

# Plasma Wakefield Acceleration and the AWAKE Project at CERN

**Patric Muggli**  
**Max Planck Institute for Physics, Munich**  
[muggli@mpp.mpg.de](mailto:muggli@mpp.mpg.de)



# OUTLINE



- ❑ Introduction to Plasma Wakefield Accelerator (PWFA)
- ❑ Introduction to the self-modulation instability (SMI)
- ❑ SMI experiments at SLAC E209 with  $e^-/e^+$
- ❑ SMI PWFA experiments at CERN with  $p^+$  : AWAKE
- ❑ Summary



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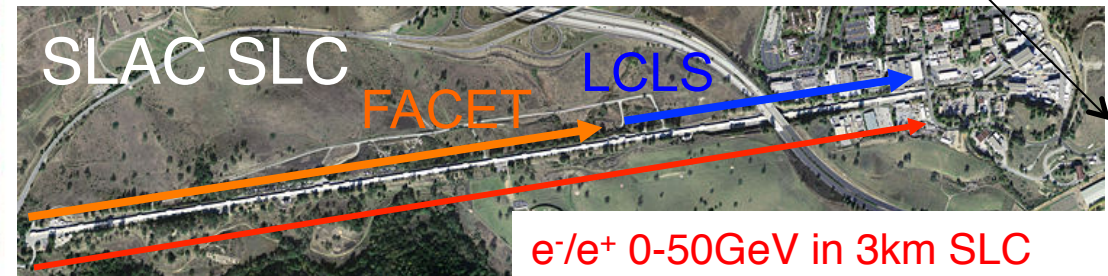
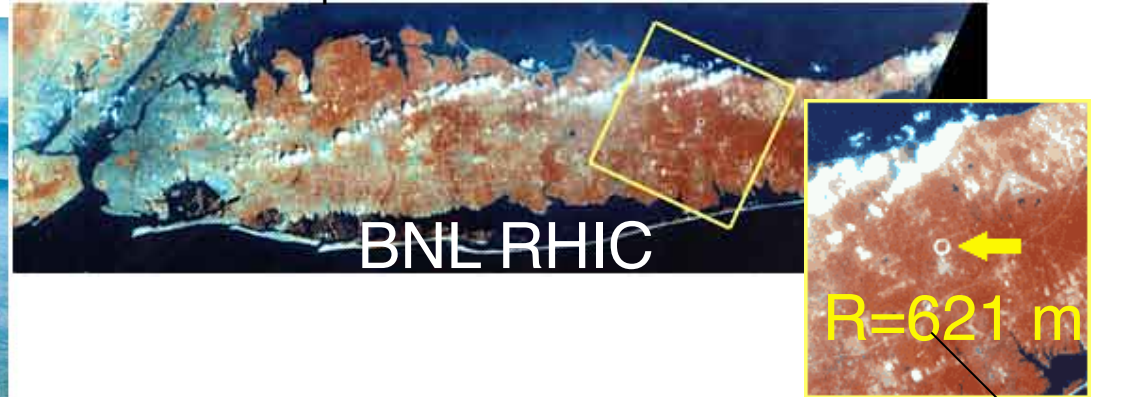


MAX-PLANCK-GESELLSCHAFT

# PARTICLE ACCELERATORS



“The 2.4-mile circumference RHIC ring is large enough to be seen from space”



$e^-/e^+$  0-50GeV in 3km SLC  
 $e^-/e^+$  0-23GeV in 2km FACET  
 $e^-$  0-14GeV in 1km LCLS

- ➡ Some of the largest and most complex (and most expensive) scientific instruments ever built!
- ➡ All use rf technology to accelerate particles
- ➡ Can we make them smaller (and cheaper) and with a higher energy?





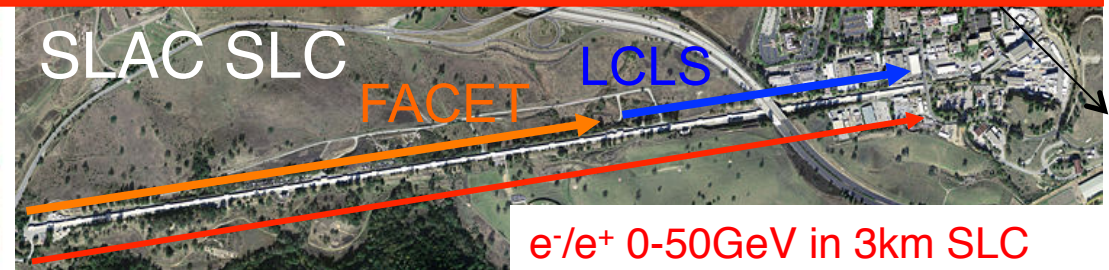


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# PARTICLE ACCELERATORS



Could plasmas be used to accelerate particles at high-gradient ( $>100\text{MeV/m}$ ) and reduce the size and cost of a future linear  $e^-/e^+$  collider or of an x-ray FEL?



$e^-/e^+$  0-50GeV in 3km SLC  
 $e^-/e^+$  0-23GeV in 2km FACET  
 $e^-$  0-14GeV in 1km LCLS

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- ➡ All use rf technology to accelerate particles
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# WHAT ABOUT PLASMAS?



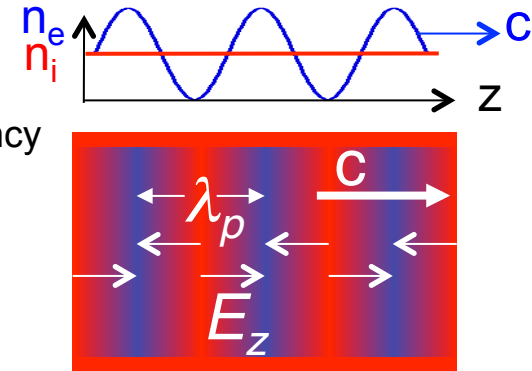
## ➔ Relativistic Electron Electrostatic Plasma Wave (Electrostatic, $E_z$ ):

$$\vec{\nabla} \cdot \vec{E} = \frac{\rho}{\epsilon_0} \quad k_p E_z = \frac{\omega_{pe}}{c} E_z = \frac{n_e e}{\epsilon_0} \quad \omega_{pe} = \left( \frac{n_e e^2}{\epsilon_0 m_e} \right)^{1/2} \text{ Plasma Frequency}$$

$$E_z = \left( \frac{m_e c^2}{\epsilon_0} \right)^{1/2} n_e^{1/2} \cong 100 \sqrt{n_e (cm^{-3})} = 1 \text{ GV} / m$$

Cold Plasma “Wavebreaking” Field

$$n_e = 10^{14} \text{ cm}^{-3}$$



**LARGE**

**Collective response!**

- ➔ Plasmas can sustain very large (collective)  $E_z$ -field, acceleration
- ➔ Wave, wake phase velocity = driver velocity ( $\sim c$  when relativistic)
- ➔ Plasma is already (partially) ionized, difficult to “break-down”
- ➔ Plasmas wave or wake can be driven by:

- Intense laser pulses (LWFA)
- Short particle bunch (PWFA)





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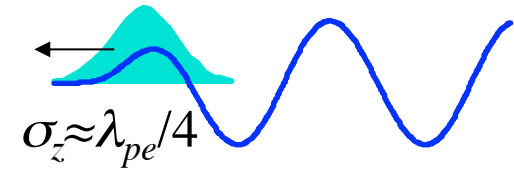
## 4 PLASMA ACCELERATORS\*



- **Plasma Wakefield Accelerator (PWFA)**

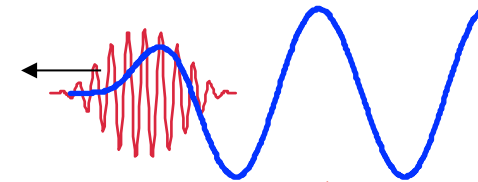
A high energy particle bunch ( $e^-$ ,  $e^+$ , ...)

P. Chen et al., Phys. Rev. Lett. 54, 693 (1985)



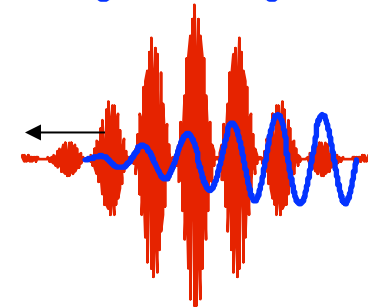
- **Laser Wakefield Accelerator (LWFA)**

A short laser pulse (photons, ponderomotive)



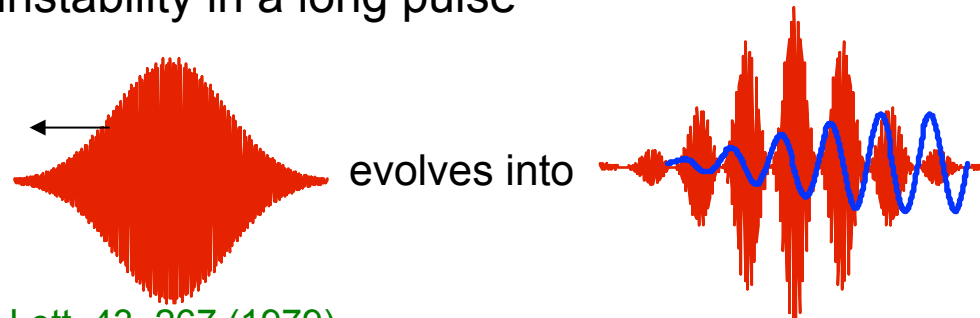
- **Plasma Beat Wave Accelerator (PBWA)**

Two frequencies laser pulse, i.e., a train of pulses



- **Self-Modulated Laser Wakefield Accelerator (SMLWFA)**

Raman forward scattering instability in a long pulse



\*Pioneered by J.M. Dawson, Phys. Rev. Lett. 43, 267 (1979)

© P. Muggli

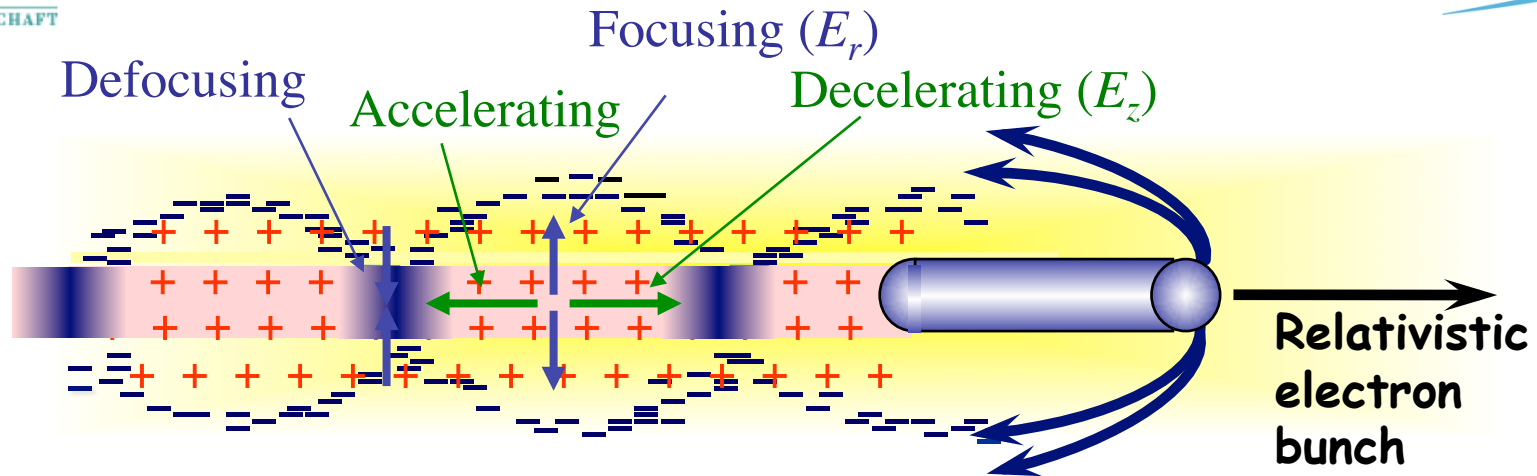
P. Muggli, JAI 21/02/2013





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# PLASMA WAKEFIELDS ( $e^-$ )



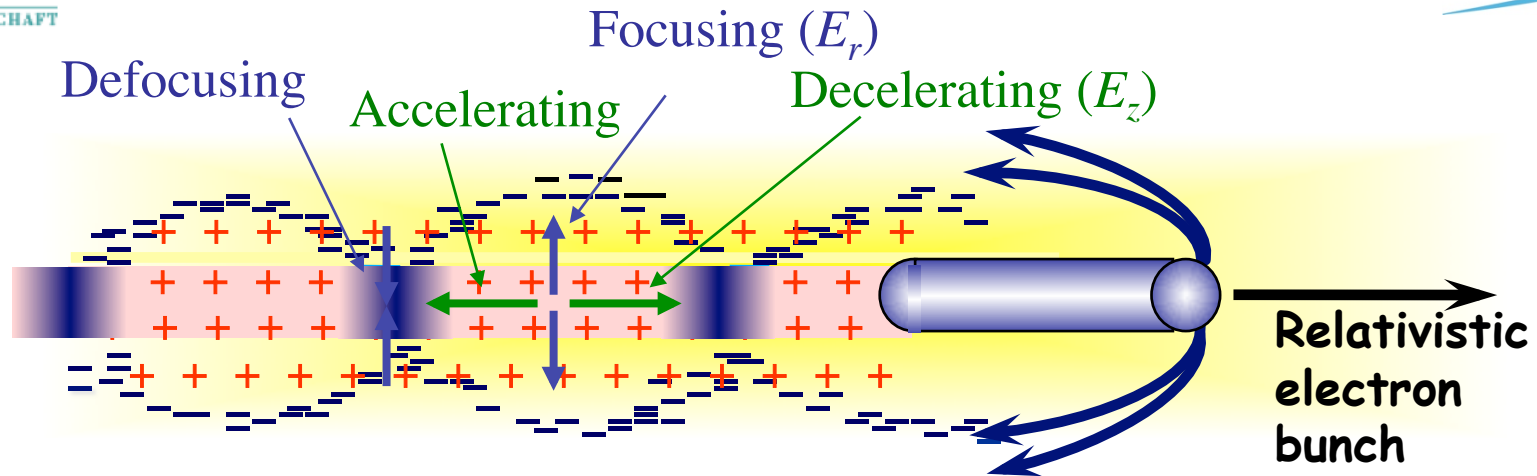
- ➡ Plasma wave/wake excited by a relativistic particle bunch
- ➡ Plasma  $e^-$  expelled by space charge force  $\Rightarrow$  deceleration + focusing (MT/m)
- ➡ Plasma  $e^-$  rush back on axis  $\Rightarrow$  acceleration  $\sim n_e^{1/2}$ , GV/m
- ➡ Ultra-relativistic driver  $\Rightarrow$  Ultra-relativistic wake  
 $\Rightarrow$  No dephasing (...)
- ➡ Particle bunches have long “Rayleigh length”  
(beta function  $\beta^* = \sigma^2 / \epsilon \sim \text{cm, m}$ )
- ➡ Acceleration physics identical PWFA, LWFA





