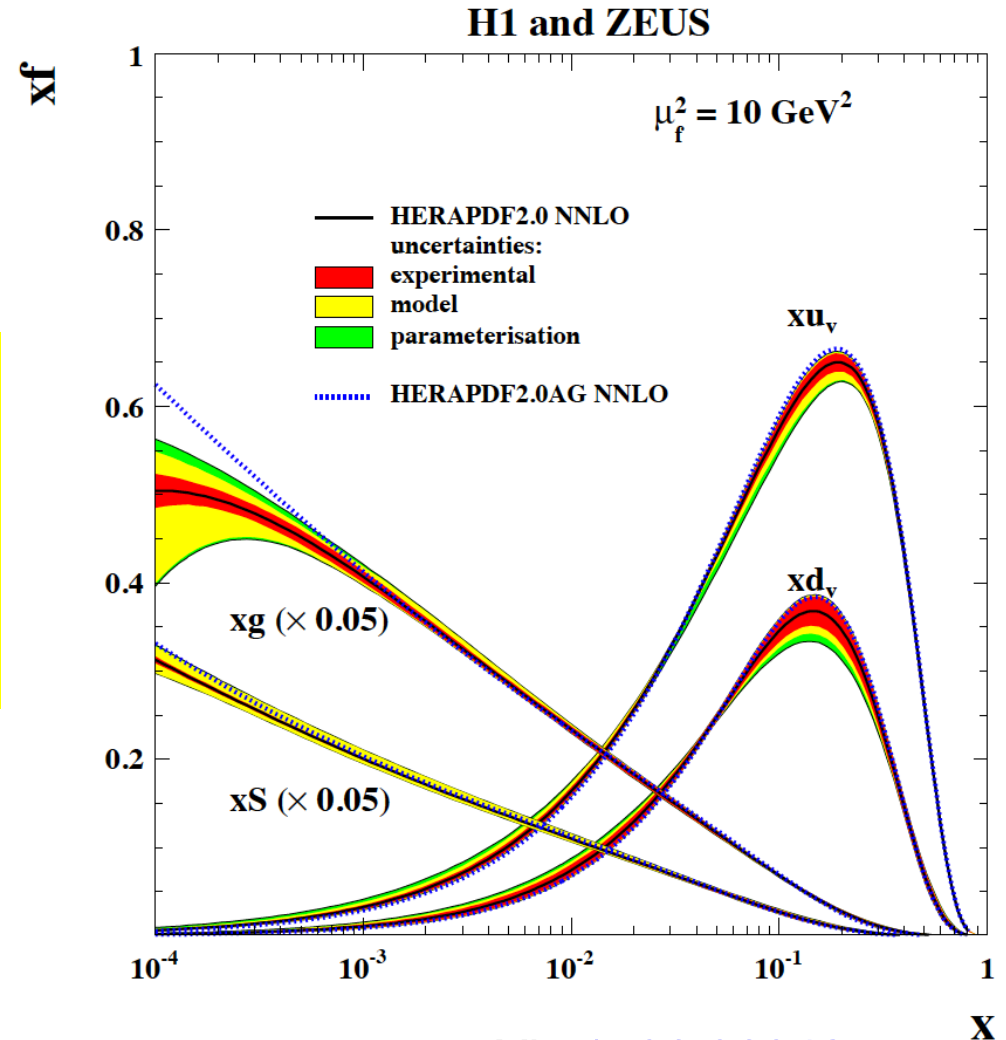
$$M_b = 4.5 \pm 0.25 \text{ GeV}$$

$$Q^2_{\text{min}} = 3.5_{-1}^{+1.5} \text{ GeV}^2$$

## parameterisation:

variation of  $Q^2_0 = 1.9 \pm 0.3 \text{ GeV}^2$ , plus addition of 15th parameter(s)

(variations as for HERAPDF2.0 analysis)



HERAPDF2.0, arXiv:[1506.06042](https://arxiv.org/abs/1506.06042)

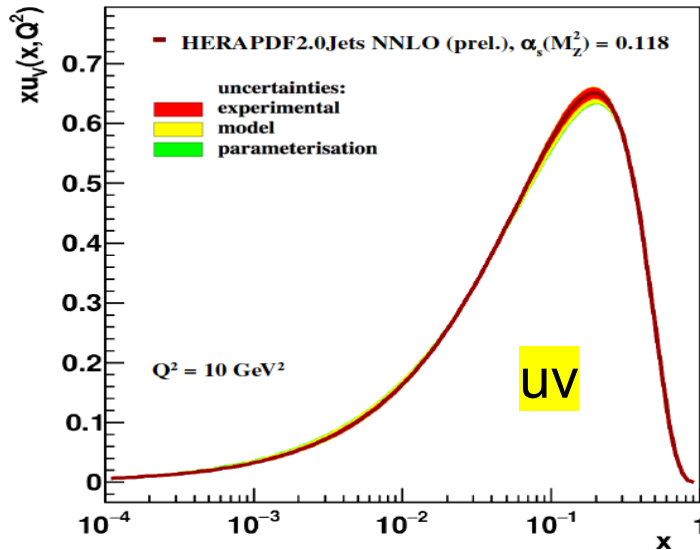
NB, for **jet cross sections**, hadronisation uncertainties also included

# HERAPDF2.0Jets NNLO

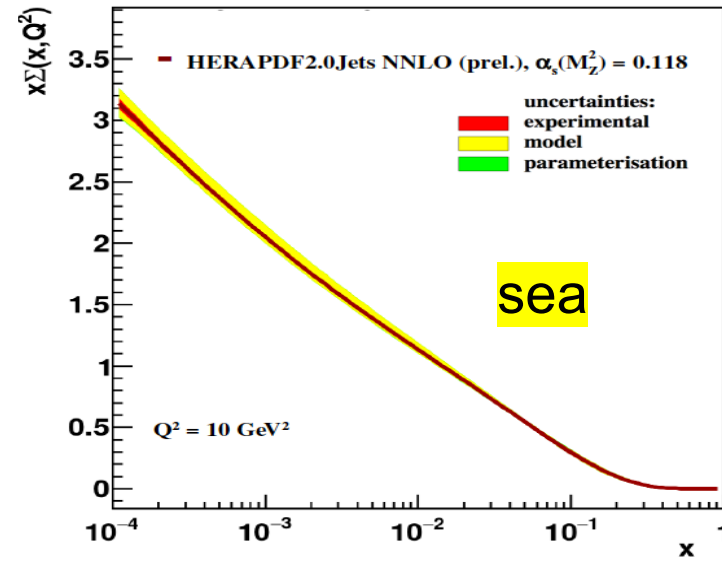
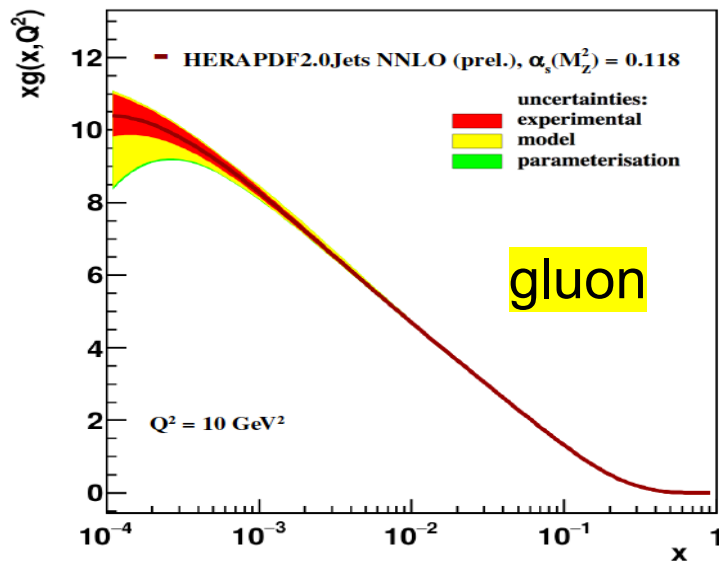
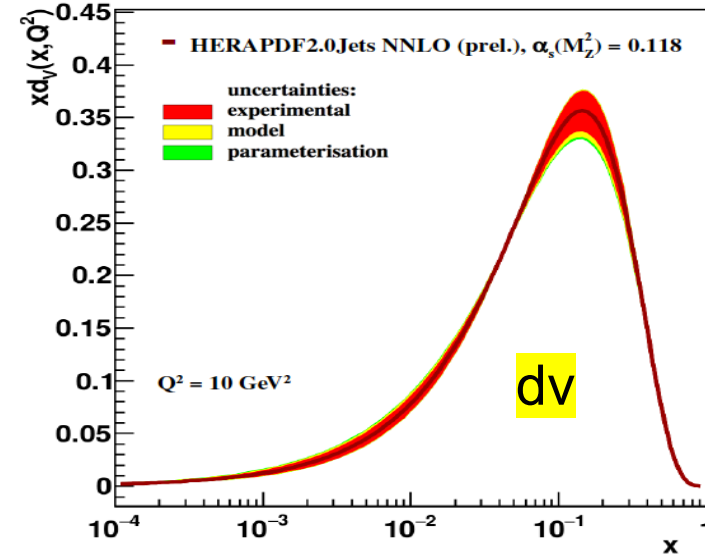
$\alpha_s(M_Z)=0.118$

