

# QCD – Lecture 7

implications for and constraints from the LHC, and Beyond

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### the SM is not as well known as you might think

momentum

fractions x1

mass and

rapidity of X

 $M = \sqrt{x_1 x_2 s}$ 

 $y = \frac{1}{2} \ln \frac{x_1}{x_2}$ 

and x2

in the QCD sector, PDFs limit our knowledge; transport PDFs to hadron-hadron cross sections using QCD factorisation theorem

$$\begin{split} \sigma_{\mathbf{X}} &= \sum_{\mathbf{a},\mathbf{b}} \int_{\mathbf{0}}^{\mathbf{1}} \mathbf{d}\mathbf{x}_{\mathbf{1}} \mathbf{d}\mathbf{x}_{\mathbf{2}} \ \mathbf{f}_{\mathbf{a}}(\mathbf{x}_{\mathbf{1}}, \mu_{\mathrm{F}}^{2}) \ \mathbf{f}_{\mathbf{b}}(\mathbf{x}_{2}, \mu_{\mathrm{F}}^{2}) \\ &\times \quad \hat{\sigma}_{\mathbf{a}\mathbf{b}\to\mathbf{X}} \left(\mathbf{x}_{\mathbf{1}}, \mathbf{x}_{\mathbf{2}}, \{\mathbf{p}_{\mathbf{i}}^{\mu}\}; \alpha_{\mathbf{S}}(\mu_{\mathrm{R}}^{2}), \alpha(\mu_{\mathrm{R}}^{2}), \frac{\mathbf{Q}^{2}}{\mu_{\mathrm{R}}^{2}}, \frac{\mathbf{Q}^{2}}{\mu_{\mathrm{F}}^{2}} \right) \end{split}$$

where  $X = W, Z, H, t, jets, prompt-\gamma,...$ and  $\sigma$  is known to some fixed order in pQCD, or in some leading logarithm approximation (LL, NLL) to all orders via resummation





### **PDFs: the situation today**



$$\frac{\partial \mathcal{L}_{ab}}{\partial \tau} = \int_0^1 dx_a dx_b f_a(x_a, M_X^2) f_b(x_b, M_X^2) \,\delta(x_a x_b - \tau) \quad (\tau = M_X^2/s)$$

### why large x PDFs matter

#### BSM searches at LHC currently limited by (lack of) knowledge of large x PDFs



gg initiated – top; Higgs; BSM, EG. gluino pair production, LQs etc.; ...

#### pdf uncertainty dominates

current BSM searches at high mass also limited by **large x valence** and **sea quark** 

4

### and other LHC measurements ...

... such as precision MW, sin<sup>2</sup>**9**W (where small discrepancies may indicate BSM physics) and Higgs, are any infinited by Pore and Higgs are any infinited by Pore and the second second

Channel	$m_{W^+} - m_{W^-}$ [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	Recoil Unc.	Bckg. Unc.	QCD Unc.	EW Unc.	PDF Unc.	Total Unc.
$\begin{array}{l} W \to e\nu \\ W \to \mu\nu \end{array}$	-29.7 -28.6	17.5 16.3	0.0 11.7	4.9 0.0	0.9 1.1	5.4 5.0	0.5 0.4	0.0 0.0	24.1 26.0	30.7 33.2
Combined	-29.2	12.8	3.3	4.1	1.0	4.5	0.4	0.0	23.9	28.0
Manager and an and a second								****		

ATLAS Mw, arXiv:1701.07240





BLUE: vary sin<sup>2</sup>**9**<sub>eff</sub> for fixed pdf ORANGE: NNPDF3.0 pdf uncertainty for fixed sin<sup>2</sup>**9**<sub>eff</sub>

### what do we know well in the SM?

W and Z production have been considered as good standard candle processes with small theoretical uncertainty; **can be used as a luminosity monitor?** 

PDF uncertainty is THE dominant contribution; **most PDF groups quote uncertainties of about 3 –** 4%

BUT PDF uncertainties from one group do not always cover differences BETWEEN groups!