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# PLASMA WAKEFIELDS ( $e^-$ )



→ Plasma wave/wake excited by a relativistic particle bunch

Very large  
energy gain  
possible with  
high-energy  
relativistic  
bunches!

by space charge force => ~~deceleration~~ + focusing (MT/m)

on axis => acceleration  $\sim n_e^{1/2}$ , GV/m

er => ultra-relativistic wake

=> no dephasing (...)

ave long Rayleigh lengths"

$2/\epsilon \sim \text{cm, m}$ )

→ Acceleration physics identical PWFA, LWFA

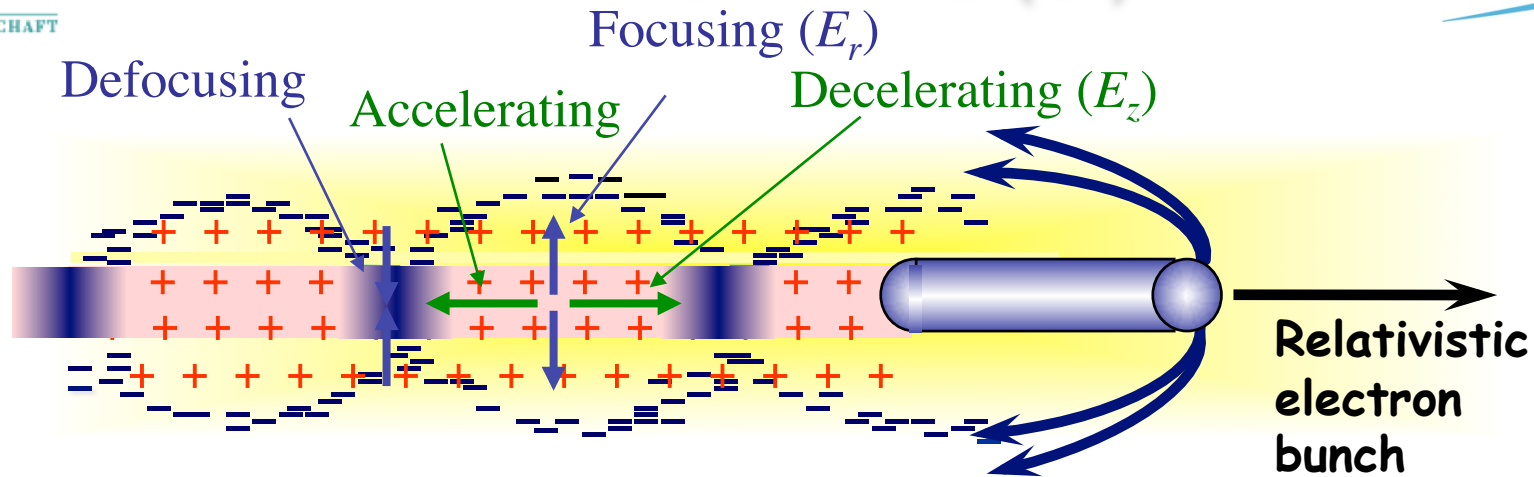






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# PWFA NUMBERS (e<sup>-</sup>)



➔ Linear theory  
( $n_b \ll n_e$ ) scaling:

$$E_{acc} \cong 110 (MV/m) \frac{N/2 \times 10^{10}}{(\sigma_z/0.6mm)^2} \approx N/\sigma_z^2$$

@  $k_{pe} \sigma_z \approx \sqrt{2}$  (with  $k_{pe} \sigma_r \ll 1$ )

➔ Focusing strength:  $\frac{B_\theta}{r} = \frac{1}{2} \frac{n_e e}{\epsilon_0 c} = 3kT/m \times n_e (10^{14} cm^{-3}) \quad (n_b > n_e)$

➔  $N=2 \times 10^{10}$ :  $\sigma_z=600 \mu m$ ,  $n_e=2 \times 10^{14} cm^{-3}$ ,  $E_{acc} \sim 100 MV/m$ ,  $B_\theta/r=6 kT/m$   
 $\sigma_z=20 \mu m$ ,  $n_e=2 \times 10^{17} cm^{-3}$ ,  $E_{acc} \sim 10 GV/m$ ,  $B_\theta/r=6 MT/m$

➔ Frequency: 100GHz to >1THz, “structure” size 1mm to 100 $\mu m$

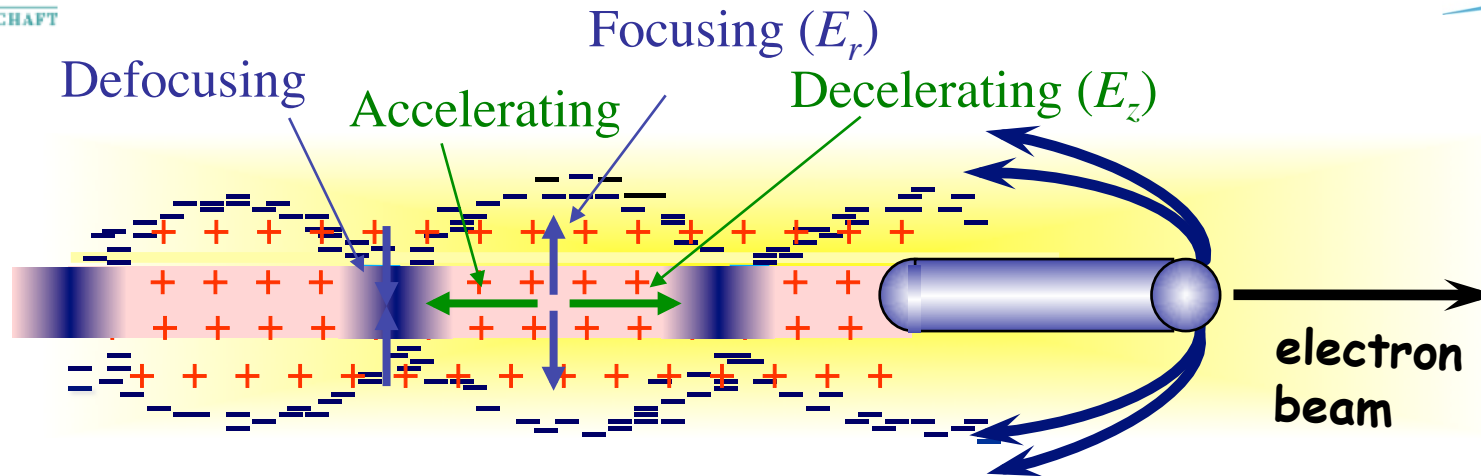
➔ Conventional accelerators: MHz-GHz,  $E_{acc} < 150 MV/m$ ,  $B_\theta/r < 2 kT/m$





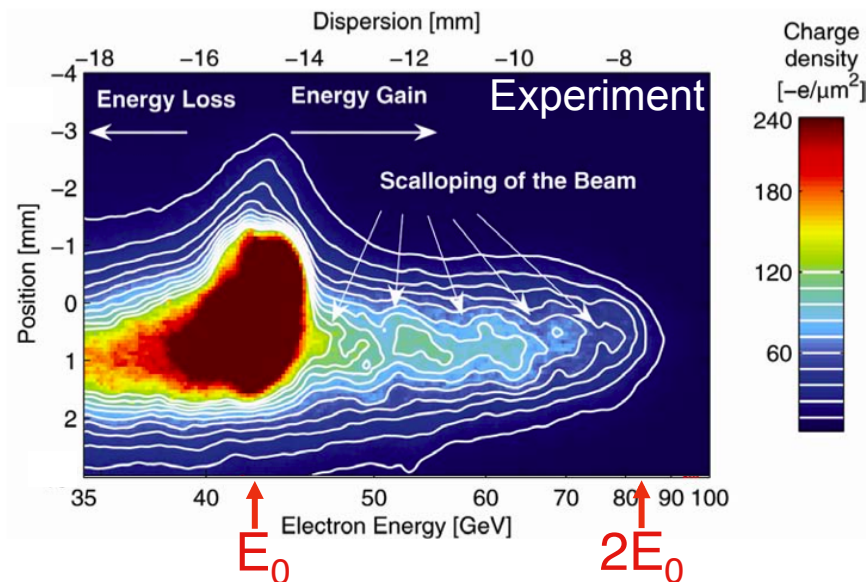
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# PLASMA WAKEFIELDS ( $e^-$ )



P. Muggli and M.J. Hogan, Comptes Rendus Physique, 10(2-3), 116 (2009).

Blumenfeld, Nature 445, 2007



42 => 84GeV in 85cm! 50GeV/m

relativistic particle bunch

forces => deceleration + focusing

=> acceleration

relativistic wake

fields (...)

"lengths"

LWFA

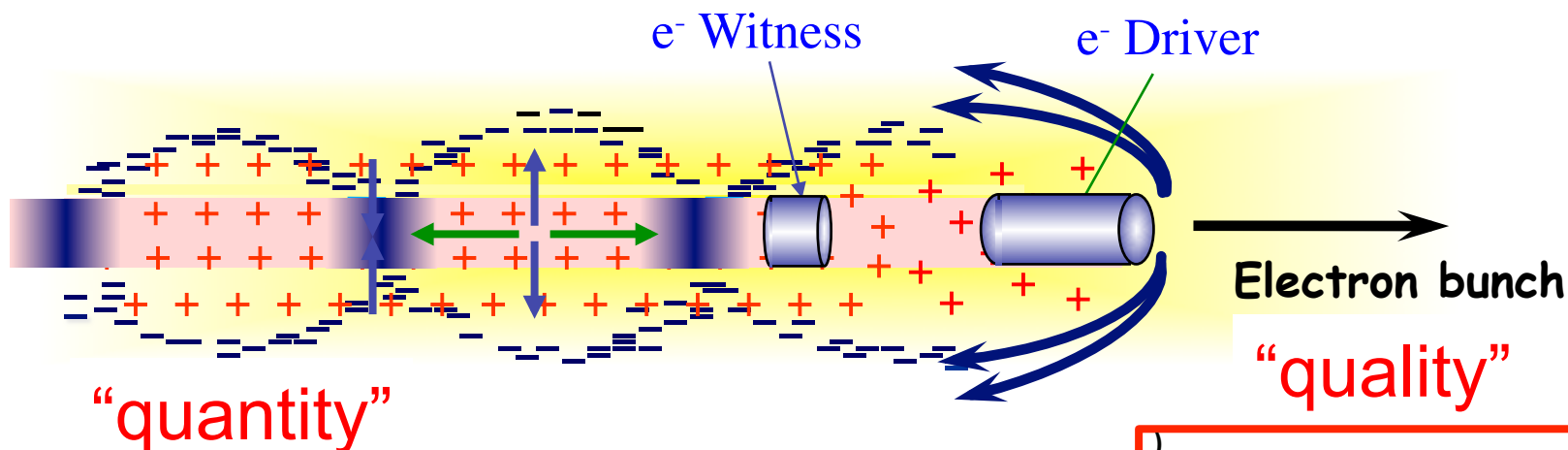


P. Muggli, JAI 21/02/2013

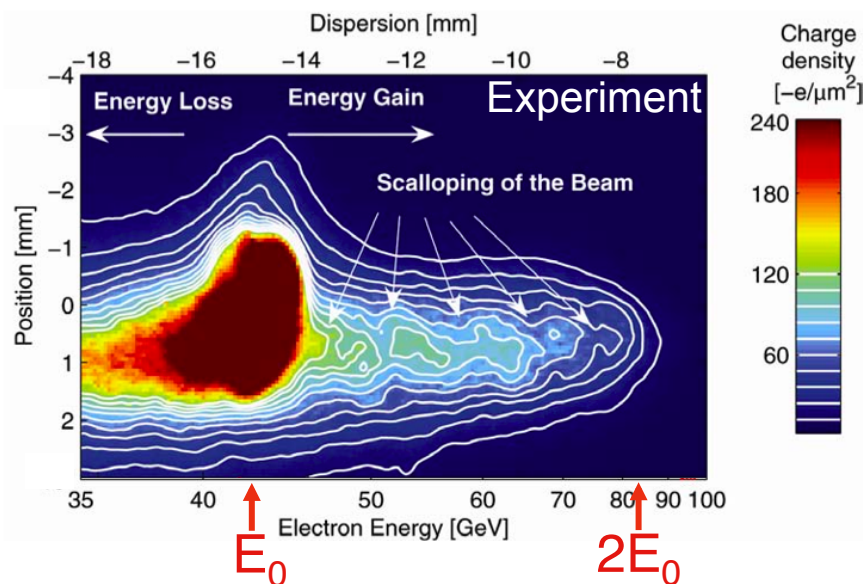


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# PLASMA WAKEFIELDS ( $e^-$ )