fixed

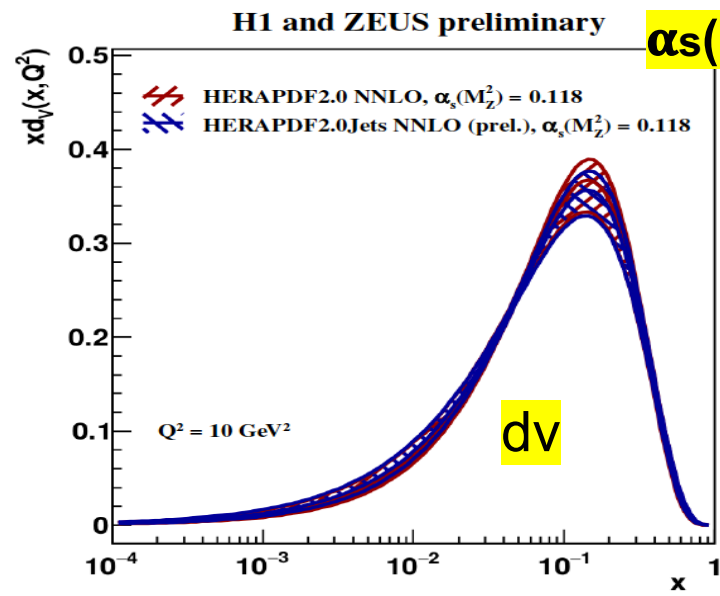
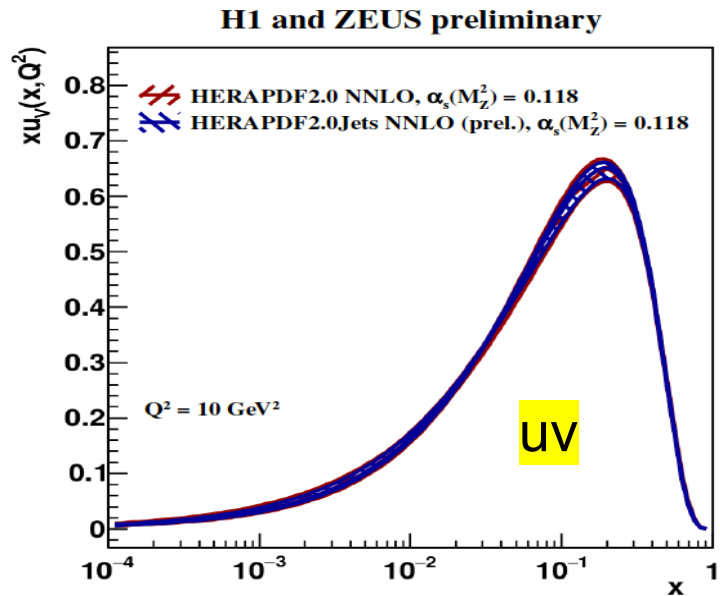
H1 and ZEUS preliminary



H1 and ZEUS preliminary

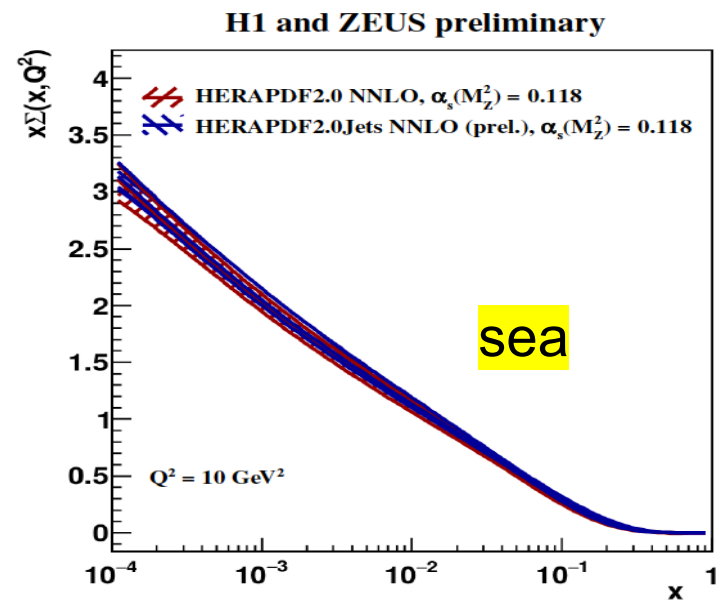
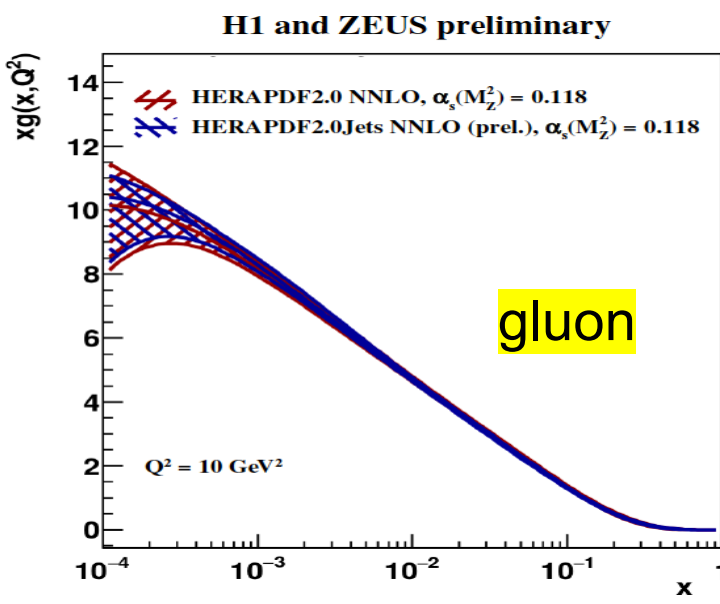