![](_page_5_Figure_4.jpeg)

just a few years ago predictions were coming into better agreement – CTEQ and MSTW predictions agreed well within their quoted uncertainties **BUT new PDF sets have come on to the 'market' which show stronger disagreements** ...

![](_page_6_Figure_0.jpeg)

### why these disagreements?

- use of different **αs(MZ) values**; a common value would bring some of the predictions into better agreement
- different ways of accounting for heavy quark production and different values of the heavy quark mass
- 3. different **input datasets** (or different cuts on data sets), with different levels of consistency and different hidden systematics, EG. evaluation of nuclear target corrections for data taken on heavy targets
- there are differences in philosophy regarding choices of PDF parameterisation and model prejudices which are imposed

![](_page_7_Figure_5.jpeg)

- one example

ed 2015

![](_page_8_Figure_2.jpeg)

10<sup>-4</sup> 10<sup>-3</sup> 10<sup>-2</sup> 10<sup>-1</sup> 1 10<sup>-4</sup>

#### improvement comes

are mostly sea partor

NOTE only experiment

![](_page_8_Figure_7.jpeg)

te the boson

![](_page_9_Figure_0.jpeg)

mass leads to a larger predicted W/Z cross sections

HQ treatment also explains much of difference in ABKM result cf. CTEQ/MSTW, since ABKM treatment is closest to a fully **FFNS** treatment

![](_page_9_Figure_3.jpeg)

![](_page_10_Figure_0.jpeg)

LHC W and Z cross section predictions (at 7 TeV) as a function of charm mass using different HQ schemes

if **fixed Mc** used, spread is considerable BUT if each prediction taken at its **own optimal mass** (determined by treating Mc as a free parameter in the fit – see Lecture 5), spread dramatically reduced

PDFs MSTW08, CTEQ6.6, NNPDF2.0 do NOT use charm mass parameters at the optimal values – this partly explains the differing predictions

(Note, NNPDF has now moved up – GMVFN scheme now used)

### W asymmetry

since PDF uncertainty feeding into all of W+, W- and Z is dominated by the **gluon**, strong correlation in uncertainties, which can be **reduced by taking ratios**,

![](_page_11_Figure_2.jpeg)

### LHC W and Z production and the strange sea

![](_page_12_Figure_1.jpeg)

can we see it?

![](_page_13_Figure_0.jpeg)

### impact of LHC on today's PDFs

![](_page_14_Figure_1.jpeg)

(NNPDF3.1 includes modern  $\sqrt{s}$ =7 and 8 TeV LHC data on W,Z+top+jets+ZPt)

### BSM physics – what do we not know well?

![](_page_15_Figure_1.jpeg)

Tevatron jet data is today considered to lie within PDF uncertainties (EG. CTEQ; arXiv:0303013)

we can decompose PDF uncertainties into eigenvector combinations of fit parameters – largest uncertainty in this case is from eigenvector 15, dominated by high x gluon **PDF** uncertainties matter for **BSM** physics

 EG. Tevatron jet data originally taken as evidence for BSM

something seemed to be going on at high ET; special PDFs like CTEQ4/5HJ were even tuned to describe it better, though quality of fit to other data deteriorated

# BUT this was all before PDF uncertainties were seriously considered!

![](_page_15_Figure_8.jpeg)

### why large x PDFs matter

#### what consequences might our lack of knowledge of the large x gluon have?

EG. such PDF uncertainties in jet cross sections compromise the LHC potential for discovery of new physics; one example: dijet cross section potential sensitivity to compactification scale of **extra spatial dimensions** (Mc) reduced from about  $6 \rightarrow 2$  TeV

![](_page_16_Figure_3.jpeg)

### what about LHC jet data?

![](_page_17_Figure_1.jpeg)