Blumenfeld, Nature 445, 2007



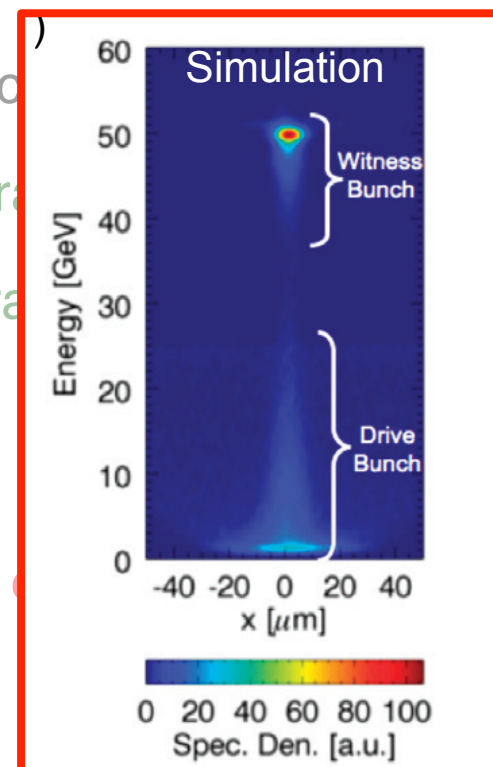
42  $\Rightarrow$  84GeV in 85cm! 50GeV/m

SLAC  
FACET

$\Rightarrow$  acceleration

Hogan,  
NJP 12, 2010

LWFA



P. Muggli, JAI 21/02/2013



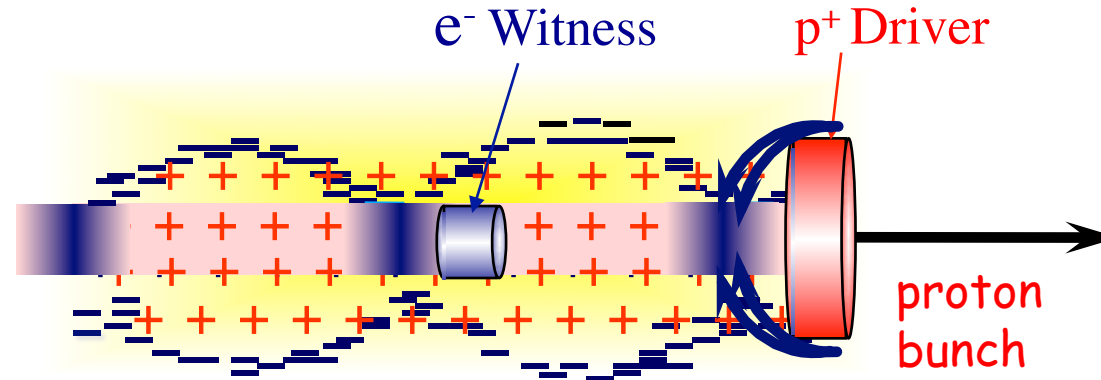
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# PROTON-DRIVEN PLASMA WAKEFIELDS



$(p^+ + e^-)$

## The “Driver Issue”



- ➔ SLAC, 20GeV bunch with  $2 \times 10^{10} e^-$       ~60J Driver  
ILC, 0.5TeV bunch with  $2 \times 10^{10} e^-$       ~1.6kJ Witness
- ➔ SLAC-like driver for staging (FACET= 1 stage, collider  $10^+$  stages)
- ➔ SPS, 450GeV bunch with  $3 \times 10^{11} p^+$       ~22kJ Driver  
LHC, 7TeV bunch with  $3 \times 10^{11} p^+$       ~336kJ Driver
- ➔ A single SPS or LHC  $p^+$  bunch could produce an ILC bunch in a single (or a few) PWFA stage(s)!
- ➔ Large average gradient! (~GeV/m, 100's m)





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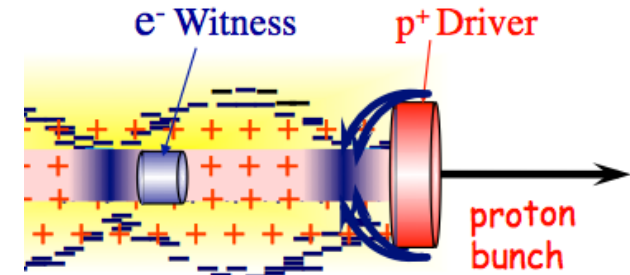
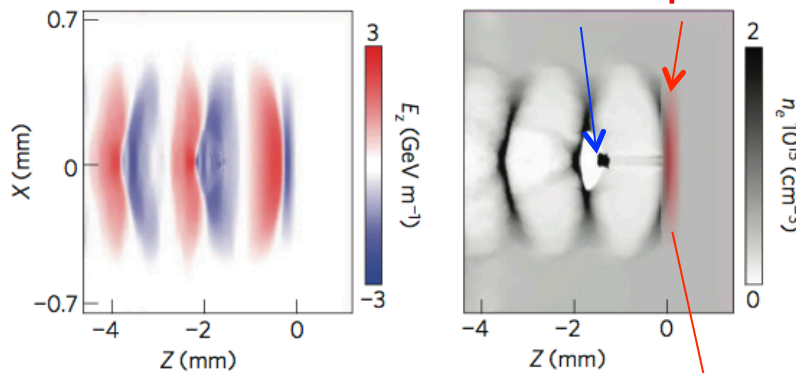
# PROTON-DRIVEN PWFA

Caldwell, Nat. Phys. 5, 363, (2009)

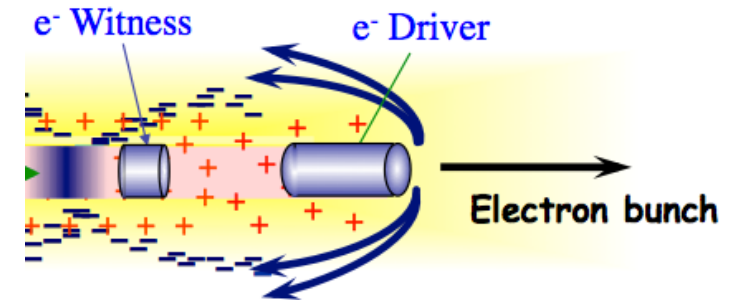


**p<sup>+</sup>:**  
 $E_0 = 1 \text{ TeV}$   
 $\sigma_z = 100 \mu\text{m}$   
 $N = 10^{11} \text{ p}^+$

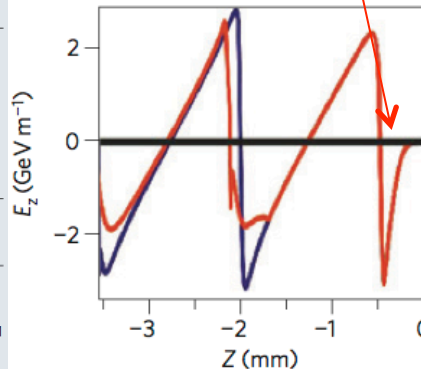
**e<sup>-</sup>:**  
 $E_0 = 1 \text{ GeV}$   
 $N = 10^{11} \text{ e}^-$



Phase difference!



Parameter	Symbol	Value	Units
Protons in drive bunch	$N_p$	$10^{11}$	
Proton energy	$E_p$	1	TeV
Initial proton momentum spread	$\sigma_p/p$	0.1	
Initial proton bunch longitudinal size	$\sigma_z$	100	$\mu\text{m}$
Initial proton bunch angular spread	$\sigma_\theta$	0.03	mrad
Initial proton bunch transverse size	$\sigma_{x,y}$	0.43	mm
Electrons injected in witness bunch	$N_e$	$1.5 \times 10^{10}$	
Energy of electrons in witness bunch	$E_e$	10	GeV
Free electron density	$n_p$	$6 \times 10^{14}$	$\text{cm}^{-3}$
Plasma wavelength	$\lambda_p$	1.35	mm
Magnetic field gradient		1,000	$\text{T m}^{-1}$
Magnet length		0.7	m



- ❑ Use “pancake” p<sup>+</sup> bunch to drive non-linear wake (cylinder for e<sup>-</sup> driver)
- ❑ Gradient ~1.5GV/m (av.)







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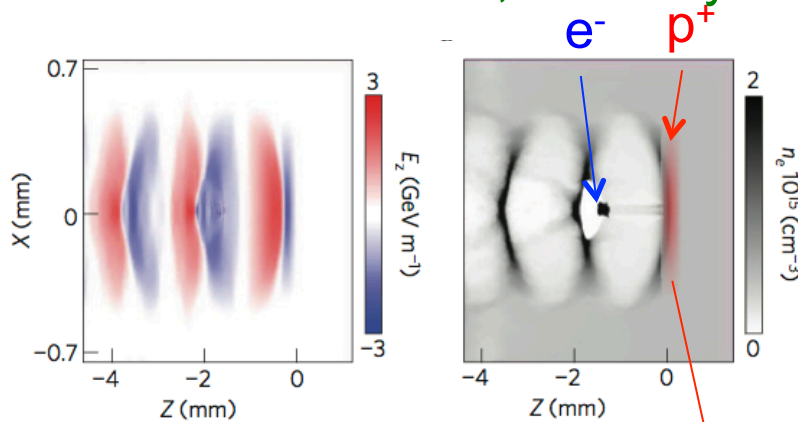
# PROTON-DRIVEN PWFA

Caldwell, Nat. Phys. 5, 363, (2009)

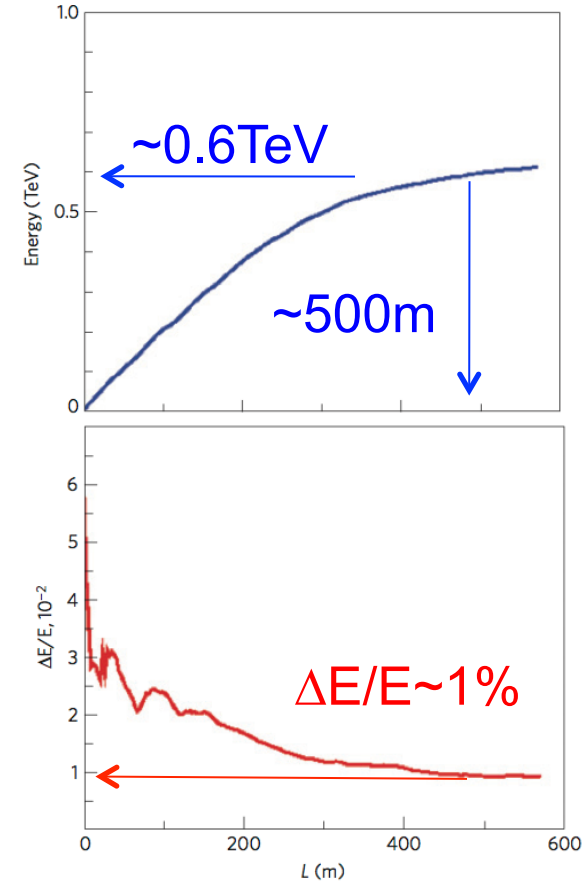
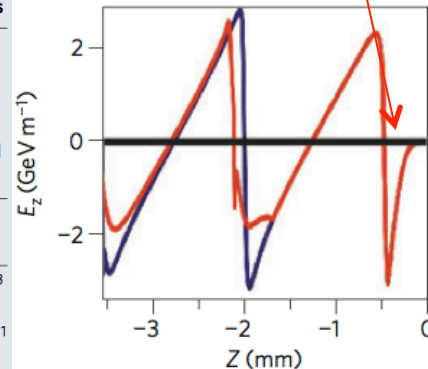


**p<sup>+</sup>:**  
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**e<sup>-</sup>:**  
 $E_0 = 1 \text{ GeV}$   
 $N = 10^{11}$



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- Energy gain  $\sim 600 \text{ GeV}$  in  $\sim 500 \text{ m}$  plasma
- Reasonable energy spread
- Dephasing of (not so) relativistic p<sup>+</sup>