# HERAPDF2.0 vs HERAPDF2.0Jets NNLO



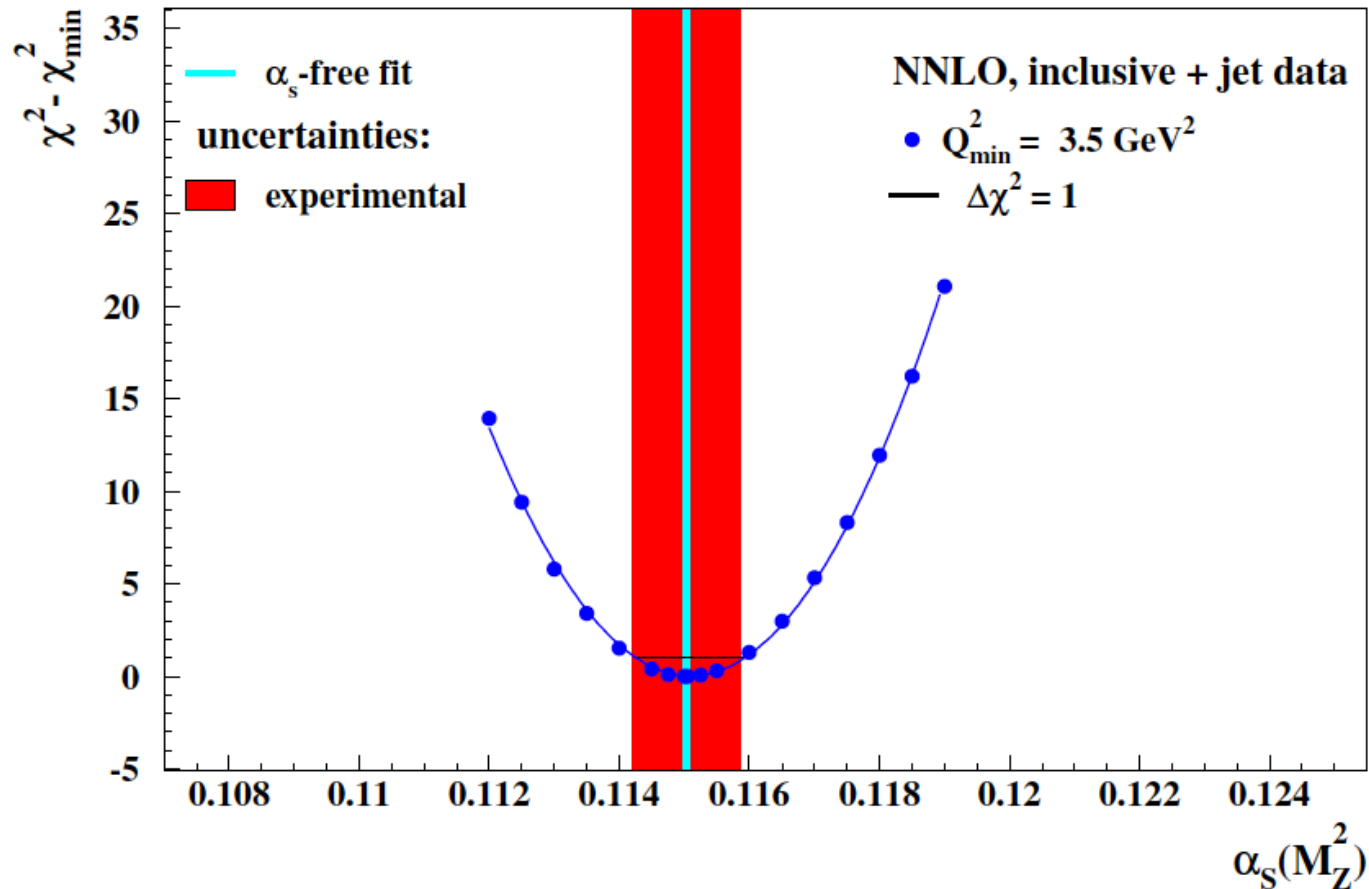
$\alpha_s(M_Z) = 0.118$

fixed



# HERAPDF2.0Jets NNLO $\alpha_s$ fits

H1 and ZEUS preliminary



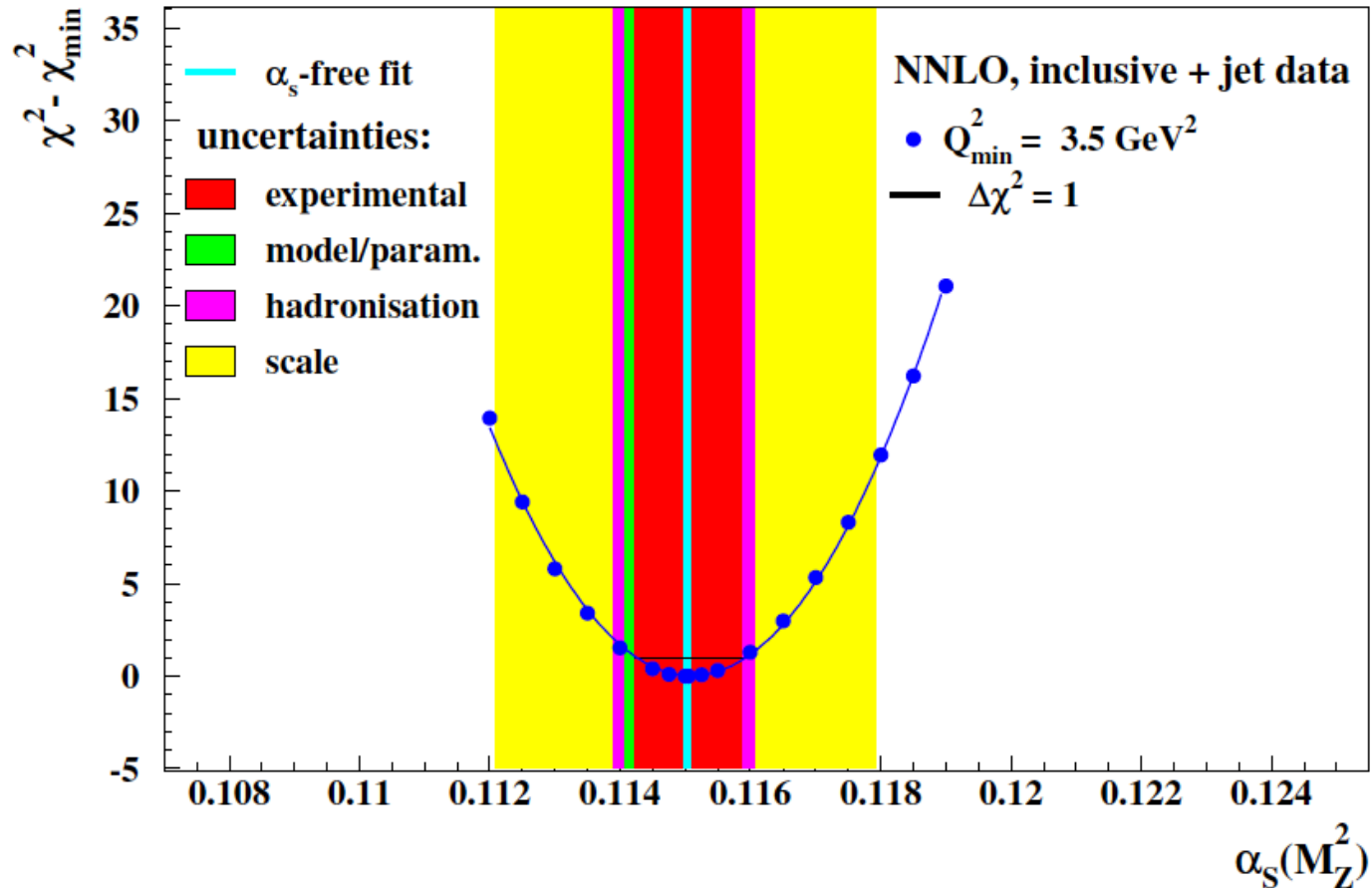
standard HERAPDF value is  $\alpha_s(M_Z)=0.118$  (shown on previous slides)

fits also performed with **free  $\alpha_s(M_Z)$** , compared here to  **$\chi^2$  scan over fixed  $\alpha_s(M_Z)$**

**perfect agreement in minimum and uncertainty**

# HERAPDF2.0 Jets NNLO $\alpha_s$ fits

H1 and ZEUS preliminary

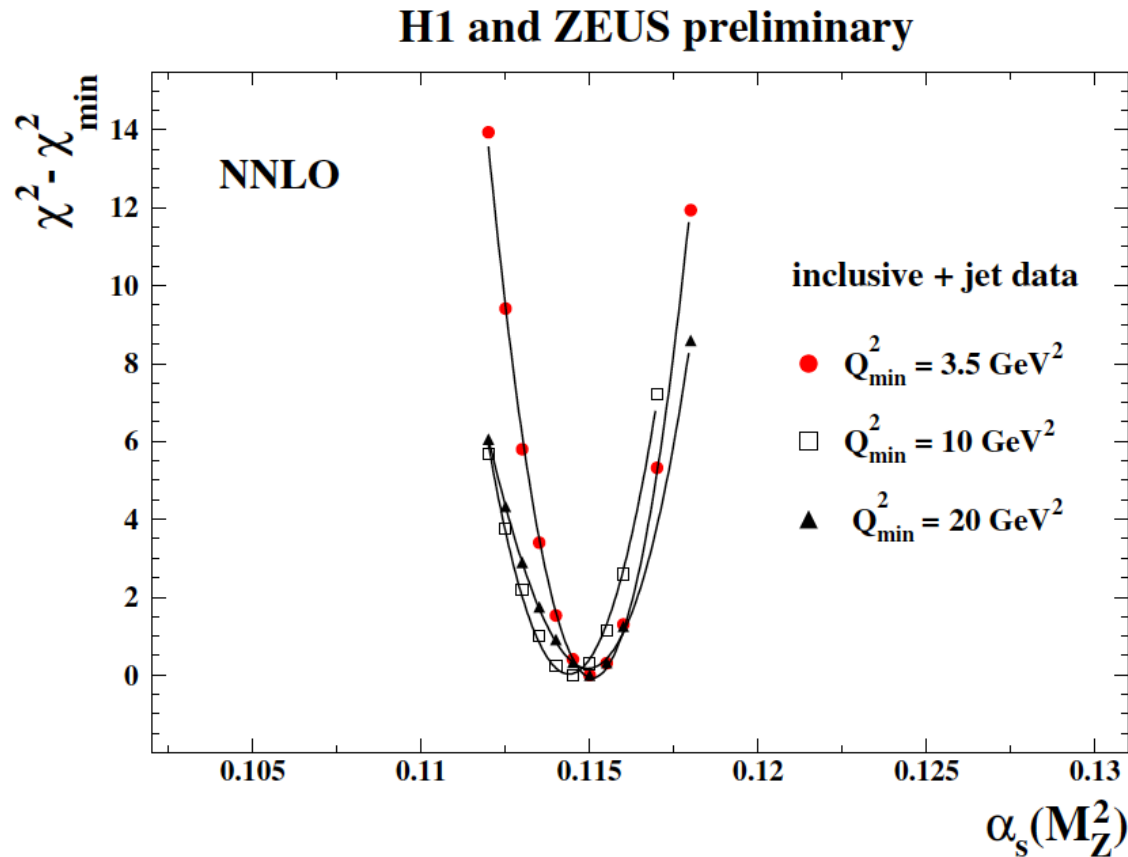


and with full uncertainties:

$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008 (\text{exp})_{-0.0005}^{+0.0002} (\text{model/par.}) \pm 0.0006 (\text{had}) \pm 0.0027 (\text{scale})$$

[NB, scale uncertainty dominates; 7-point variation considered, with  $\mu_R$ ,  $\mu_F$  varied by factor of 2]

# sensitivity to minimum $Q^2$ cut



central values from the 3 scans:

$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008 \text{ (exp)} \quad Q^2 > 3.5 \text{ GeV}^2$$

$$\alpha_s(M_Z^2) = 0.1144 \pm 0.0010 \text{ (exp)} \quad Q^2 > 10 \text{ GeV}^2$$

$$\alpha_s(M_Z^2) = 0.1148 \pm 0.0010 \text{ (exp)} \quad Q^2 > 20 \text{ GeV}^2$$

EG, arXiv:[1506.06042](https://arxiv.org/abs/1506.06042), [1710.05935](https://arxiv.org/abs/1710.05935)

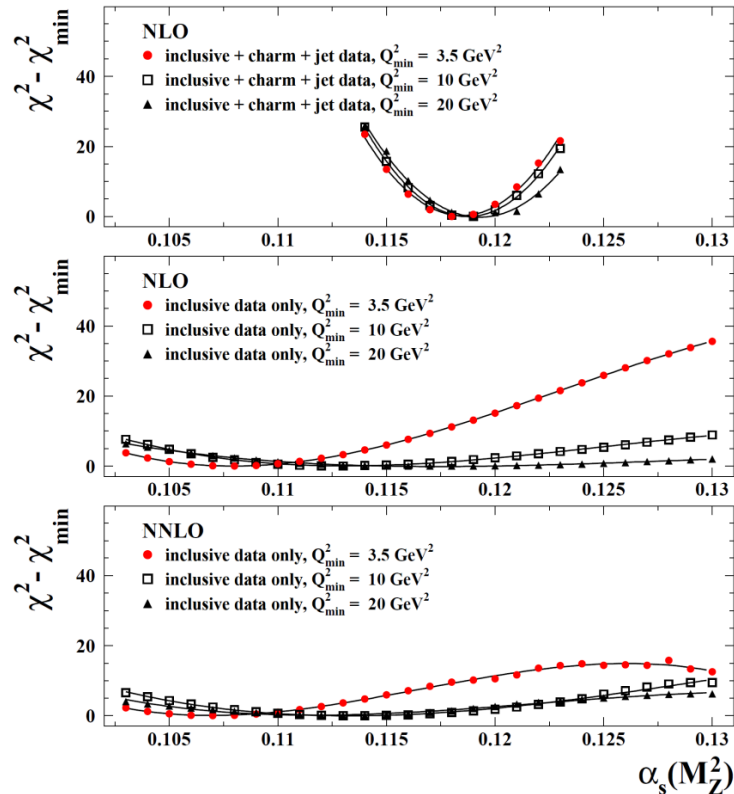
HERA data at low  $x$ ,  $Q^2$  may be subject to need for  $\ln(1/x)$  resummation or higher twist effects;  
 $\chi^2$  scans also performed with harder minimum  $Q^2$  cuts

**no significant change to extracted value of  $\alpha_s(M_Z)$**

# comparison to previous NLO result

arXiv: [1506.06042](https://arxiv.org/abs/1506.06042)

H1 and ZEUS



**NNLO scans using inclusive and jet data** are compared to previously published scans at NLO, plus corresponding scans using only inclusive data

similar level of precision at NNLO and NLO

smaller value of  $\alpha_s(M_Z)$  preferred at NNLO

NB, conclusion holds independent of updated scale choices; with old scales, NNLO result would be even lower at 0.1135

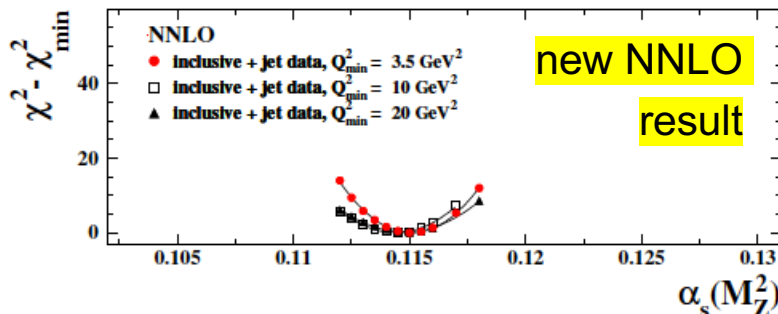
**NNLO:**

$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008 (\text{exp})_{-0.0005}^{+0.0002} (\text{model/par.}) : \pm 0.0006 (\text{had}) \pm 0.0027 (\text{scale})$$

cf. **NLO:** arXiv: [1506.06042](https://arxiv.org/abs/1506.06042)

$$\alpha_s(M_Z^2) = 0.1183 \pm 0.0009 (\text{exp}) \pm 0.0005 (\text{model/par.}) \pm 0.0012 (\text{had})_{-0.0030}^{+0.0037} (\text{scale})$$