ATLAS inclusive jet cross sections at 7, 8 and 13 TeV, now probing up to pt ~ 3.5 TeV and dijet cross sections up to invariant masses mjj ~ 9 TeV ! (there are also three-jet and four-jet measurements) – and nothing NEW seen so far

### LHC jet cross section measurements

![](_page_18_Figure_1.jpeg)

#### arXiv:<u>1711.02692</u>

measurements have been quantitatively compared to NLO QCD predictions using different PDFs

there is progress in both range and precision of measurements, AND in different PDF predictions, EG. previously ABM11 was very bad (see arXiv:<u>1410.8857</u>), ABMP16 is not **NNLO QCD calculations** also now

available (arXiv:<u>1611.01460</u>, <u>1705.10271</u>)

can we use these data to improve our knowledge of PDFs?

### LHC jet data: impact on global PDF fit

![](_page_19_Figure_1.jpeg)

EG. MMHT PDF (arXiv:1711.05757)

impact on **gluon PDF** from inclusion of inclusive jet data from ATLAS (arXiv:<u>1410.8857</u>), CMS (arXiv:<u>1406.0324</u>), Tevatron (arXiv:<u>1110.3771</u>, <u>0701051</u>)

treatment of correlated systematic uncertainties must be carefully considered for ATLAS jet data, and fitting all data together has proved problematic (MMHT decorrelated certain systematics; issue also seen by ATLAS, CT, NNPDF)

#### can also take ratios of jet cross sections at different CM energies, EG. arXiv:1304.4739

- exp. uncerts. reduced in ratio; PDF sensitivity remains since different beam energies probe different x,Q2 for same pt and y

### HM Drell-Yan and the photon PDF

#### High mass Drell-Yan data can also be searched for BSM effects

![](_page_20_Figure_2.jpeg)

if/when none found, then a precision measurement can improve the knowledge of **high x sea quark PDFs** 

LHC measurements at  $\sqrt{s}=7,8$  TeV showed little PDF discrimination BUT evidence for a QED effect – some events are photon induced, **ie. there is a photonic component in the proton** 

### top-quark pair production

### LHC top quark pair data have sensitivity primarily to high x gluon BUT ATLAS/CMS agreement not very good – particularly for mtt

(and even within a single experiment there are discrepancies when fitting different spectra, see EG. arXiv: 1909.10541)

PDF groups are making choices for these measurements; they use some spectra and not others

![](_page_21_Figure_4.jpeg)

![](_page_22_Figure_0.jpeg)

### Higgs – is it the SM Higgs?

#### what the SM predicts depends on which PDF you chose High-mass BSM cross-sections

![](_page_23_Figure_2.jpeg)

![](_page_23_Figure_3.jpeg)

Must use (at least) NNLO calculations and PDFs – differences to NLO are LARGE (for ggH, N<sup>3</sup>LO QCD now available)

inclusive H production uncertainties (arXiv:<u>1602.00695</u>)

#### Also note the strong $\alpha$ s dependence;

this is a contentious issue; a recent bench-marking study gets better agreement by taking all NNLO PDFs at  $\alpha$ s(MZ) =0.118

PDF+ $\alpha$ s dominant theory uncertainty on calculations of H cross sections

### **Higgs – is it the SM Higgs?**

![](_page_24_Figure_1.jpeg)

Higgs production depends on gg luminosity, which also differs between PDF groups; H(125) is about as good as it gets – still a spread in ggH cross section of  $\mathcal{O}(10\%)$ 

### what we might expect in the future: HL-LHC PDFs

![](_page_25_Figure_1.jpeg)

study PDF constraints expected from LHC measurements by end of the HL-LHC phase (2026 ~ 2038) ATLAS+CMS 3 ab<sup>-1</sup> LHCb 0.3 ab<sup>-1</sup> (studies in arXiv:1810.03639; prepared for CERN

Yellow Report, arXiv:<u>1902.04070</u>)

concentrate on datasets sensitive to mid-to-high-x; and not already systematics dominated

$$sys(14 \text{ TeV}) \sim f_{corr} \times f_{red} \times sys(8/13 \text{ TeV})$$

#### **Hessian profiling of PDF4LHC15**

with tolerance T=3

- systematic uncertainties taken from existing data;
- treated as uncorrelated, with factor fcorr=0.5, chosen to approximately reproduce effect of syst. correlations in existing measurements;
- variable factor fred to estimate improvement to systs.