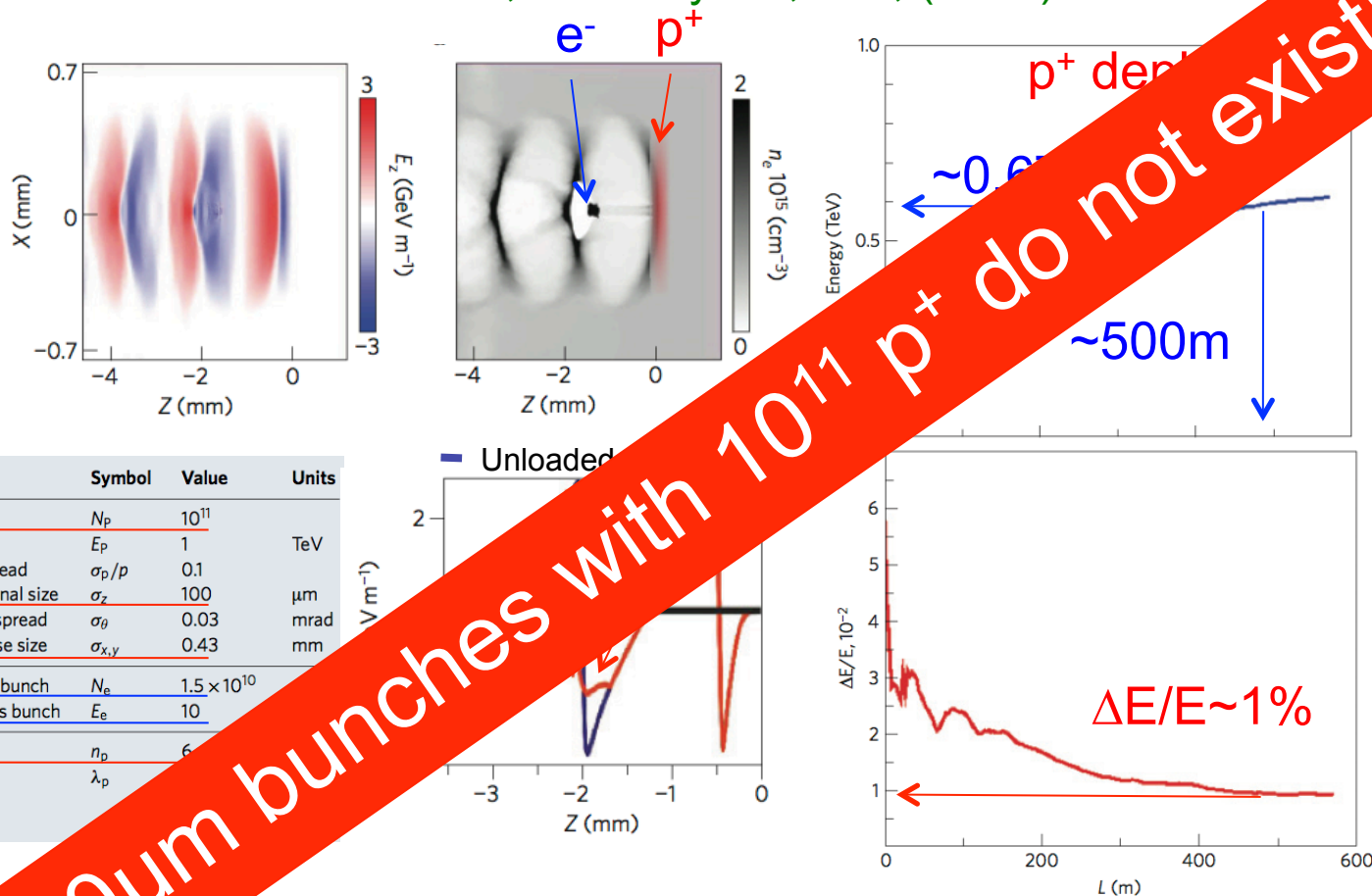




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# PROTON-DRIVEN PWFA

Caldwell, Nat. Phys. 5, 363, (2009)



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Electrons injected in witness bunch	$N_e$	$1.5 \times 10^{10}$	
Energy of electrons in witness bunch	$E_e$	10	
Free electron density	$n_p$	6	
Plasma wavelength	$\lambda_p$		
Magnetic field gradient			
Magnet length			

□  $E_z \approx 1.5 \text{ GV/m}$  (av.), efficiency  $\sim 10\%$

○  $\sigma_z$  like  $e^-$  bunch from a single  $p^+$ -driven PWFA

□ Driver recycling?





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# SELF-MODULATION INSTABILITY (SMI)



- ❑ CERN p<sup>+</sup> bunches (PS, SPS, LHC) ~12cm long

PRL 104, 255003 (2010)

PHYSICAL REVIEW LETTERS

week ending  
25 JUNE 2010

## Self-Modulation Instability of a Long Proton Bunch in Plasmas

Naveen Kumar\* and Alexander Pukhov

*Institut für Theoretische Physik I, Heinrich-Heine-Universität, Düsseldorf D-40225 Germany*

Konstantin Lotov

*Budker Institute of Nuclear Physics and Novosibirsk State University, 630090 Novosibirsk, Russia*

(Received 16 April 2010; published 25 June 2010)

An analytical model for the self-modulation instability of a long relativistic proton bunch propagating in uniform plasmas is developed. The self-modulated proton bunch resonantly excites a large amplitude plasma wave (wakefield), which can be used for acceleration of plasma electrons. Analytical expressions for the linear growth rates and the number of exponentiations are given. We use full three-dimensional particle-in-cell (PIC) simulations to study the beam self-modulation and transition to the nonlinear stage. It is shown that the self-modulation of the proton bunch competes with the hosing instability which tends to destroy the plasma wave. A method is proposed and studied through PIC simulations to circumvent this problem, which relies on the seeding of the self-modulation instability in the bunch.

DOI: 10.1103/PhysRevLett.104.255003

PACS numbers: 52.35.-g, 52.40.Mj, 52.65.-y

- ❑ Idea developed “thanks” to the non-availability of short p<sup>+</sup> bunches
- ❑ Very similar to Raman self-modulation of long laser pulses (LWFA of the 20<sup>th</sup> century)



# OUTLINE

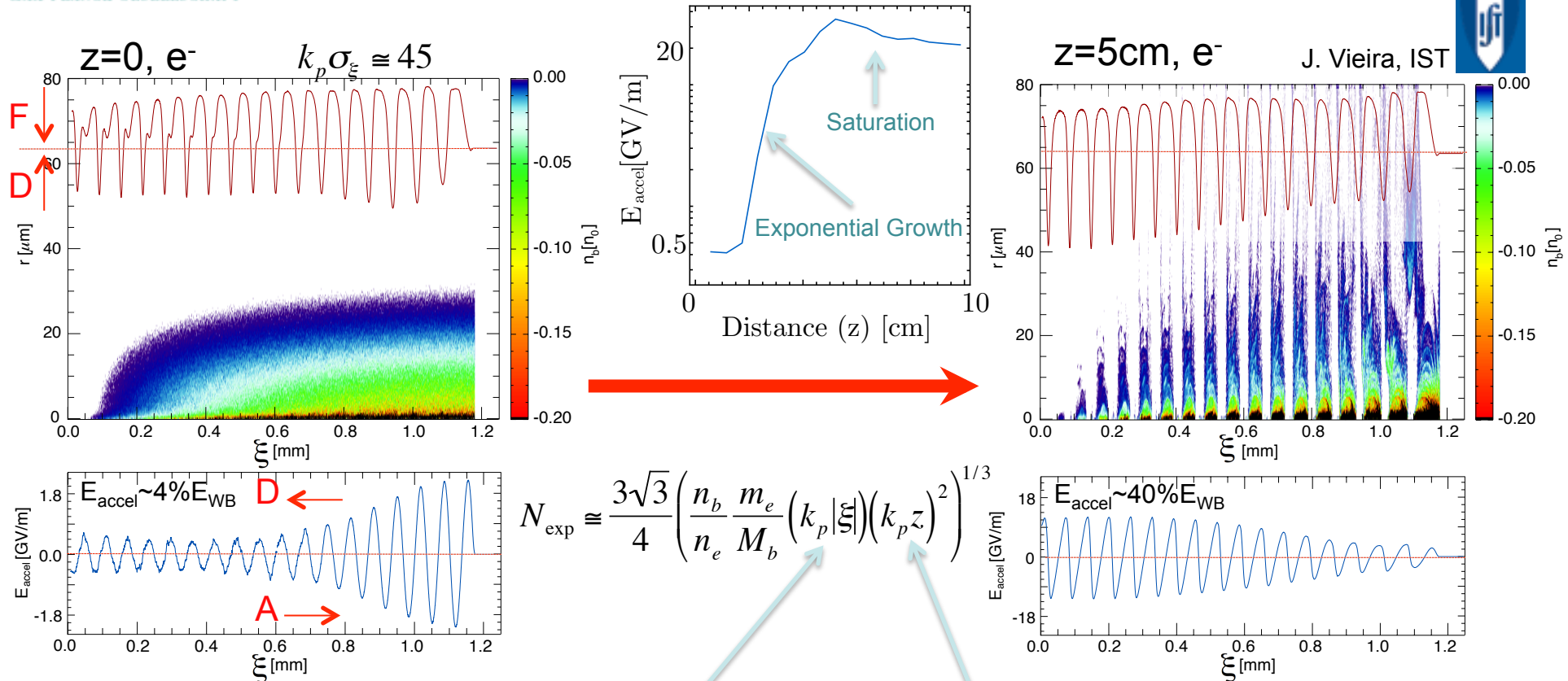
- ❑ Introduction to Plasma Wakefield Accelerator (PWFA)
- ❑ Introduction to the self-modulation instability (SMI)
- ❑ SMI experiments at SLAC E209 with  $e^-/e^+$
- ❑ SMI PWFA experiments at CERN with  $p^+$  : AWAKE
- ❑ Summary





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# SELF-MODULATION INSTABILITY (SMI)



Grows along the bunch & along the plasma  
Convective instability

Pukhov et al., PRL 107, 145003 (2011)  
Schroeder et al., PRL 107, 145002 (2011)

- Initial small transverse wakefields modulate the bunch density
- Associated longitudinal wakefields reach large amplitude through resonant excitation:  $\sim E_{\text{WB}} = mc\omega_{pe}/e \sim 46 \text{ GV/m}$  @  $n_e = 2.3 \times 10^{17} \text{ cm}^{-3}$

J. Vieira et al., Phys. Plasmas 19, 063105 (2012)

P. Muggli, JAI 21/02/2013







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# SM-PWFA PARAMETERS

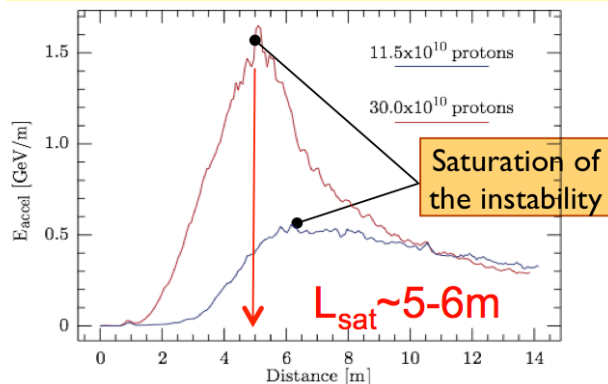


Experimental parameters determined by beam parameters

## CERN AWAKE



- p<sup>+</sup>-driven
- SMI saturates in ~5m
- Study SMI or p<sup>+</sup>-bunches
- Remain in ~linear PWFA regime
- ~GV/m over 10<sup>+</sup> m
- Externally inject e<sup>-</sup>
- Accelerator experiments

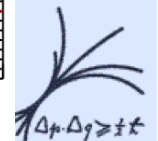
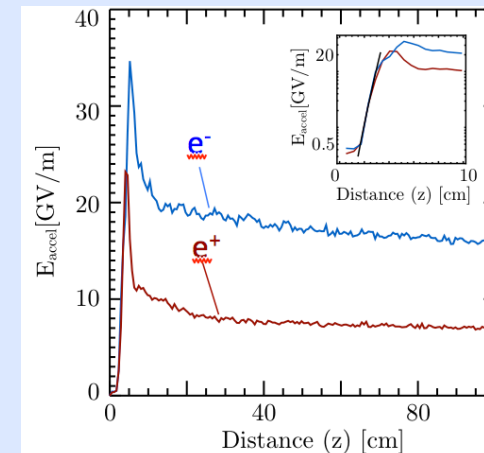


Parameter	PDPWFA	PWFA
$n_e[\text{cm}^{-3}]$	$6 \times 10^{14}$	$2.3 \times 10^{17}$
$f_{pe}[\text{GHz}]$	220	4'300
$\sigma_r[\mu\text{m}]$	200	10
$\sigma_r[c/\omega_{pe}]$	0.9	0.9
$\sigma_\xi[\text{cm}]$	12	$5 \times 10^{-2}$
$\sigma_\xi[c/\omega_{pe}]$	553	45
$\sigma_\xi/\lambda_{pe}$	88	7
$E_0[\text{GeV}]$	400	20.5
$\gamma_0$	426	40'000
$N_{\text{part}}$	$30 \times 10^{10}$	$2 \times 10^{10}$
$n_b/n_0$	$2 \times 10^{-2}$	$10^{-1}$
$L_{\text{plasma}}[\text{m}]$	10	1
$L_{\text{plasma}}[c/\omega_{pe}]$	46'056	90'173
$L_{\text{plasma}}/\lambda_{pe}$	7'330	14'352
$\epsilon_N[\text{mm} \cdot \text{mrad}]$	3.83	50

## SLAC E209



- e<sup>-</sup>/e<sup>+</sup>-driven
- SMI saturates in ~5cm
- Compare SMI of e<sup>-</sup>/e<sup>+</sup> bunches
- Reaches nonlinear PWFA regime
- >10GV/m
- Multi GeV energy gain (drive particles) in ~1m
- SMI diagnostic



P. Muggli, JAI 21/02/2013



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# SMI-PWFA SIMULATIONS

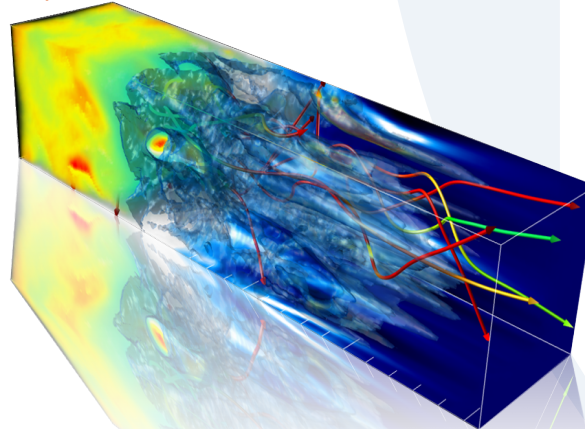


## OSIRIS 2.0



### osiris framework

- Massively Parallel, Fully Relativistic Particle-in-Cell (PIC) Code
- Visualization and Data Analysis Infrastructure
- Developed by the osiris.consortium  
⇒ UCLA + IST