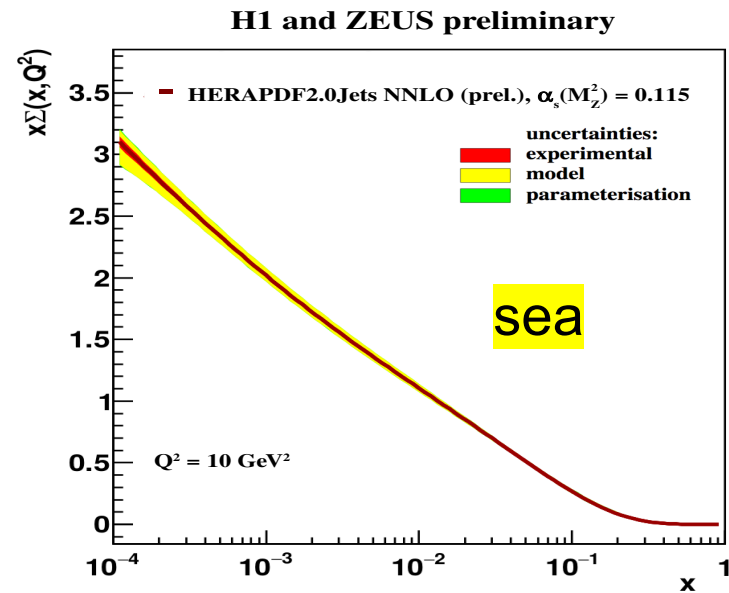
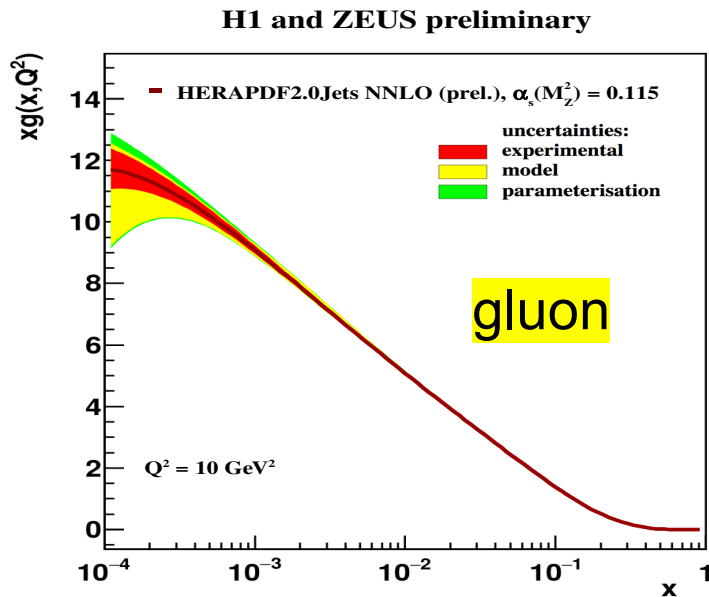
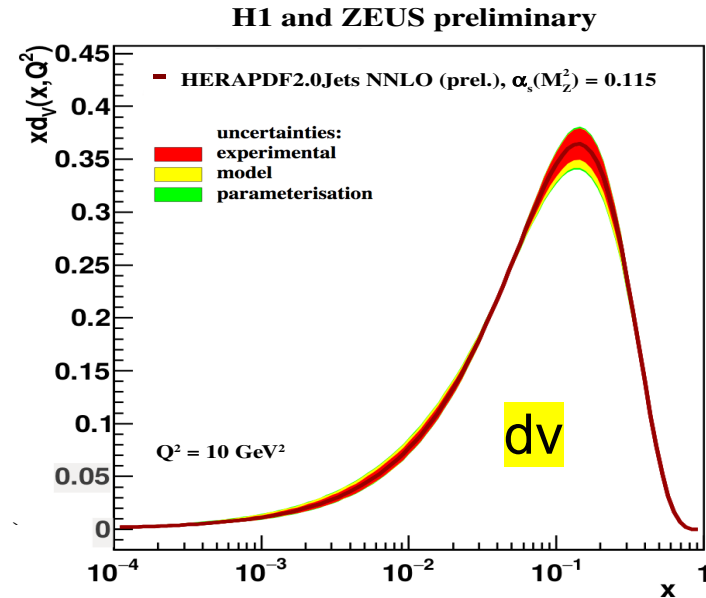
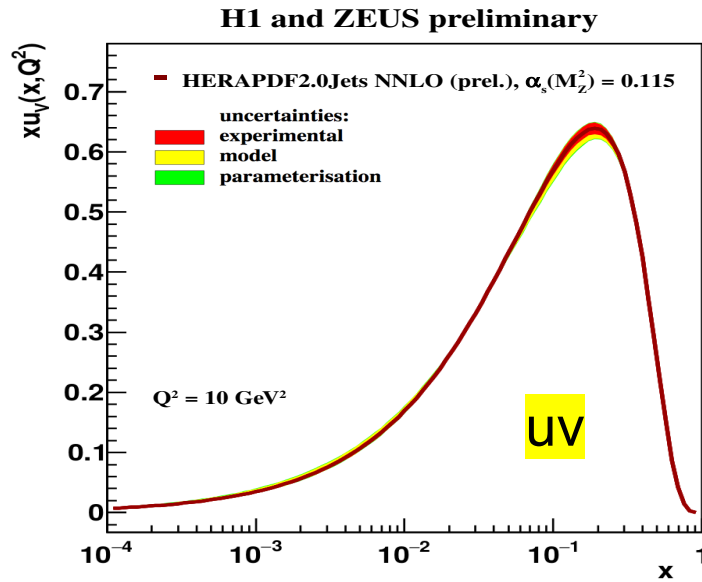
H1 and ZEUS preliminary



# HERAPDF2.0Jets NNLO

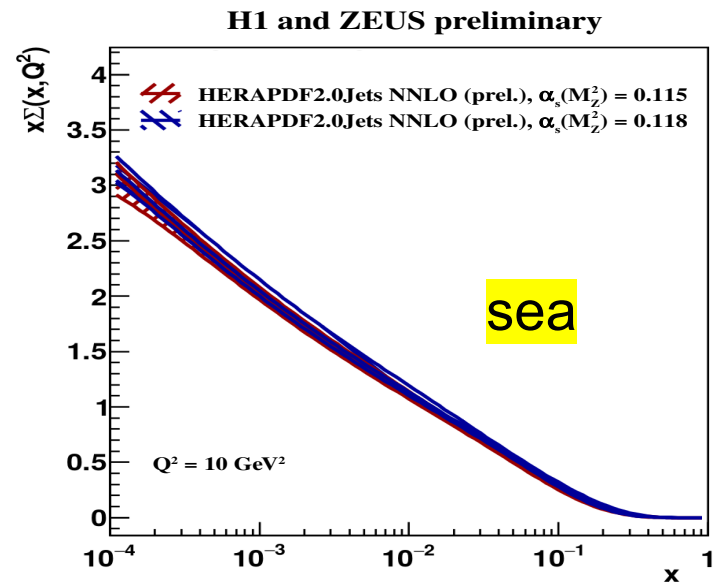
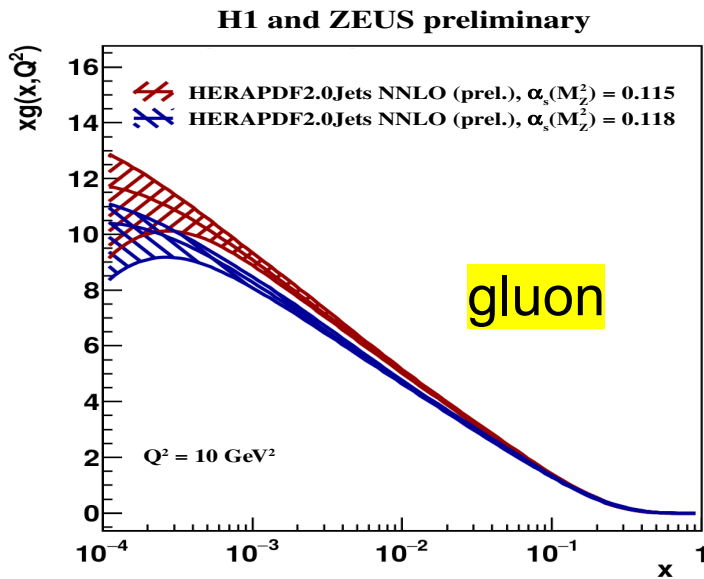
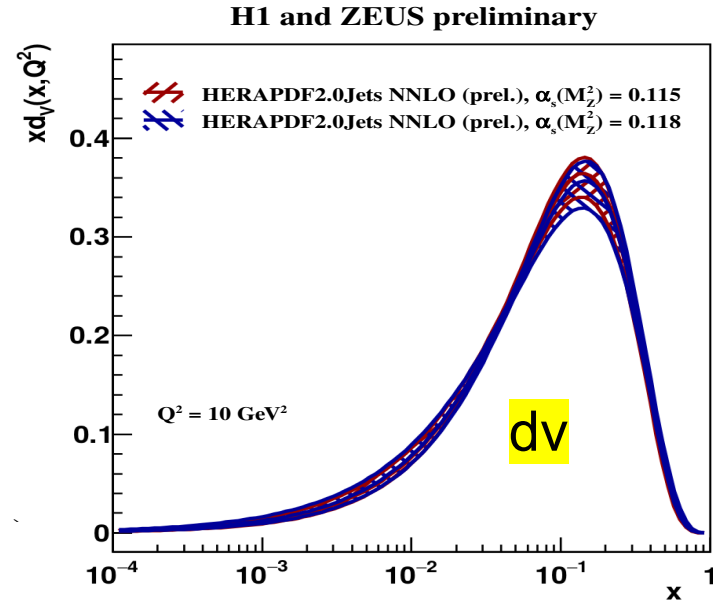
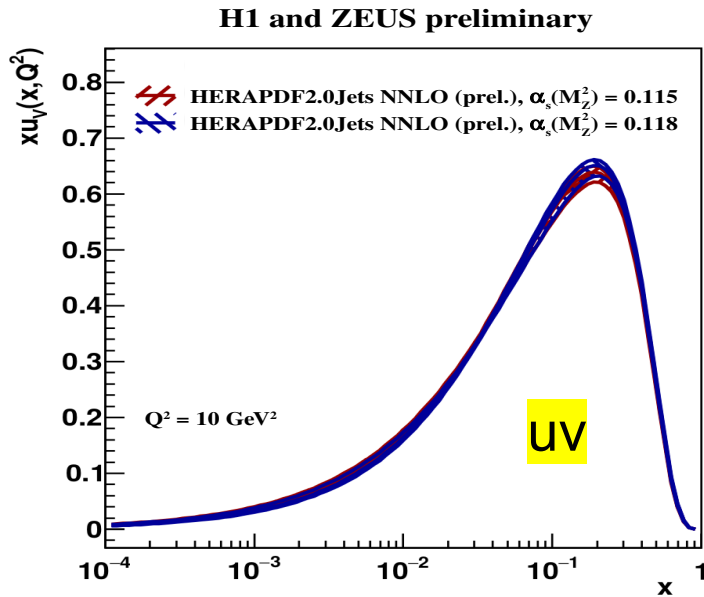
$\alpha_s(M_Z)=0.115$