### **HL-LHC** parton luminosities

![](_page_26_Figure_2.jpeg)

 $f_{red} = \begin{cases} 1/0.5 \ (8/13) \text{TeV} & \text{scenario A: conservative} \\ 0.4/0.2 \ (8/13) \text{TeV} & \text{scenario C: optimistic} \end{cases}$ 

(together with **intermediate** scenario B, all are available in lhapdf format)

### can we do better? ep colliders!

![](_page_27_Figure_1.jpeg)

operating **synchronously** with and using p beam from:

- the HL-LHC (or HE-LHC)
   p: 7 (14) TeV, √s ≈ 1.3 (1.8) TeV
- and/or later using an FCC (LE)
   p: 50 (20) TeV, √s ≈ 3.5 (2.2) TeV

**† FCC (LE):** a lower energy configuration that could operate earlier in an FCC tunnel, using current magnet technology

#### proposed ep colliders: LHeC, FCC-eh

energy recovery LINAC e beam: up to 60 GeV Lint  $\rightarrow$  1 ab<sup>-1</sup> (1000× HERA; per 10 yrs)

![](_page_27_Figure_8.jpeg)

### kinematic coverage

![](_page_28_Figure_1.jpeg)

opportunity for unprecedented increase in DIS kinematic reach. ×1000 increase in lumi. cf. HERA no nuclear corrections, free of symmetry

assumptions,

. . . precision pdfs up to  $x \rightarrow 1$ , and exploration of small x regime; plus extensive additional physics programme

 $\times$ 15/120 extension in Q<sup>2</sup>,1/x reach vs HERA

### quark and gluon pdfs

![](_page_29_Figure_2.jpeg)

s,c,b,t disentangles all flavours; jets for improvement to xg etc.

### pinning down the low x behaviour

#### arXiv:<u>1710.05935</u>

![](_page_30_Figure_2.jpeg)

F2 and FL predictions for simulated kinematics of LHeC and FCC-eh

**ep simulated data very precise** – significant constraining power to discriminate between theoretical scenarios of small x dynamics

#### measurement of FL has a critical role to play

see also arXiv:<u>1802.04317</u>

### why small x matters

![](_page_31_Figure_1.jpeg)

- RECALL: recent evidence for onset of BFKL dynamics in HERA inclusive data
- impact for LHC and most certainly at ultra low x values probed at FCC

### implications for observables at the LHC and beyond

![](_page_32_Figure_1.jpeg)

effect of small x resummation on ggH cross section for LHC, HE-LHC, FCC impact on other EW observables could be of similar size

arXiv:<u>1802.07758</u>; also recent work on forward Higgs production, arXiv:<u>2011.03193</u>; and other processes in progress

### strong coupling, αs at the LHeC

![](_page_33_Figure_1.jpeg)

#### accurate and precise **αs** needed:

to constrain GUT scenarios; for cross section predictions, including Higgs; ...

### **Higgs**

![](_page_34_Figure_1.jpeg)

#### NNNLO pp-Higgs Cross Sections at 14 TeV

as well as αs to potentially permille precision ... LHeC also has an extensive Higgs program in its own right

![](_page_35_Picture_0.jpeg)

### extras

#### Kinematics of a 100 TeV FCC

Plot by J. Rojo, Dec 2013

![](_page_37_Figure_2.jpeg)

small x becomes relevant even for "common" physics (EG. W, Z, H, t)

### the strange sea

![](_page_38_Figure_1.jpeg)