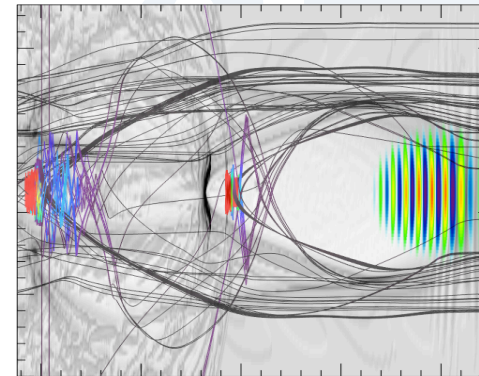


Ricardo Fonseca: [ricardo.fonseca@ist.utl.pt](mailto:ricardo.fonseca@ist.utl.pt)

Frank Tsung: [tsung@physics.ucla.edu](mailto:tsung@physics.ucla.edu)

<http://cfp.ist.utl.pt/golp/epp/>

<http://exodus.physics.ucla.edu/>



### New Features in v2.0

- Bessel Beams
- Binary Collision Module
- Tunnel (ADK) and Impact Ionization
- Dynamic Load Balancing
- PML absorbing BC
- Optimized higher order splines
- Parallel I/O (HDF5)
- Boosted frame in 1/2/3D



Patric Muggli | May 23rd 2012 | IPAC - New Orleans Louisiana, USA

Benchmarking with (for AWAKE only!):

- ❑ OSIRIS: R. A. Fonseca et al., Lect. Notes Comput. Sci. 2331, 342 (2002).
- ❑ VLPL A: Pukhov, J. Plasma Phys. 61, 425 (1999)
- ❑ LCODE: K. V. Lotov, Phys. Rev. ST Accel. Beams 6, 061301 (2003)



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# OUTLINE



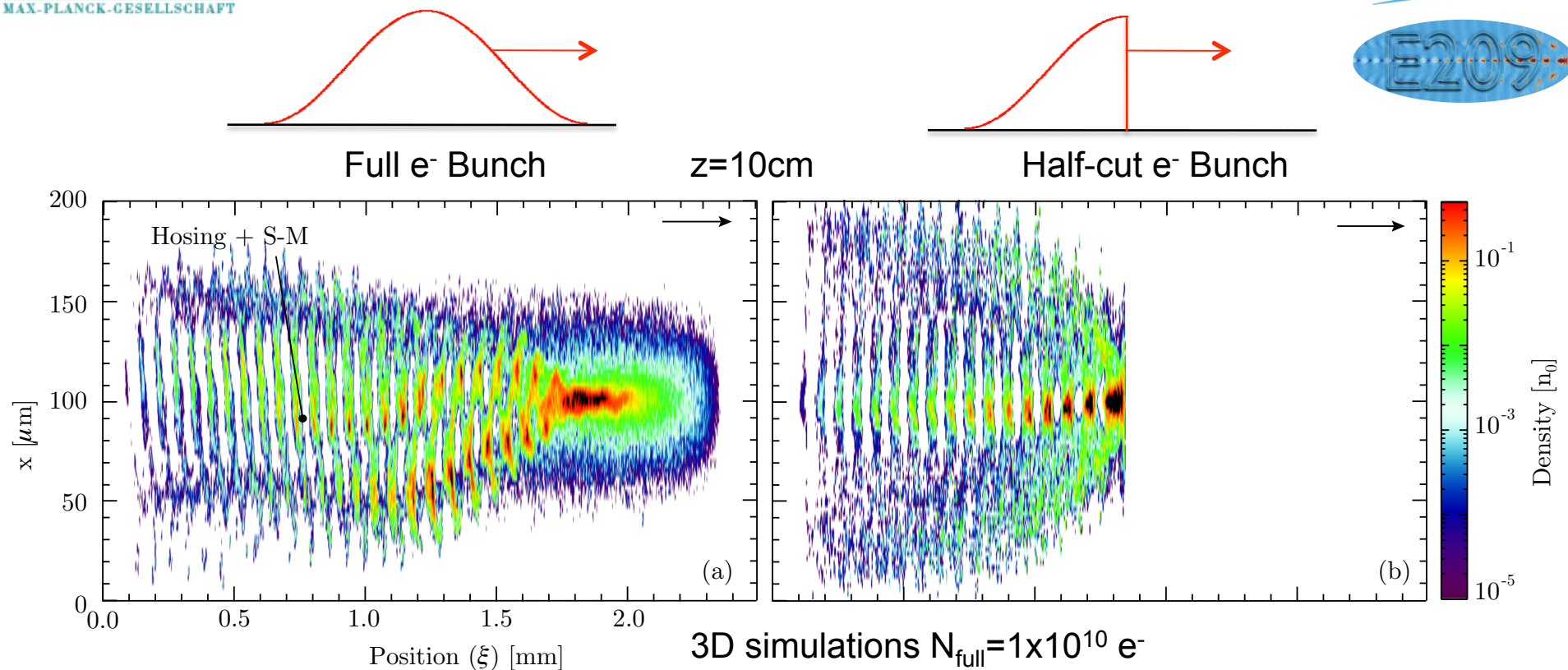
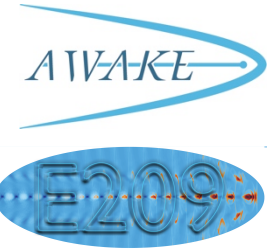
- ❑ Introduction to Plasma Wakefield Accelerator (PWFA)
- ❑ Introduction to the self-modulation instability (SMI)
- ❑ SMI PWFA experiments at SLAC E209 with  $e^-/e^+$
- ❑ SMI PWFA experiments at CERN with  $p^+$  : AWAKE
- ❑ Summary





MAX-PLANCK-GESELLSCHAFT

# SEEDING OF SMI



- ❑ Long bunches in plasmas are subject a two-stream instability or hosing-like instability [Witthum, Phys. Fluids B 4, 730 \(1992\).](#)
- ❑ Seeding SM with shaped bunch decreases hosing (preformed plasma)
- ❑ Use 2D simulations with shaped bunches  $\Leftrightarrow$  no hosing

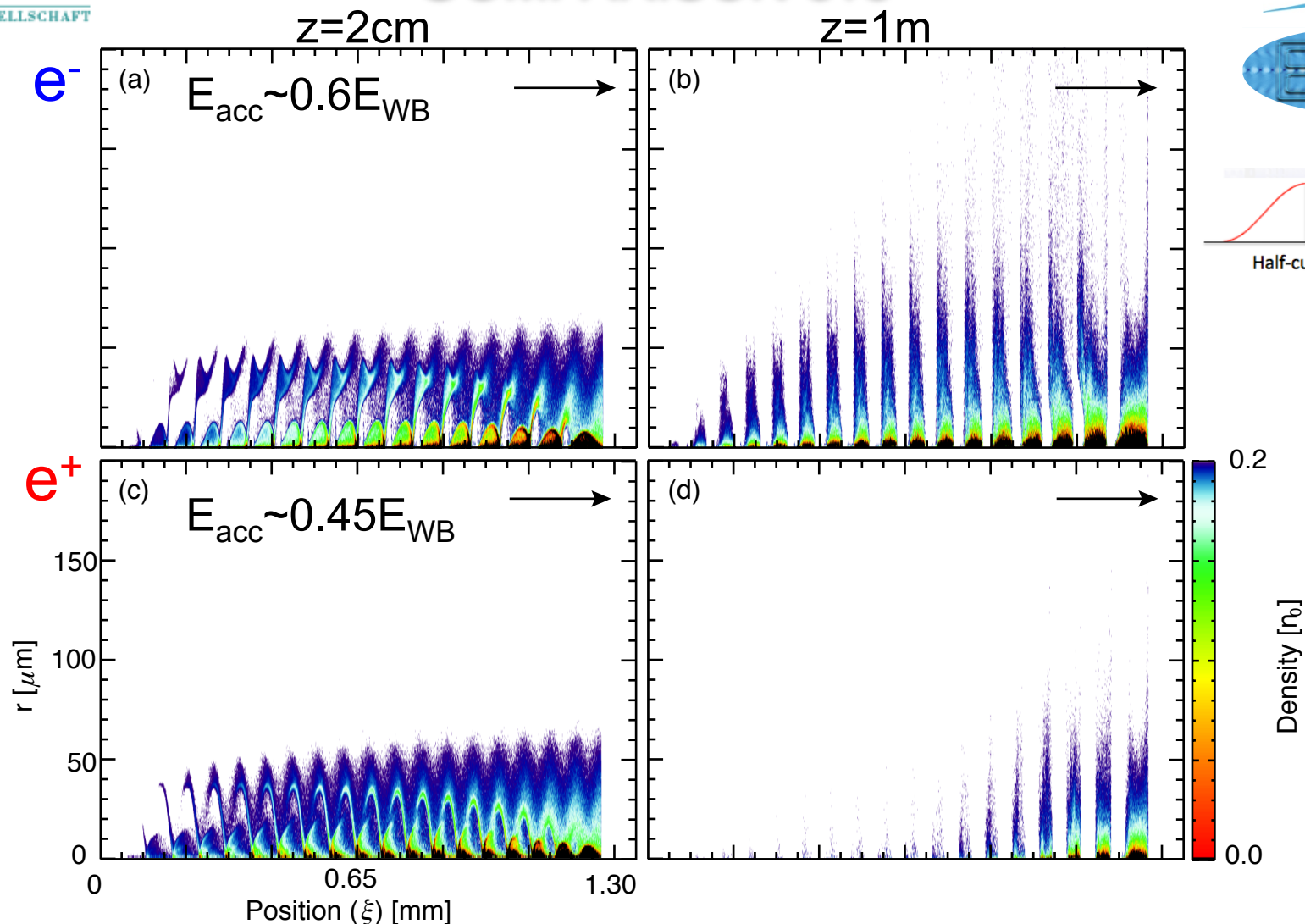






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## COMPARISON $e^-/e^+$



- ☐ SMI of  $e^-$  and  $e^+$  identical only in linear regime ( $E_{\text{acc}} \ll E_{\text{WB}}$ )
- ☐ SMI leads to the resonant excitation of wakefields
- ☐ Less  $e^+$  remain to drive wakefields in the non-linear regime

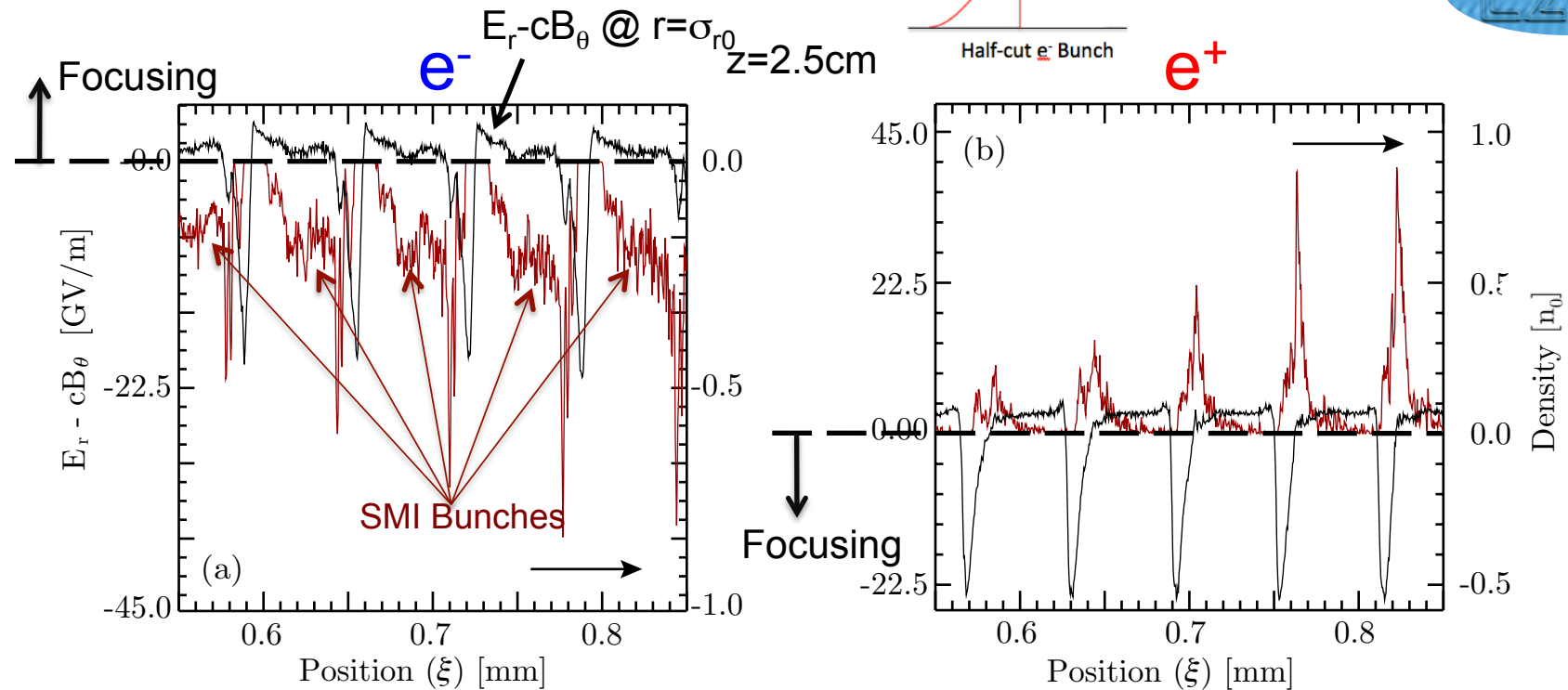
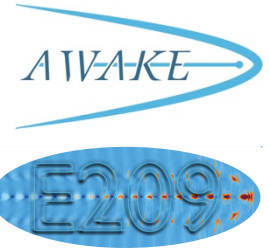