fixed



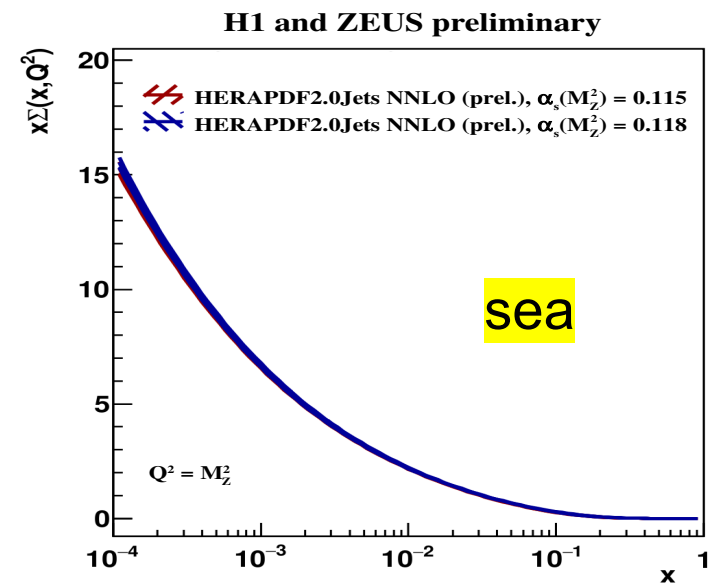
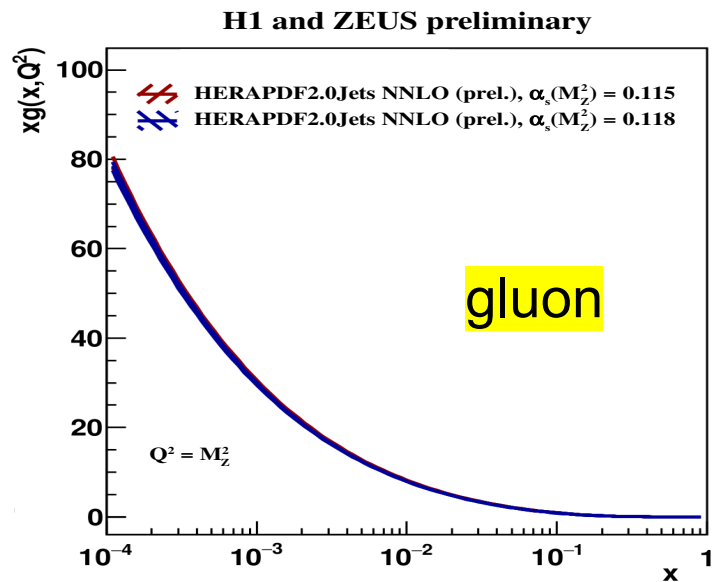
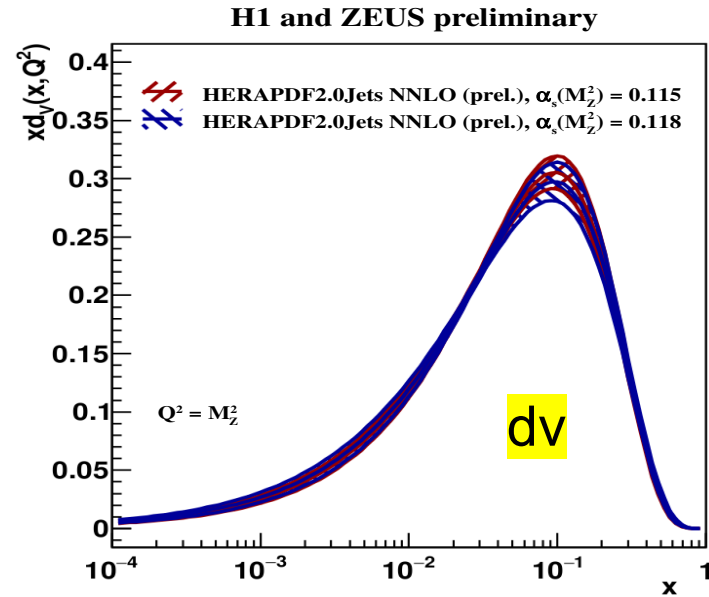
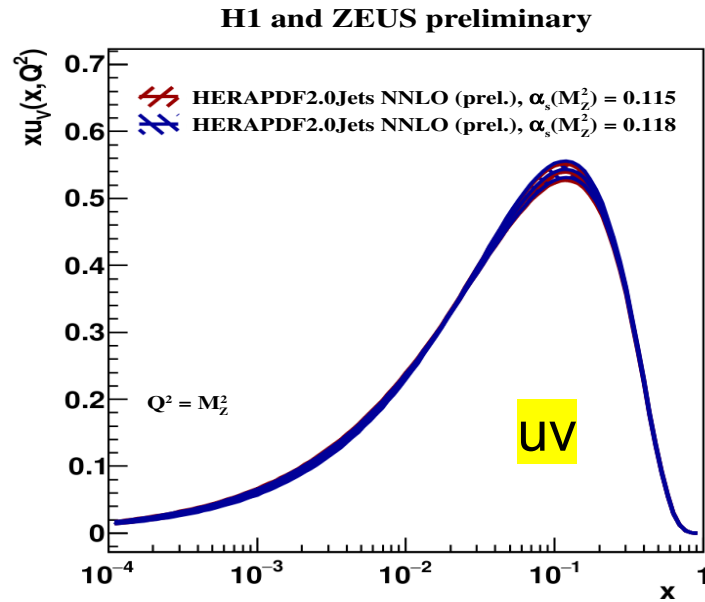


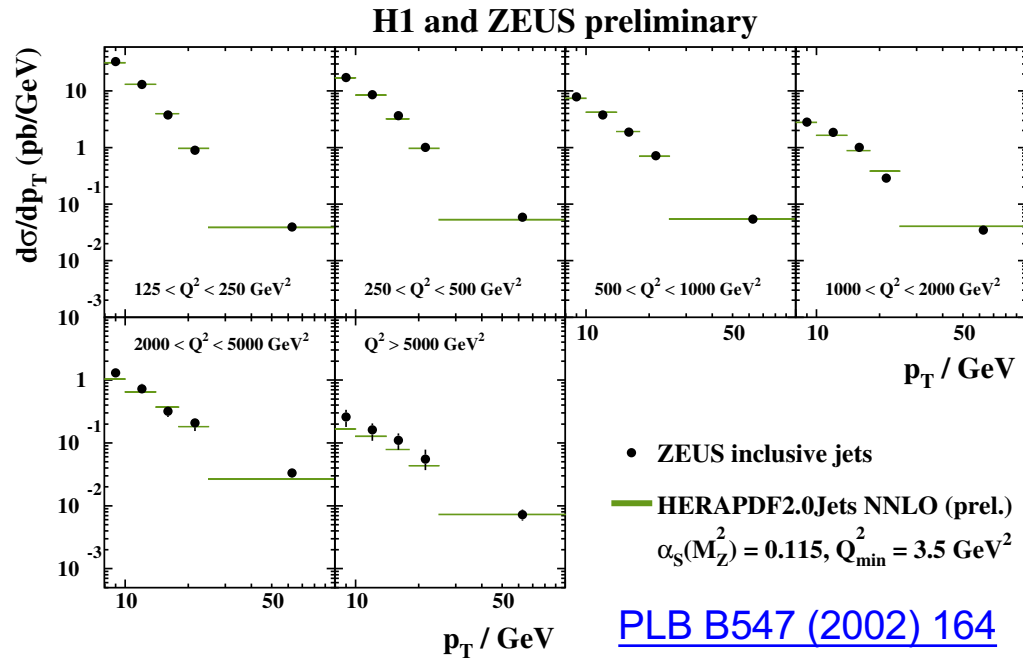
# comparison of $\alpha_s(M_Z)=0.115$ and $0.118$