0.2

10-3

x<sup>10<sup>-1</sup></sup>

10-2

39

x<sup>10<sup>-1</sup></sup>

10-2

### impact on valence quarks from ATLAS W and Z

![](_page_39_Figure_1.jpeg)

### top-quark pair production

![](_page_40_Figure_1.jpeg)

![](_page_40_Figure_2.jpeg)

arXiv:1909.10541

- ATLAS 8 TeV ttbar (in lepton+jet decay channel)
- cross section measurements exist differential in several observables, EG. Mtt, ytt
- Mtt wants harder gluon, ytt a softer gluon and is in tension with some other datasets
- these findings have been observed also by other groups: ATLAS, CT, NNPDF ...

### top-quark pair to Z cross section ratios

• measuring ratios has also been suggested as a good discriminator

![](_page_41_Figure_2.jpeg)

EG. **ATLAS ttbar/Z ratio at 13 TeV**: ttbar mostly relates to gluon, Z mostly to quarks; ABM12 too little gluon, many other PDFs not enough Z (recall strangeness study)

### jet cross section ratio measurements

![](_page_42_Figure_2.jpeg)

- even better: take ratios of jet measurements at different CM energies
- EG. ratio of ATLAS 2.76 to 7 TeV inclusive jet cross sections (itself shown as a ratio to NLO QCD)
- experimental uncerts. reduced in ratio and generally smaller than theory uncerts.
- potential for PDF discrimination/constraint since different beam energies probe different x, Q2 values for same pt and y range

### jet cross section ratios

![](_page_43_Figure_1.jpeg)

this is an older result with relatively small statistics, but stands as a proofof-principle comparison of **gluon PDF** for fits using only HERA data compared to using HERA+ATLAS 2.76 and 7 TeV inclusive jets

# gluon becomes harder, uncertainties are reduced

impact stronger than if either 2.76 or 7 TeV data used individually

treatment of correlated systematic uncertainties must be carefully considered for ATLAS jet data; 87 separate sources of correlated uncertainty in this example! Jet energy scale uncertainty down to 3% but taking the ratio is what really helps control it

### V+jets

#### W/Z+Jets is a channel which bridges from SM to BSM physics

EG. looking at ratios such as: W+N-Jets/W+(N–1)-Jets or Z+N-Jets/W+N-Jets is a good way to search for BSM signals while reducing common systematic uncertainties

![](_page_44_Figure_3.jpeg)

Illustrated is MSugra SU(4) compared to Standard Model for 200pb<sup>-1</sup> of data in the W/Z +2 jets channel

### V+jets

#### arXiv:1711.03296

![](_page_45_Figure_2.jpeg)

#### BUT nothing has been seen

current measurements mainly used for testing Monte Carlo modelling of QCD (Sherpa, ALPGEN, MC@NLO, BlackHat)

PDF fits using such measurements have been very recently performed, EG. arXiv:2101.05095 so far, main impact on **d** and **s** sea quarks;

in principle sensitivity also to gluon

![](_page_45_Figure_7.jpeg)

### ptZ

#### JHEP09 (2014) 145 EPJ C76 (2016) 291

![](_page_46_Figure_2.jpeg)

experimentally, very precise

ATLAS: ee,  $\mu\mu$  channels; combined precision better than 0.5% precision for pt < 100 GeV

theoretically challenging — low pt region dominated by soft particle emission (resummation, shower models); high pt region dominated by emission of hard partons (pdfs)

### examples of heavy quark data

![](_page_47_Figure_1.jpeg)

48

### top-quark pair total cross sections

![](_page_48_Figure_1.jpeg)

... already yield PDF discrimination? top cross sections strongly dependent on gg luminosity and on αs(MZ); PDFs which get it right for top should be getting it right for Higgs BUT calculation also depends on top quark mass and whether running mass or pole mass is used

![](_page_49_Figure_0.jpeg)

#### EG. CTEQ; arXiv/<u>0303013</u>

![](_page_50_Figure_1.jpeg)