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# FOCUSING NONLINEAR REGIME



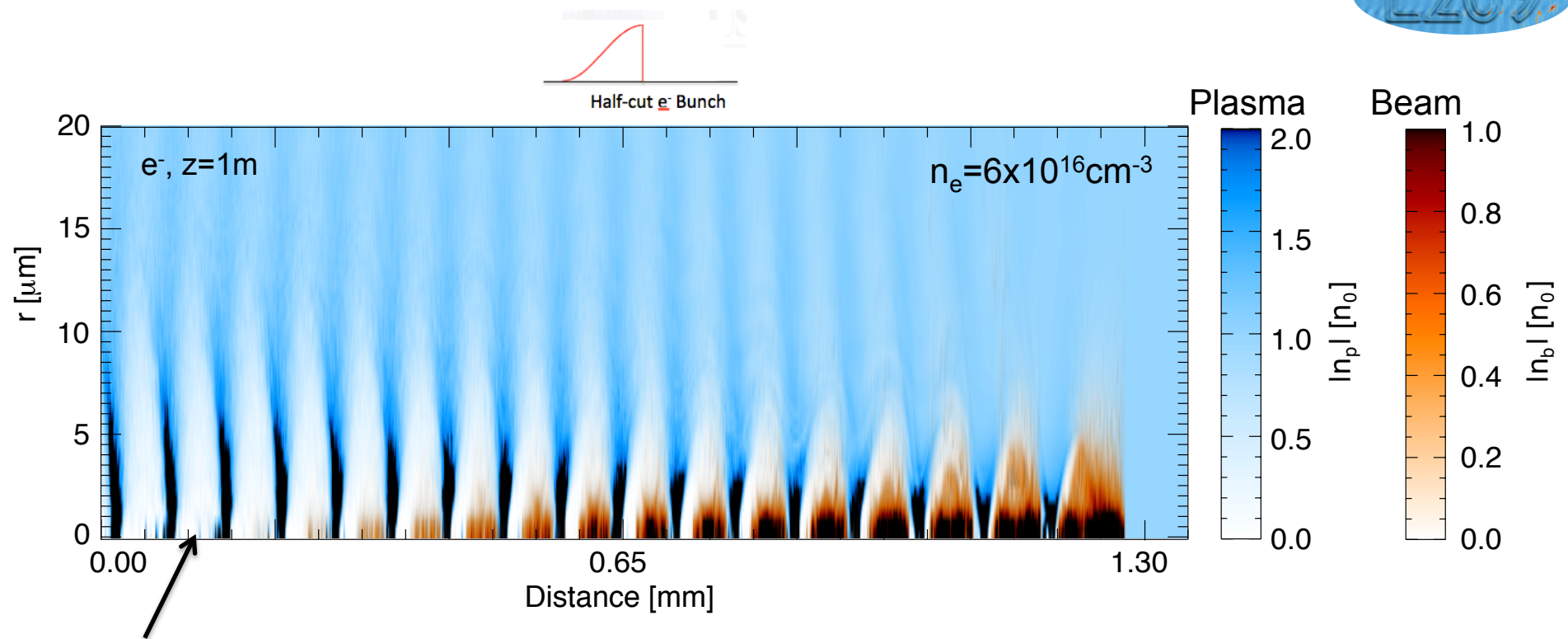
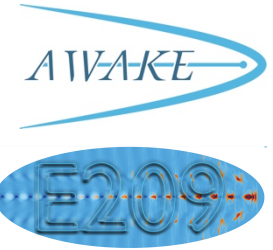
- ❑ Focusing structure in the nonlinear, blowout regime more favorable for  $e^-$  than for  $e^+$
- ❑ More  $e^-$  to drive wakefields to larger amplitudes
- ❑ Focusing and bunch profiles evolve along  $z$





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# WEAKLY NONLINEAR REGIME



Injection of a witness bunch

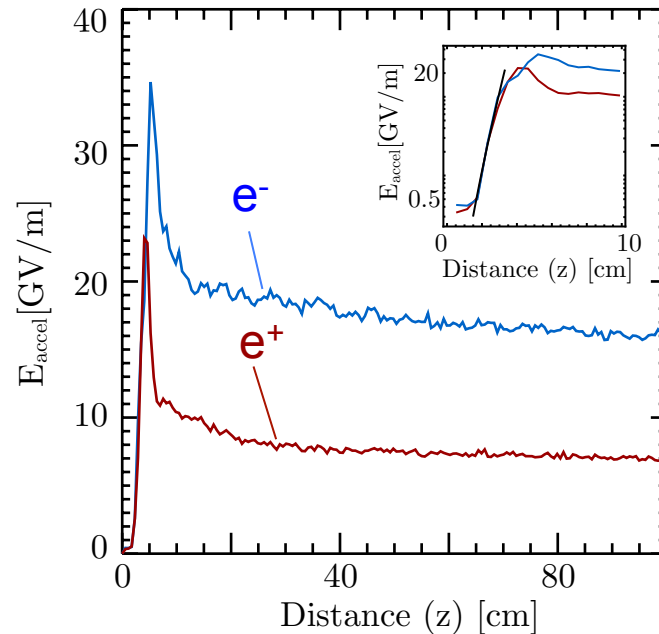
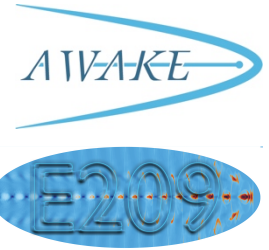
- Evolves into  $n_b > n_e$ , fields add, reach weakly non-linear regime
- “Bubbles”, pure ion column generated, but fields add  $r_{\text{Bubble}} \approx r_{\text{beam}}$



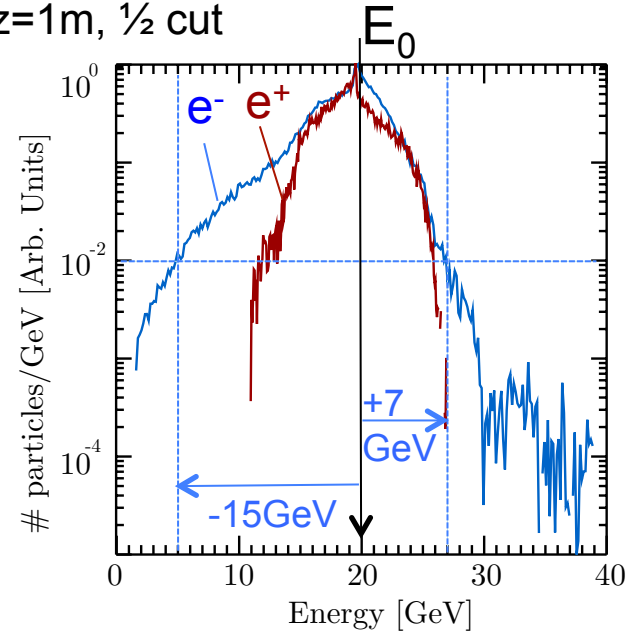


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# WAKEFIELDS & ENERGY CHANGE (by drive particles)



$z=1\text{m}, 1/2 \text{ cut}$



- ❑ Peak SMI wakefield ( $\sim 35\text{GV/m}$ )  $\sim$  single bunch peak field ( $\sim 50\text{GV/m}$ )  
 $E_{\text{WB}} = 46\text{GV/m}$  @  $n_e = 2.3 \times 10^{17}\text{cm}^{-3}$
- ❑ Large energy loss  $> 10\text{GeV}$  ( $e^-$  @ 1%/GeV level)
- ❑ Energy gain  $> 5\text{GeV}$  ( $e^-, e^+$  @ 1%/GeV level)
- ❑ No externally injected particles





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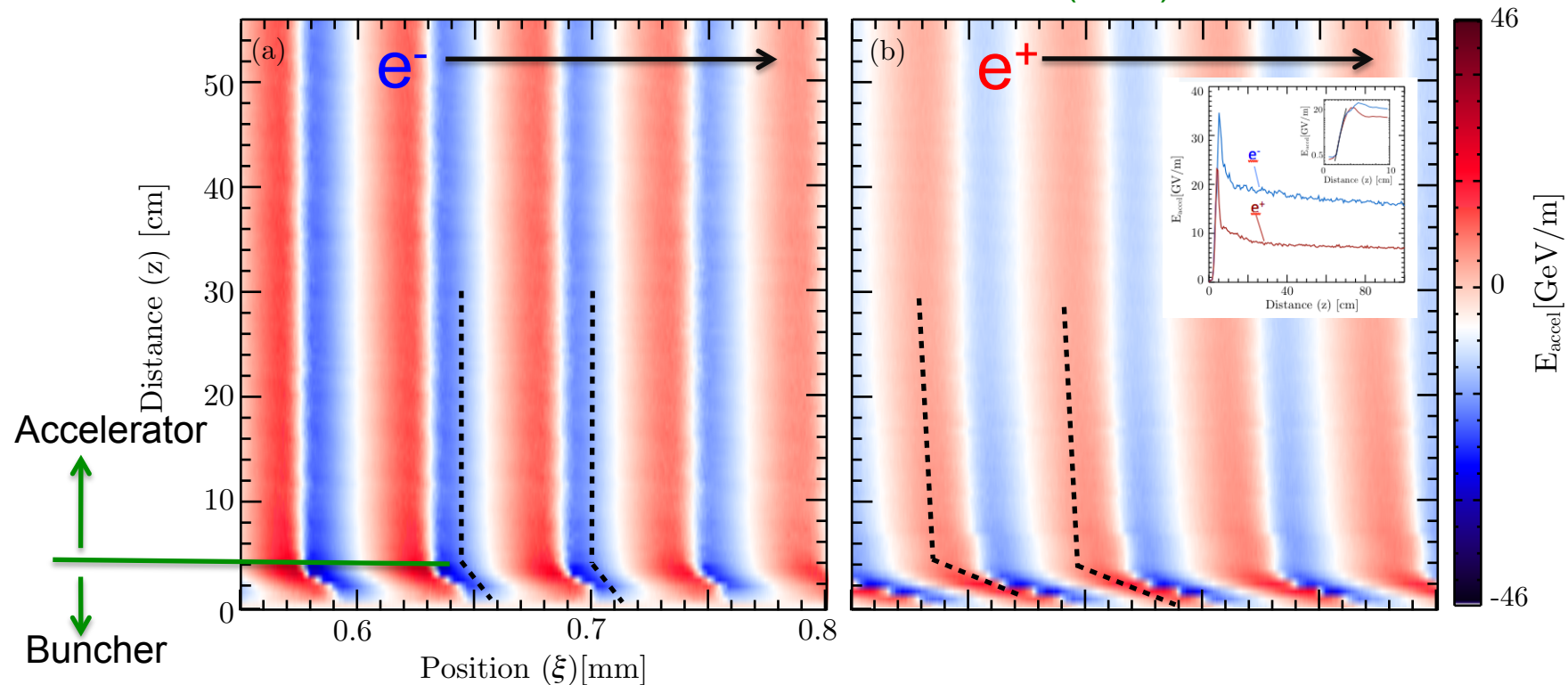
# SMI PHASE VELOCITY

Schroeder et al., PRL 107, 145002 (2011)

Pukhov et al., PRL 107, 145003 (2011)



Half-cut  $e^-$  Bunch



- Wakefield slips “backwards” for  $z < 5\text{cm}$   $\Rightarrow$  buncher  
Wakefield  $\sim v_b \sim c$  for  $z > 5\text{cm}$   $\Rightarrow$  accelerator

- Better structure with  $e^-$  than with  $e^+$

- Observable effect? Not so important since no external injection





- ❑ SMI physics with  $e^-$  and  $e^+$
- ❑ Seeding SMI with shaped bunch in pre-formed plasma
- ❑ SMI – hosing instability competition
- ❑ No externally injected  $e^-$
- ❑ Multi-GeV energy gain/loss in m plasma







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# OUTLINE



- ❑ Introduction to Plasma Wakefield Accelerator (PWFA)
- ❑ Introduction to the self-modulation instability (SMI)
- ❑ SMI experiments at SLAC E209 with  $e^-/e^+$
- ❑ SMI PWFA experiments at CERN with  $p^+$  : AWAKE
- ❑ Summary