# comparison of $\alpha_s(M_Z)=0.115$ and $0.118$

at higher  
scale  
 $Q^2=M_Z^2$

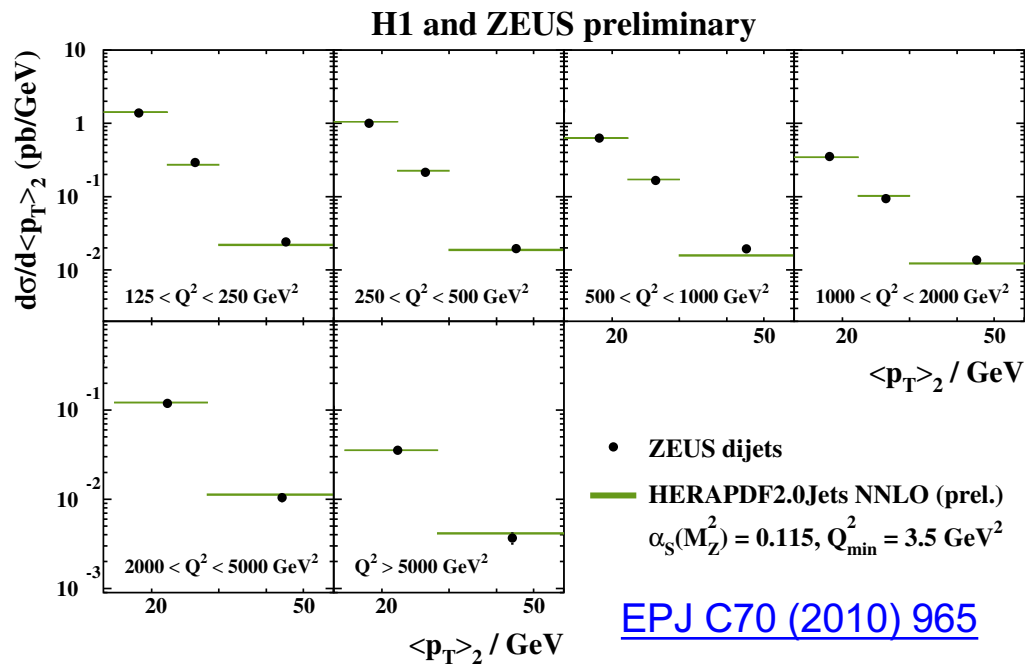




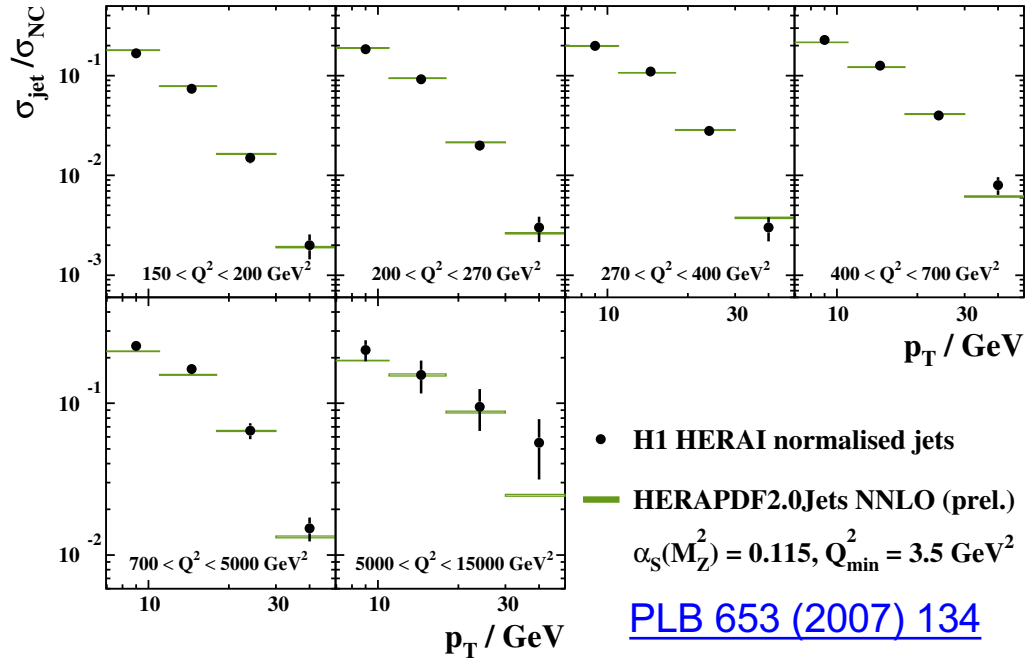
cf. HERA jet data

HERAPDF2.0JetsNLO

$\alpha_s(M_Z) = 0.115$



H1 and ZEUS preliminary

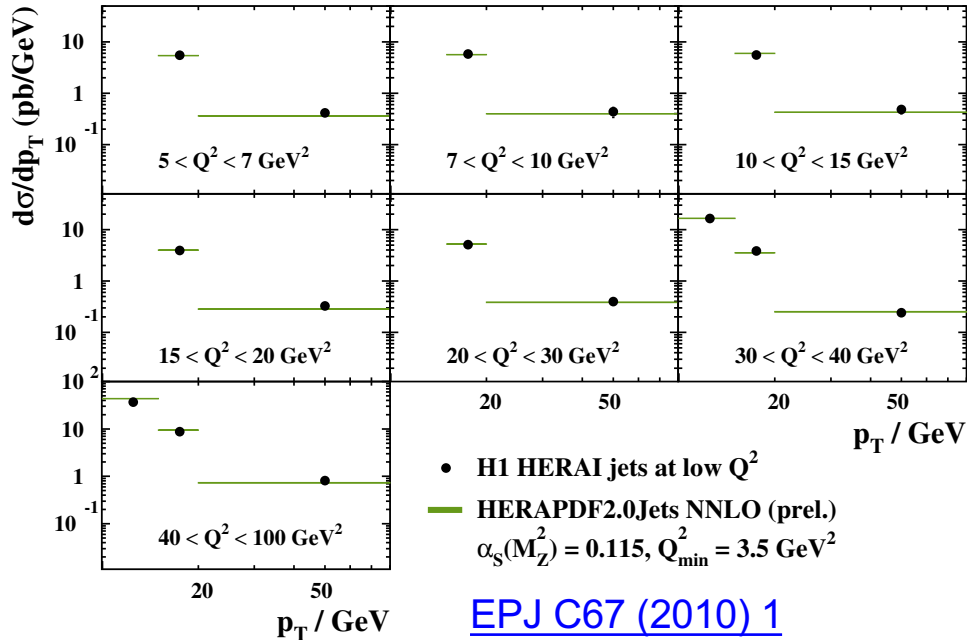


cf. HERA jet data

HERAPDF2.0JetsNLO

$\alpha_s(M_Z) = 0.115$

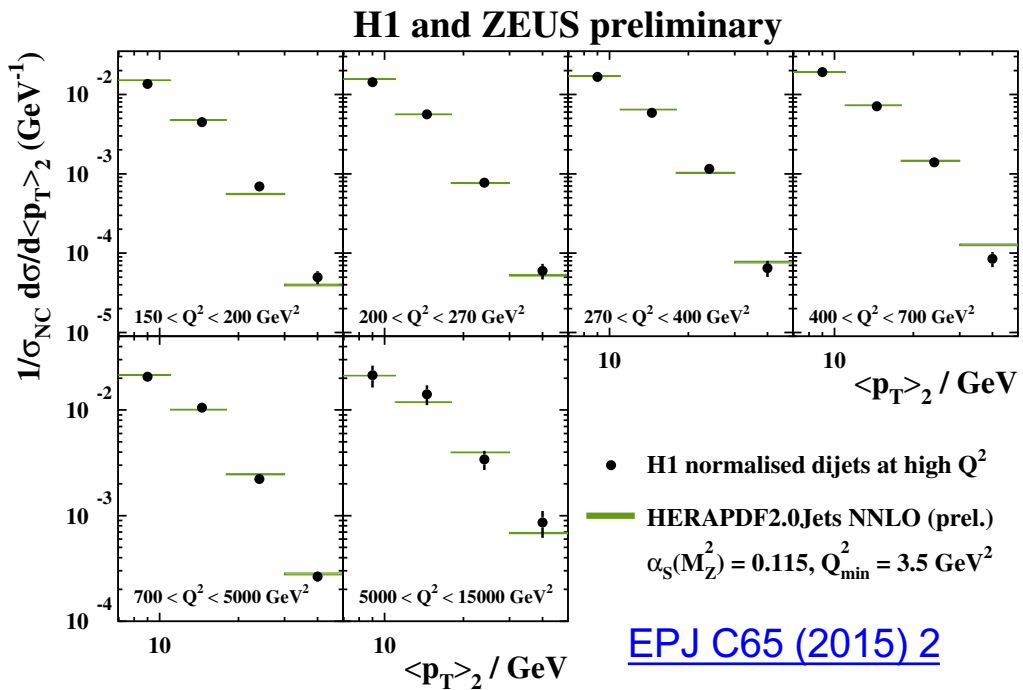
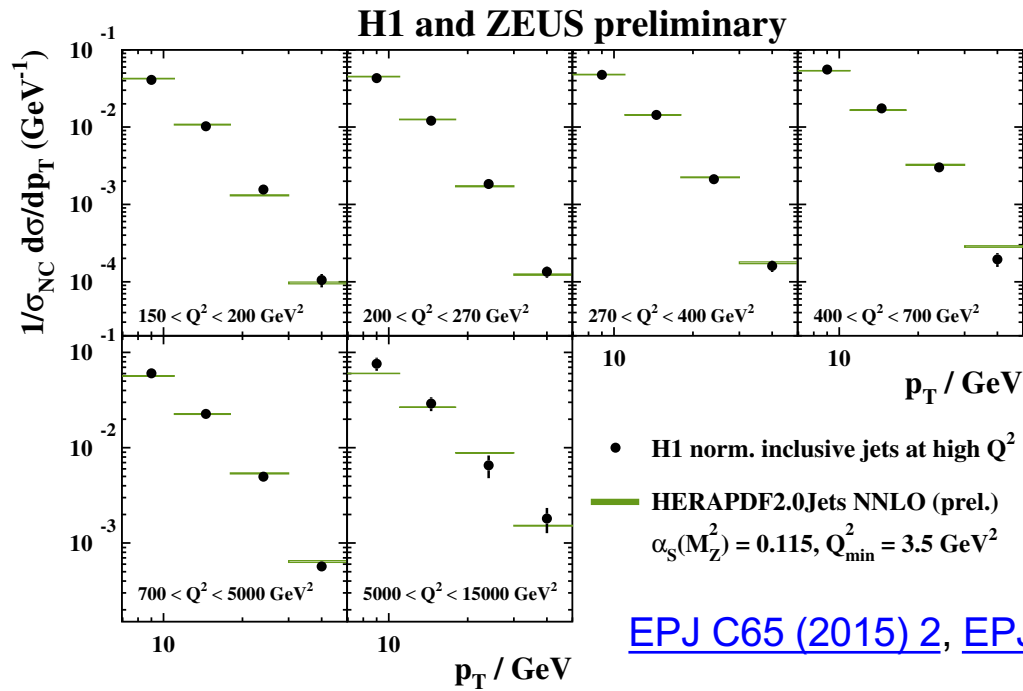
H1 and ZEUS preliminary