#### There are CMS inclusive jet and di-jet data from 5fb<sup>-1</sup> of 2011 data

![](_page_51_Figure_1.jpeg)

# A PDF fit of these CMS inclusive jet data together with the combined HERA-I inclusive deep inelastic scattering (DIS) data (JHEP 1001 -109) shows the potential of the CMS data to constrain PDFs, in particular the gluon

![](_page_52_Figure_1.jpeg)

![](_page_52_Figure_2.jpeg)

Note reduced uncertainty and change of shape of both gluon and u-valence The strong coupling constant from a simultaneous fit of PDfs and  $\alpha_{s}(M_{z})$  is  $\alpha_{s}(M_{z}) = 0.1192 \pm 0.0016(exp/NP)$ 

## CMS have recently (arXiv:1703.01630) presented double differential top distributions in mass and rapidity of the t-tbar pair

![](_page_53_Figure_1.jpeg)

When input to a PDF fit these double differential is much more constraining than the single BUT analysis can only be done at NLO presently since there are no predictions at NNLO for the double differential distributions

### **PDF Luminosities**

![](_page_54_Figure_1.jpeg)

### other $\alpha$ s determinations from QCD fits

![](_page_55_Figure_1.jpeg)

### **HL-LHC PDFs**

![](_page_56_Figure_2.jpeg)

all are available in Ihapdf format)

### impact on LHC phenomenology

![](_page_57_Figure_1.jpeg)

### ep colliders

![](_page_58_Figure_1.jpeg)

#### Lepton—Proton Scattering Facilities

**HERA**: world's first and still only ep collider ( $\sqrt{s} \approx 300 \text{ GeV}$ )

LHeC: future ep (eA) collider, proposed to run concurrently with HL/HE-LHC; CDR arXiv:1206.2913 (complementary to LHC; extra discovery channels; Higgs; precision pdfs and αs)

**FCC-eh:** further future **ep** (eA) collider, integrated with FCC (further kinematic extension wrt **LHeC**)

![](_page_59_Figure_0.jpeg)

60

### d/u ratio at large x

![](_page_60_Figure_1.jpeg)

![](_page_60_Figure_2.jpeg)

### LHeC empowering the LHC: Higgs and BSM

![](_page_61_Figure_1.jpeg)

external, reliable, precise **pdfs** needed for

![](_page_61_Figure_2.jpeg)

![](_page_61_Figure_3.jpeg)

#### NNNLO pp-Higgs Cross Sections at 14 TeV

#### arXiv:2007.14491

### **CONTACT INTERACTIONS:** $\mathcal{L}_{CI} = \frac{g^2}{\Lambda^2} \eta_{ij} (\bar{q}_i \gamma_\mu q_i) (\bar{\ell}_i \gamma^\mu \ell_i)$

Model	ATLAS (Ref. $[702]$ )	HL-LHC				
	$\mathcal{L} = 36  \mathrm{fb}^{-1}  (\mathrm{CT14nnlo})$	$\mathcal{L} = 3 \mathrm{ab}^{-1} \;(\mathrm{CT14nnlo})$	$\mathcal{L} = 3  \mathrm{ab}^{-1} \; (\mathrm{LHeC})$			
LL (constr.)	$28{ m TeV}$	$58{ m TeV}$	$96\mathrm{TeV}$			
LL (destr.)	$21{ m TeV}$	$49\mathrm{TeV}$	$77{ m TeV}$			
RR (constr.)	$26{ m TeV}$	$58{ m TeV}$	$84{ m TeV}$			
RR (destr.)	$22{ m TeV}$	$61{ m TeV}$	$75\mathrm{TeV}$			
LR (constr.)	$26{ m TeV}$	$49\mathrm{TeV}$	$81{ m TeV}$			
LR (destr.)	$22{ m TeV}$	$45\mathrm{TeV}$	$62{ m TeV}$			

### **FL at LHeC**

![](_page_62_Figure_1.jpeg)