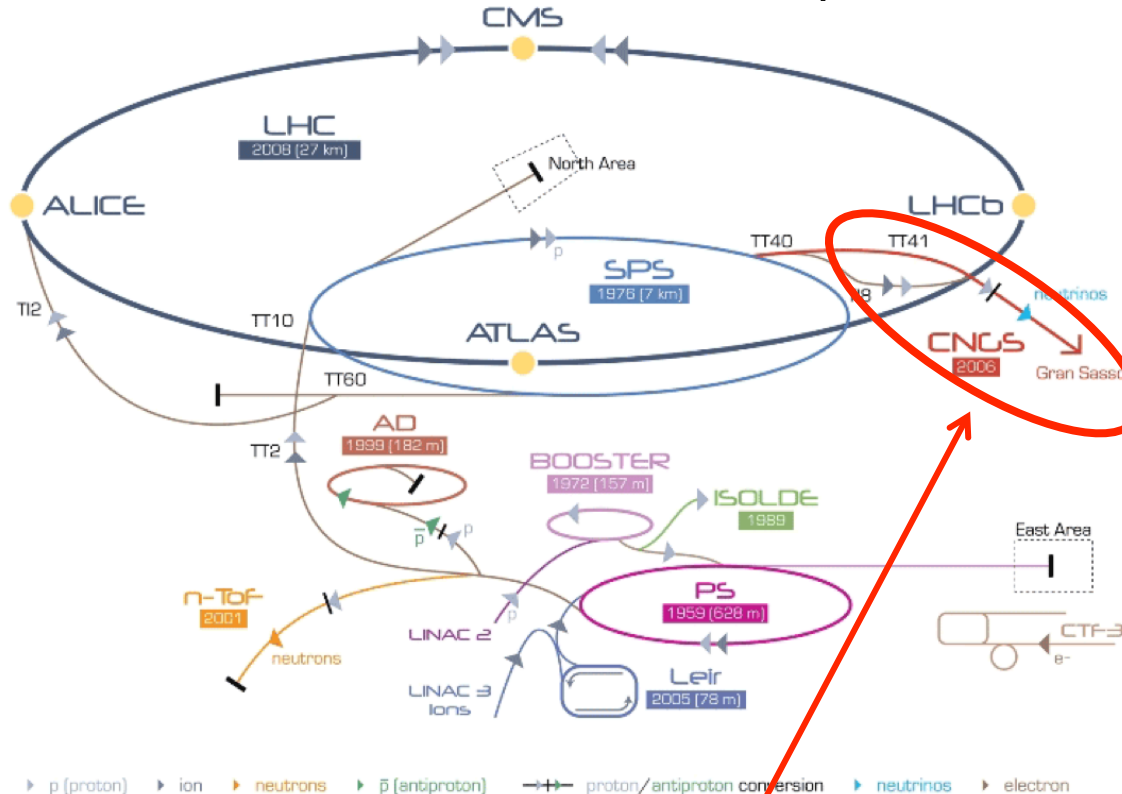


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# PROTON BEAMS @ CERN



## CERN Industrial Beam Complex



CNGS experimental area

Parameter	PS	SPS	SPS Opt
$E_0$ (GeV)	24	450	450
$N_p$ ( $10^{10}$ )	13	10.5	30
$\Delta E/E_0$ (%)	0.05	0.03	0.03
$\sigma_z$ (cm)	20	12	12
$\epsilon_N$ (mm-mrad)	2.4	3.6	3.6
$\sigma_r^*$ ( $\mu\text{m}$ )	400	200	200
$\beta^*$ (m)	1.6	5	5

$L_p \sim 5-10\text{m}$

$n_e \sim 7 \times 10^{14} \text{cm}^{-3}$  ( $k_p \sigma_r \approx 1$ )

$\lambda_{pe} \sim 1.3 \text{mm} \ll \sigma_z = 12 \text{cm}$

$f_{pe} \sim 240 \text{GHz}$

- ❑ Choose SPS beam: Higher energy, low  $\sigma_r^*$ , long  $\beta^*$
- ❑ Goal:  $\sim \text{GeV}$  energy gain by externally injected  $e^-$ , in 5-10m of plasma in self-modulated  $p^+$  driven PWFA





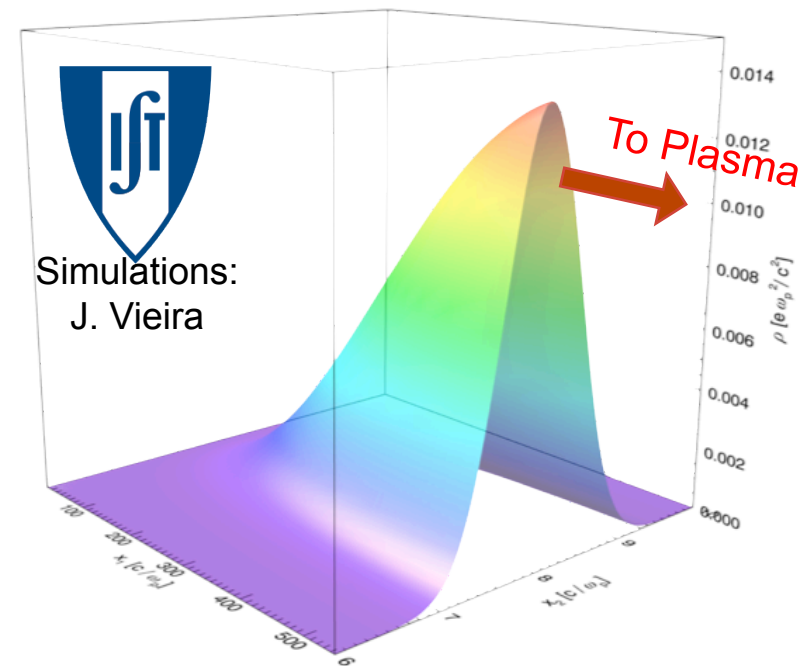
MAX-PLANCK-GESELLSCHAFT

# PROTON-DRIVEN PWFA @ CERN



- ❑ Self-modulation of long ( $\sim 12\text{cm} \sim 100\lambda_{pe}$ ), 450GeV SPS bunch
- ❑ OSIRIS 2D cylindrical simulations

Proton bunch	Electron bunch
<ul style="list-style-type: none"><li>▶ <math>\sigma_{  } = 12\text{ cm}</math></li><li>▶ <math>\sigma_{\perp} = 200\text{ }\mu\text{m}</math></li><li>▶ <math>N = 11.5 \times 10^{10}</math> (<math>30.0 \times 10^{10}</math>)</li><li>▶ <math>n_b/n_0 = 0.00217</math> (linear PWFA)</li><li>▶ <math>\gamma = 479.6</math></li></ul>	<ul style="list-style-type: none"><li>▶ <math>\sigma_{  } = 10\text{ cm}</math> (very long)</li><li>▶ <math>\sigma_{\perp} = 200\text{ }\mu\text{m}</math></li><li>▶ <math>n_b/n_0 = 1.32 \times 10^{-7}</math></li><li>▶ <math>\gamma = 20</math> (10 MeV)</li></ul>
Plasma	Box
<ul style="list-style-type: none"><li>▶ <math>n_0 = 7 \times 10^{14}\text{ cm}^{-3}</math></li><li>▶ <math>\lambda_p = 1.2\text{ mm} \sim \sigma_{  }/100</math></li><li>▶ Uniform density</li><li>▶ Immobile ions</li><li>▶ Length = up to 15 meters</li></ul>	<ul style="list-style-type: none"><li>▶ <math>n_{\perp} = 425</math> cells</li><li>▶ <math>n_{  } = 18000</math> cells</li><li>▶ 4 particles per cell</li><li>▶ quadratic splines</li></ul>



- ❑ Simulations include seeding of the instability (cut  $p^+$  bunch, short ionizing laser pulse)
- ❑ Long, test-particle  $e^-$  witness bunch



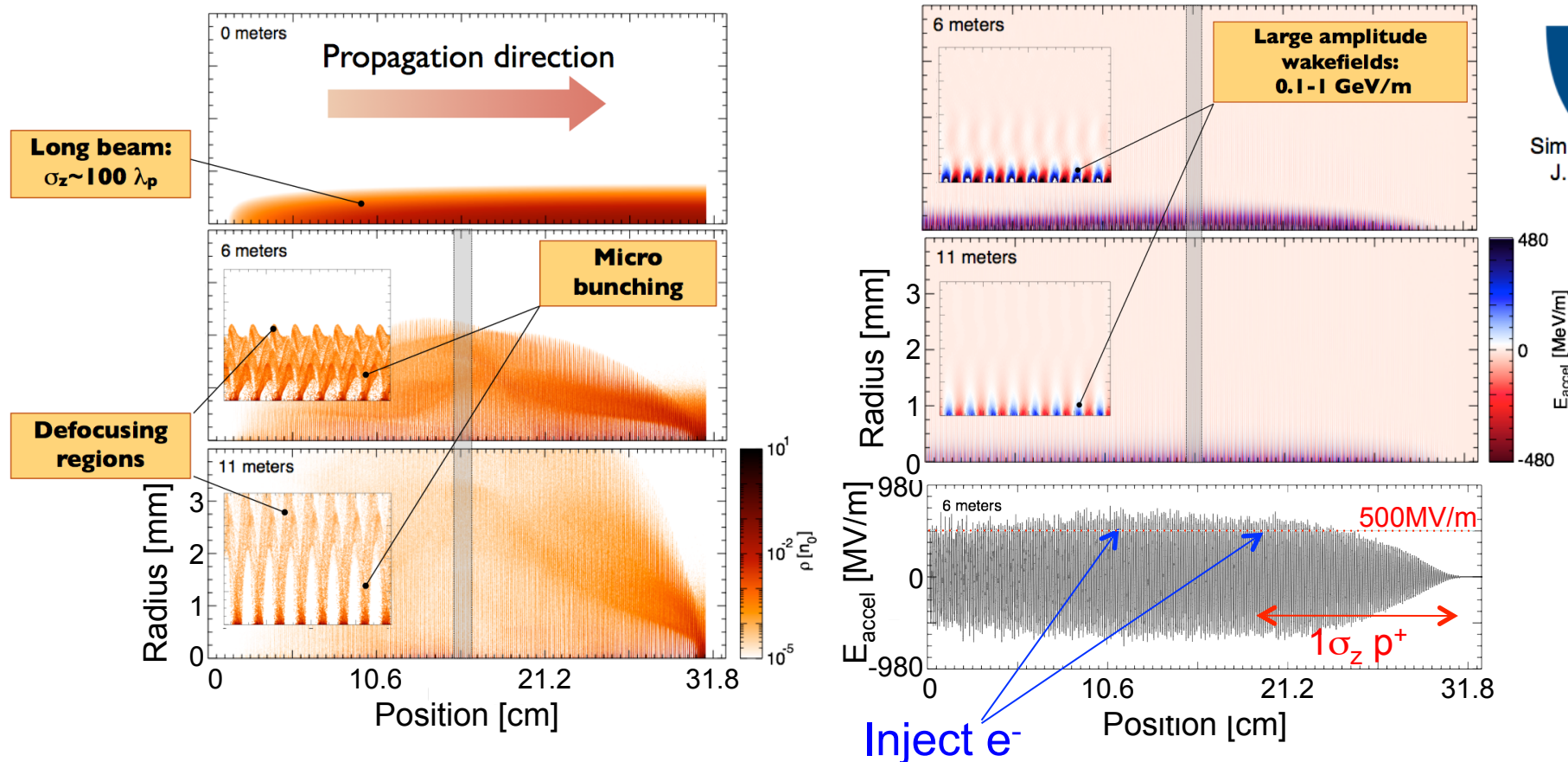


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# PROTON-DRIVEN PWFA @ CERN



- SMI of long ( $\sim 12\text{cm}$ ), 450GeV SPS bunch @  $\lambda_{pe} \approx 1.2\text{mm}$



Simulations:  
J. Vieira

- Drives large amplitude (0.1-1GV/m) accelerating fields
- $E_z$  (acceleration) sampled by injecting ( $\sim 10\text{MeV}$ )  $e^-$  bunch





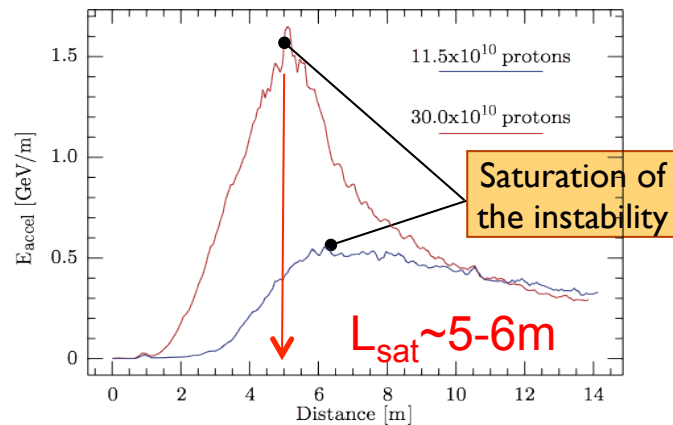
MAX-PLANCK-GESELLSCHAFT

# PROTON-DRIVEN PWFA @ CERN



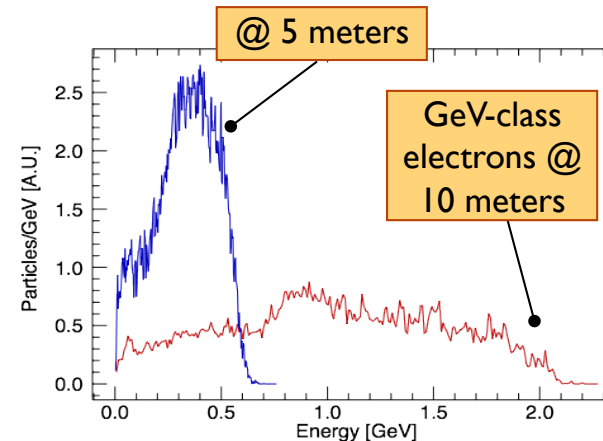
❑ SMI of long ( $\sim 12\text{cm}$ ), 450GeV SPS bunch @  $\lambda_{pe}$

## Maximum accelerating gradients



- ▶ Maximum fields achieved at 5 m of propagation
- ▶ GeV/m wakefields can be excited
- ▶ Wake phase velocity on the order of driver velocity (large dephasing lengths)

## Test electron beam spectra using $3 \times 10^{11} \text{ p}^+$



- ▶ Acceleration of external electrons to high energies
- ▶ High energies can be achieved (once the instability saturates lengths)



Simulations:  
J. Vieira

$\sigma_l = 10 \text{ cm}$  (very long)  
 $\sigma_t = 200 \mu\text{m}$   
 $n_b/n_0 = 1.32 \times 10^{-7}$   
 $\gamma = 20$  (10 MeV)