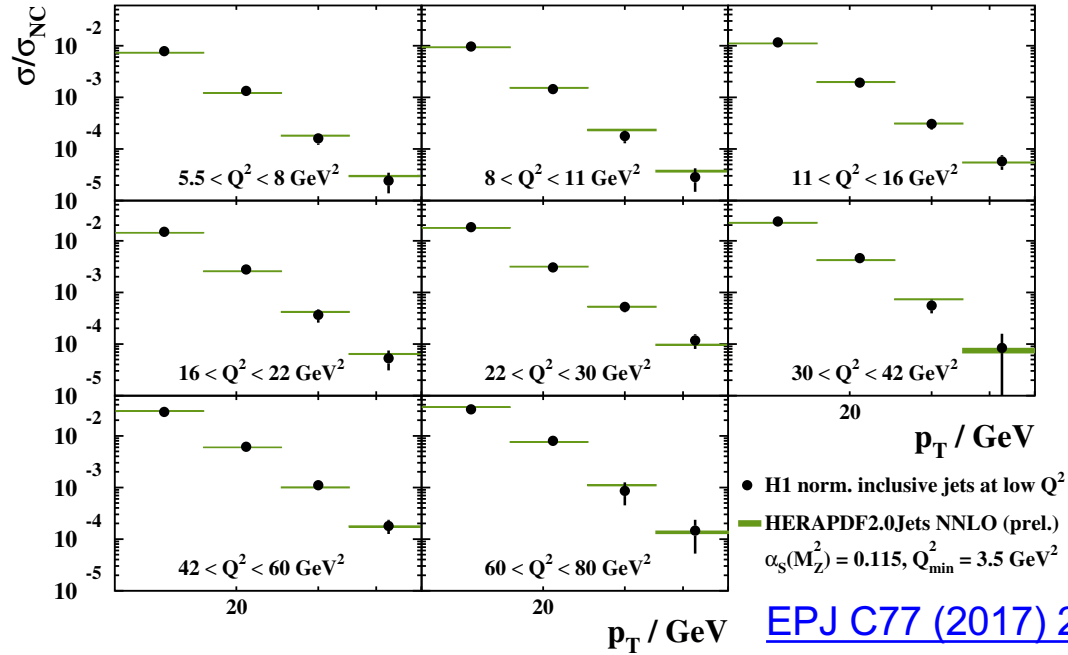
cf. HERA jet data

HERAPDF2.0JetsNLO

$\alpha_s(M_Z)=0.115$



### H1 and ZEUS preliminary

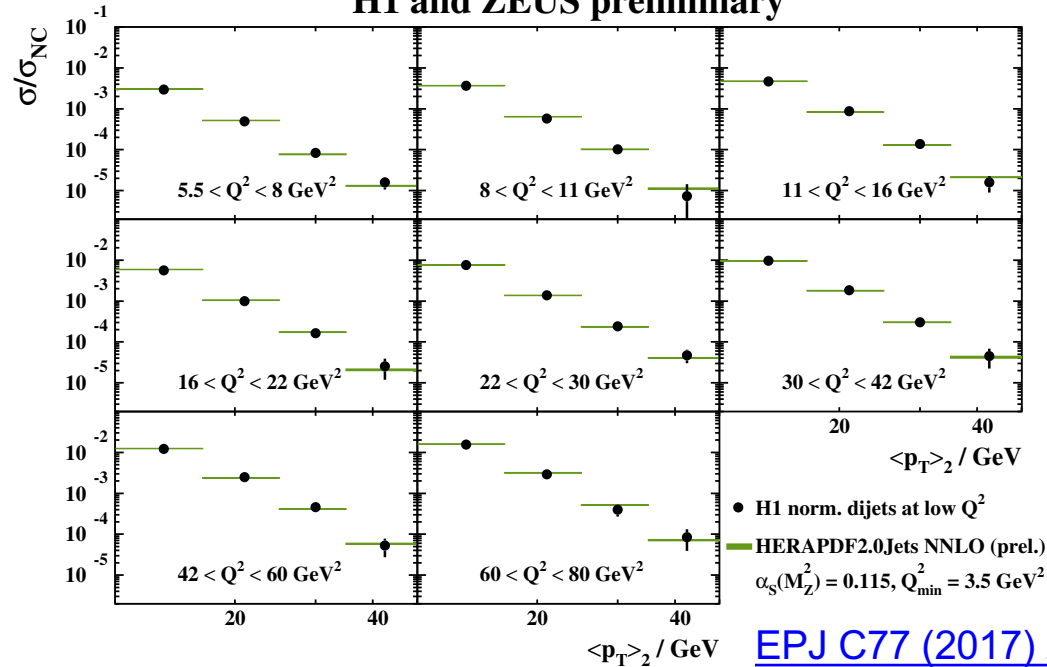


cf. HERA jet data

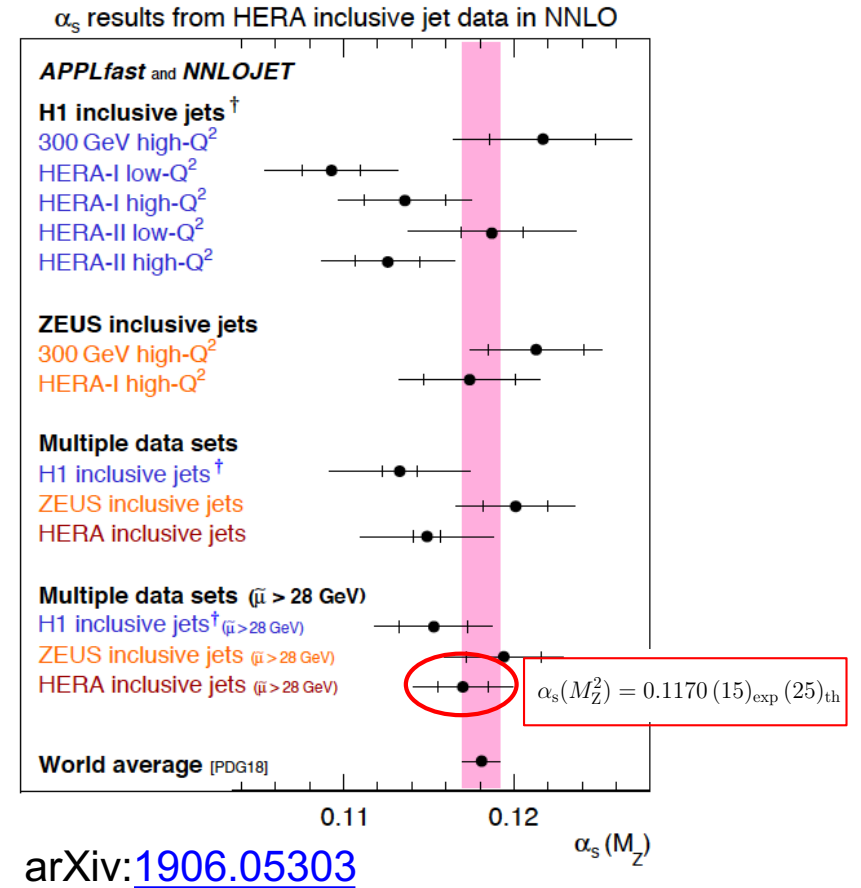
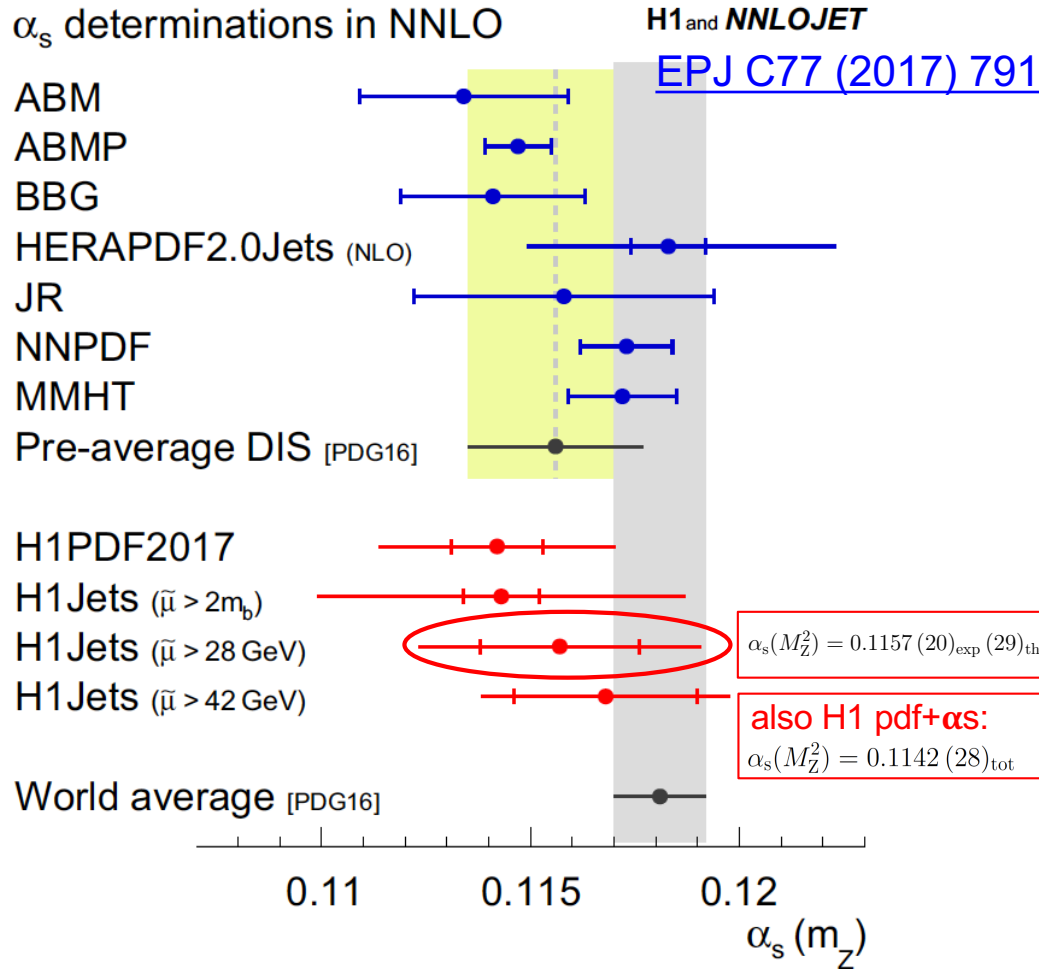
HERAPDF2.0JetsNLO

$\alpha_s(M_Z) = 0.115$

### H1 and ZEUS preliminary



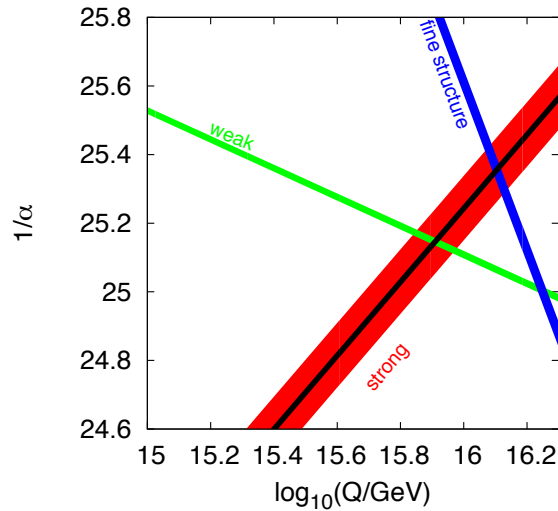
# cf. other NNLO determinations



NNLOJet+APPLfast colls., **new result**,  
**HERA inclusive jets**

**NNLO (this analysis):**  $\alpha_s(M_Z^2) = 0.1150 (8)_{\text{exp}} (28)_{\text{th}}$

# impact at LHC

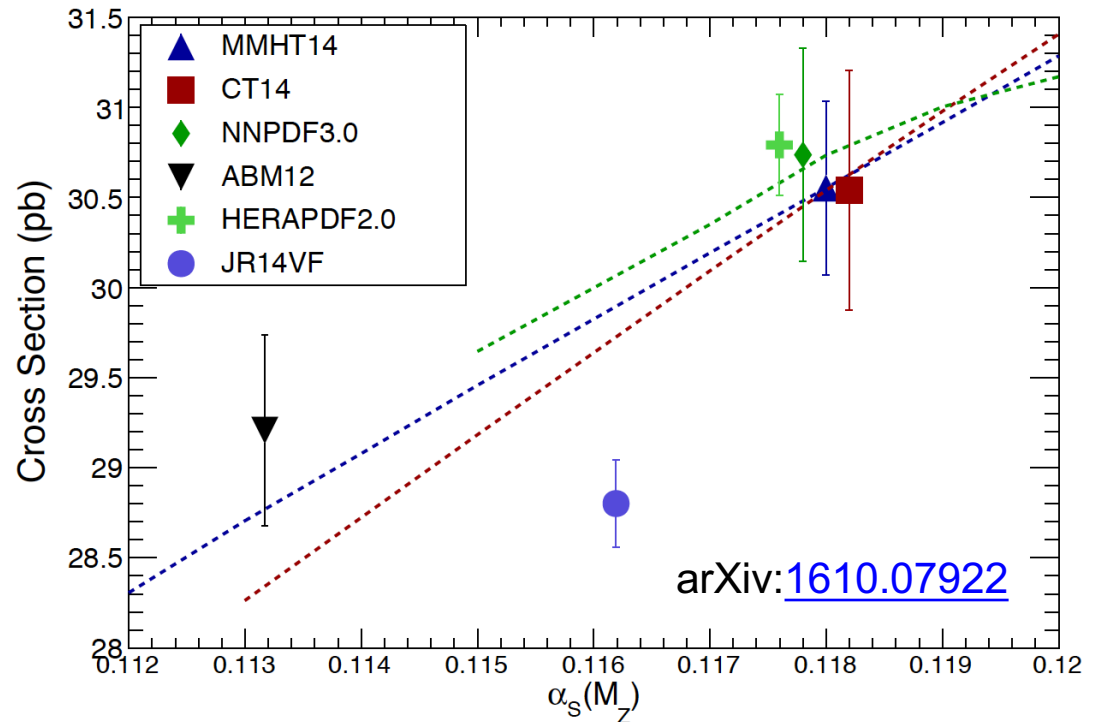


- $\alpha_s$  is least known coupling constant;  
needed to constrain GUT scenarios;  
cross section predictions, including Higgs; ...

**PDG18:**  $\alpha_s = 0.1181 \pm 0.0011$

( $\alpha_s = 0.1174 \pm 0.0016$ ; w/o lattice QCD)

Gluon-Fusion Higgs production, LHC 13 TeV



- what is true central value and uncertainty?  
new precise determinations have important role to play



# summary

**HERAPDF2.0 family of PDFs completed by performing an NNLO fit including HERA DIS jet data**

possible only due to recent **theoretical** and **grid technology** developments (NNLOJet, APPLfast)

**TWO new PDF sets:**

HERAPDF2.0JetsNNLO  $\alpha_s(M_Z)=0.118$  (the PDG value)

HERAPDF2.0JetsNNLO  $\alpha_s(M_Z)=0.115$  (value favoured by our new fits)

**the jet data allows us to constrain  $\alpha_s(M_Z)$ ; NNLO value:**

$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008 (\text{exp})_{-0.0005}^{+0.0002} (\text{model/par.}) \pm 0.0006 (\text{had}) \pm 0.0027 (\text{scale})$$

**cf. NLO value:**

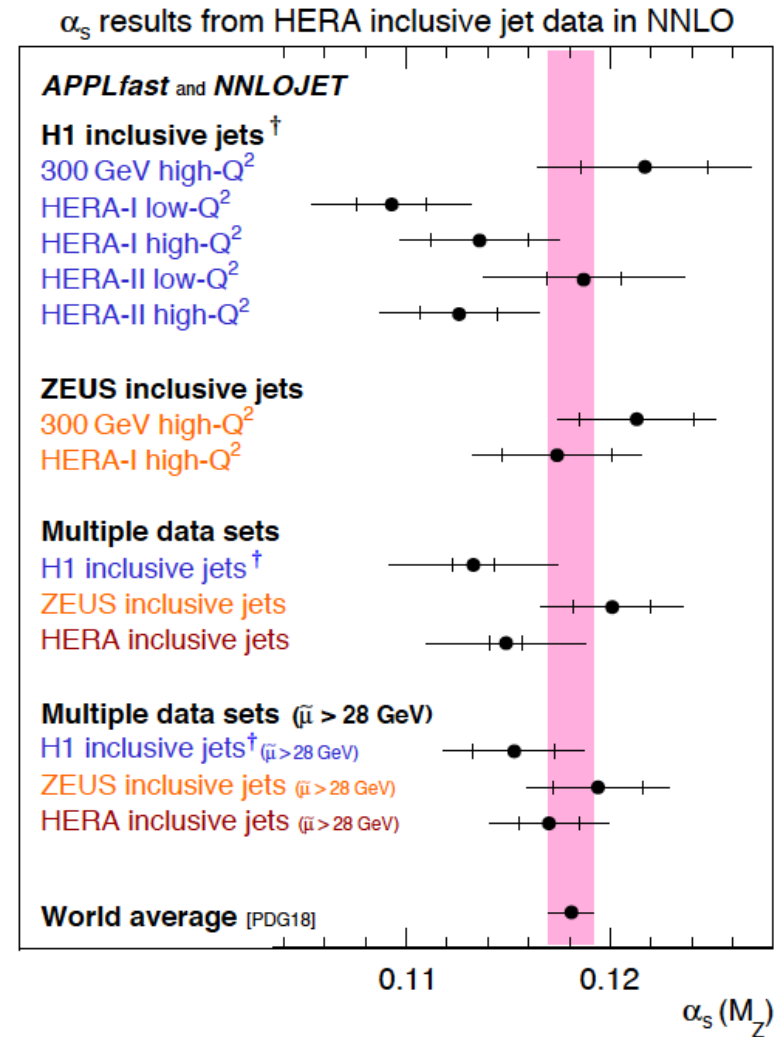
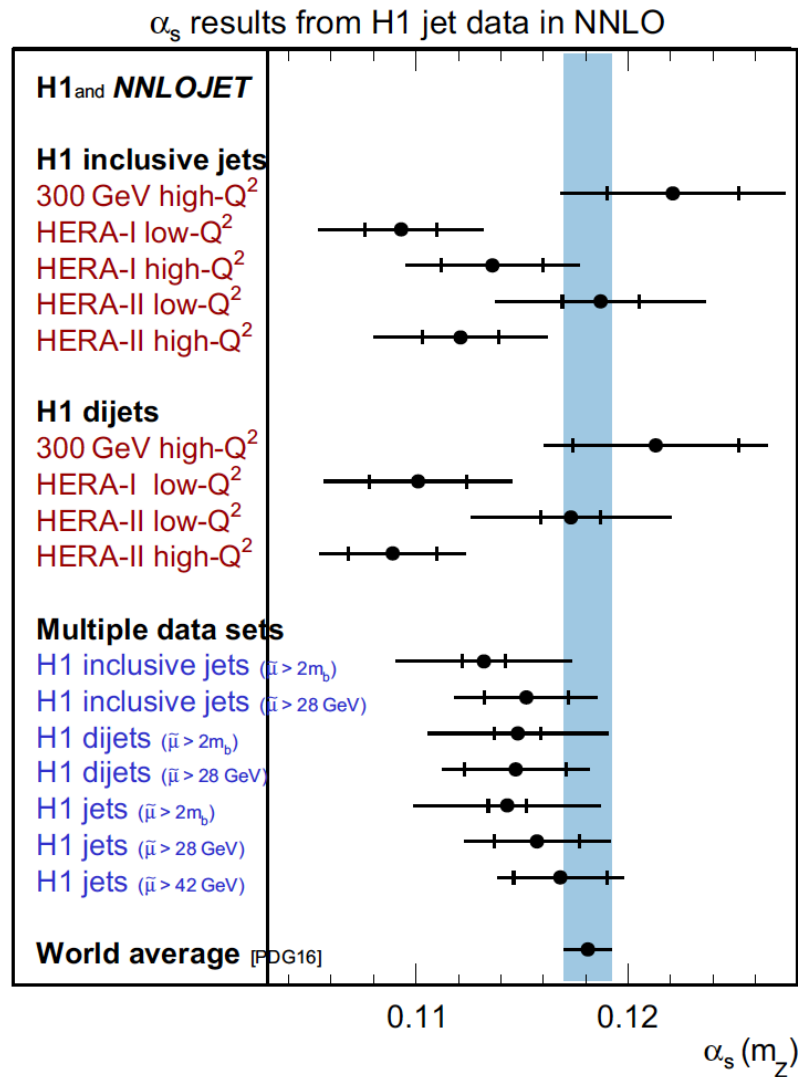
$$\alpha_s(M_Z^2) = 0.1183 \pm 0.0009 (\text{exp}) \pm 0.0005 (\text{model/par.}) \pm 0.0012 (\text{had})_{-0.0030}^{+0.0037} (\text{scale})$$

systematic shift downwards at NNLO even taking scale change into account



extras

# cf. other NNLO results using HERA jets



H1, NNLOJet, APPLfast colls., [EPJ C77 \(2017\) 791](#)

NNLOJET+APPLfast, arXiv:[1906.05303](#)