Test  $e^-$

- ❑ Growth of instability /  $\text{p}^+$  density modulation /  $E_z$
- ❑ Injected  $e^-$  gain  $\sim 1-2\text{GeV}$  in 5-7m plasma
- ❑ Injected of short  $e^-$  bunch would produce narrow  $\Delta E/E$
- ❑ Preserve large  $E_z$  by changing  $n_e$  (K. Lotov)

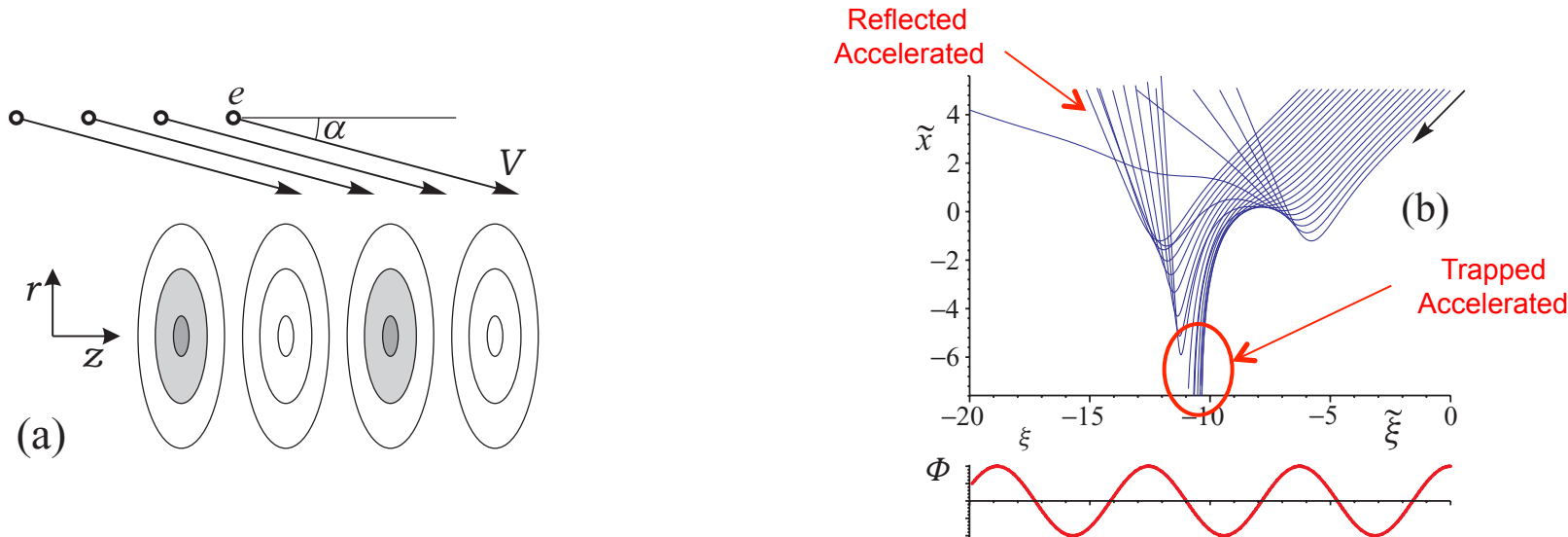




# e<sup>-</sup> SIDE INJECTION

Lotov, J. Plasma Phys. (2012)

- Low energy test e<sup>-</sup> injected sideways are trapped and bunched



$$\alpha_{opt} \sim \frac{v_{\phi} - v_{e-}}{c} \sim \frac{1}{2\gamma_{e-}^2} \sim mrad \quad \text{for } E_{e-} = 5-20 \text{ MeV}$$

- Generates narrow final energy spectrum
- Trapping efficiency <60%, test particles
- Must inject in saturated SMI, where  $v_{\phi} = v_b$





# Phase velocity of the wake

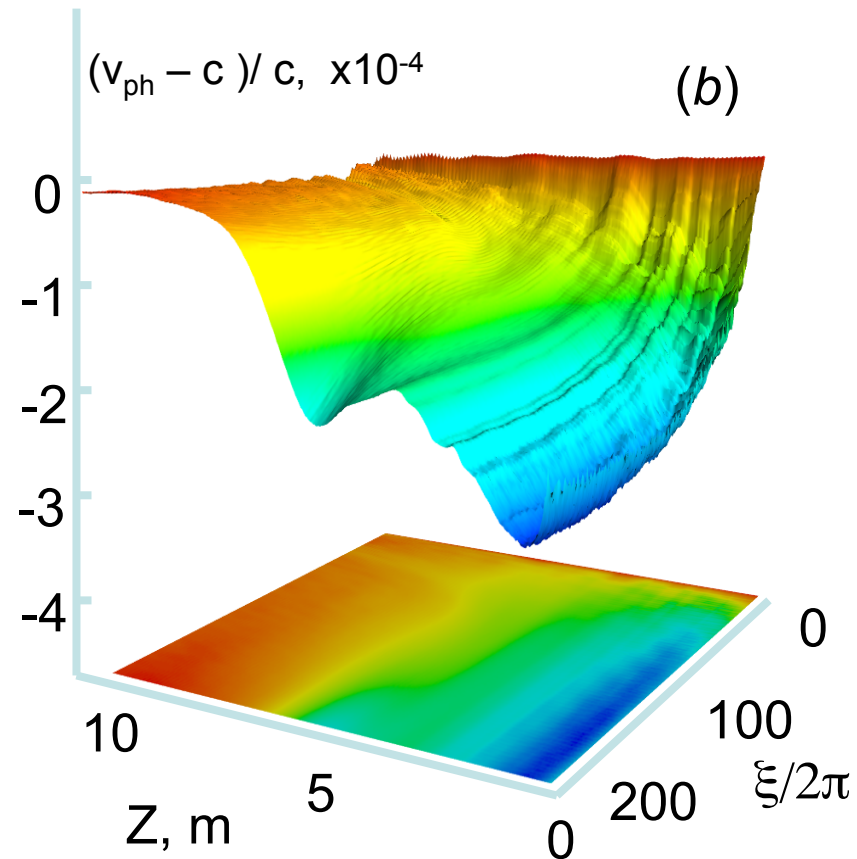
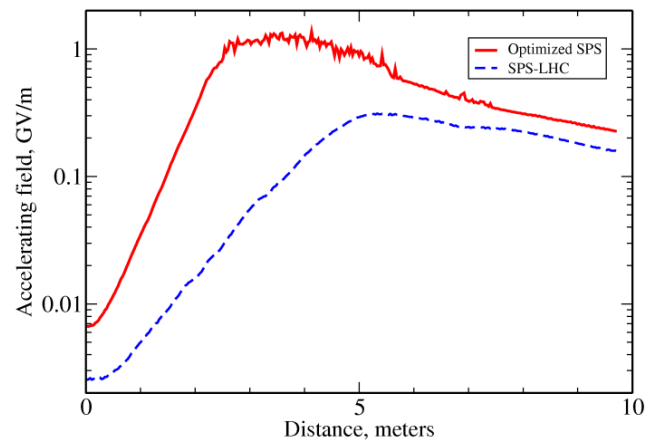
Pukhov et al., Phys Rev Lett (2011)

## HQ-VLPL3D simulation

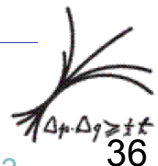
The wake is slowed down. Its minimum gamma-factor is

$$\gamma_{\min} \sim 40$$

This is order of magnitude below that of the beam



pukhov@tp1.uni-duesseldorf.de





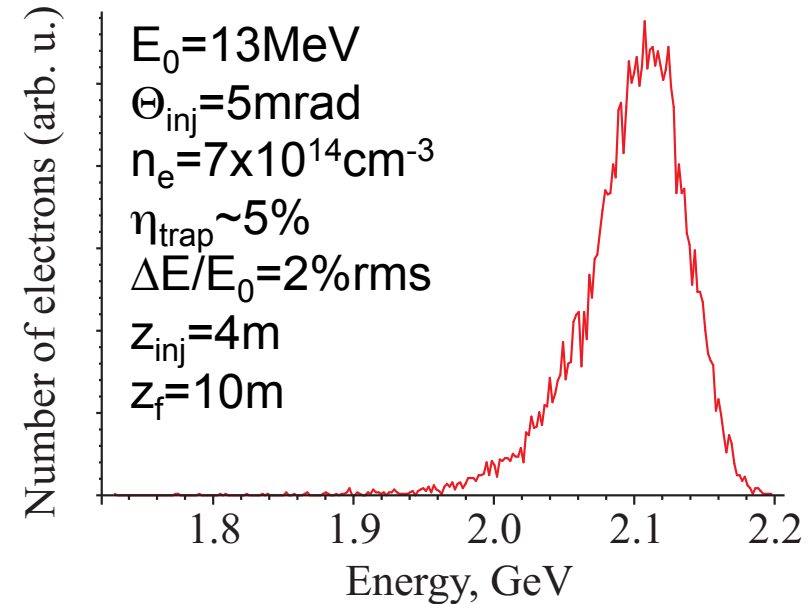
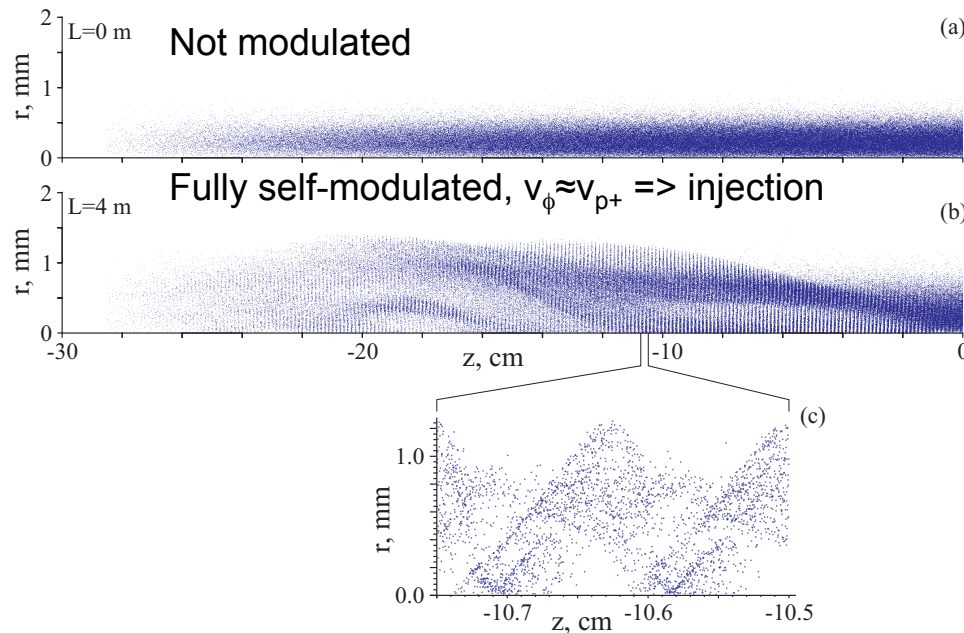
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# SIDE INJECTION SIMULATION RESULTS



**Table 1:** Proton beam parameter at upstream entrance of the plasma cell.

Parameter	Nominal Value
Energy	400GeV
Bunch Intensity	$3 \times 10^{11} \text{ p}^+$
Energy per Bunch	19.2kJ
Repetition Rate	0.03Hz
Energy Spread	0.34% (rms)
Transverse Normalized Emittance	$\epsilon_N = 3.5 \text{ mm-mrad}$
Focused Transverse Size (at $\beta^* = 5 \text{ m}$ )	$\sigma_{t^*} = 0.2 \text{ mm}$
Bunch Length	$\sigma_z = 12 \text{ cm}$
Angle Accuracy	$< 0.05 \text{ mrad}$
Pointing Accuracy	$< 0.5 \text{ mm}$
Focal Position	Plasma Cell Entrance
Number of Run Periods/Year	4
Length of Run Period	2 weeks
Total Number of Protons/Year	$4.86 \times 10^{16}$



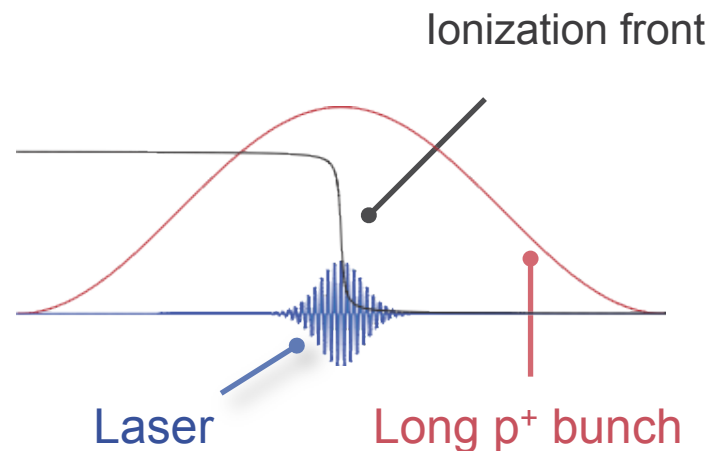
Results from LCODE, K. Lotov



# Creating plasma and cut proton bunch simultaneously ionizing laser pulse



## Laser pulse on top of proton bunch



- ▶ Laser pulse creates ionization front
- ▶ Ionization front acts as if long proton bunch is sharply cut
- ▶ Laser pulse excites wakes to directly seed the instability

D. Gordon et al, PRE, **64** 046404 (2001).

## PIC simulations are demanding

- ▶  $\omega_0/\omega_{pe} \sim 1000 - 4000$
- ▶ 1000-4000x smaller  $\Delta x_{||}$
- ▶ 1000-4000x more CPUh
- ▶ **~10 million CPUhours using standard full-PIC for 5 m**

## Equation for the laser envelope Ponderomotive guiding center

Equation for laser pulse envelope:

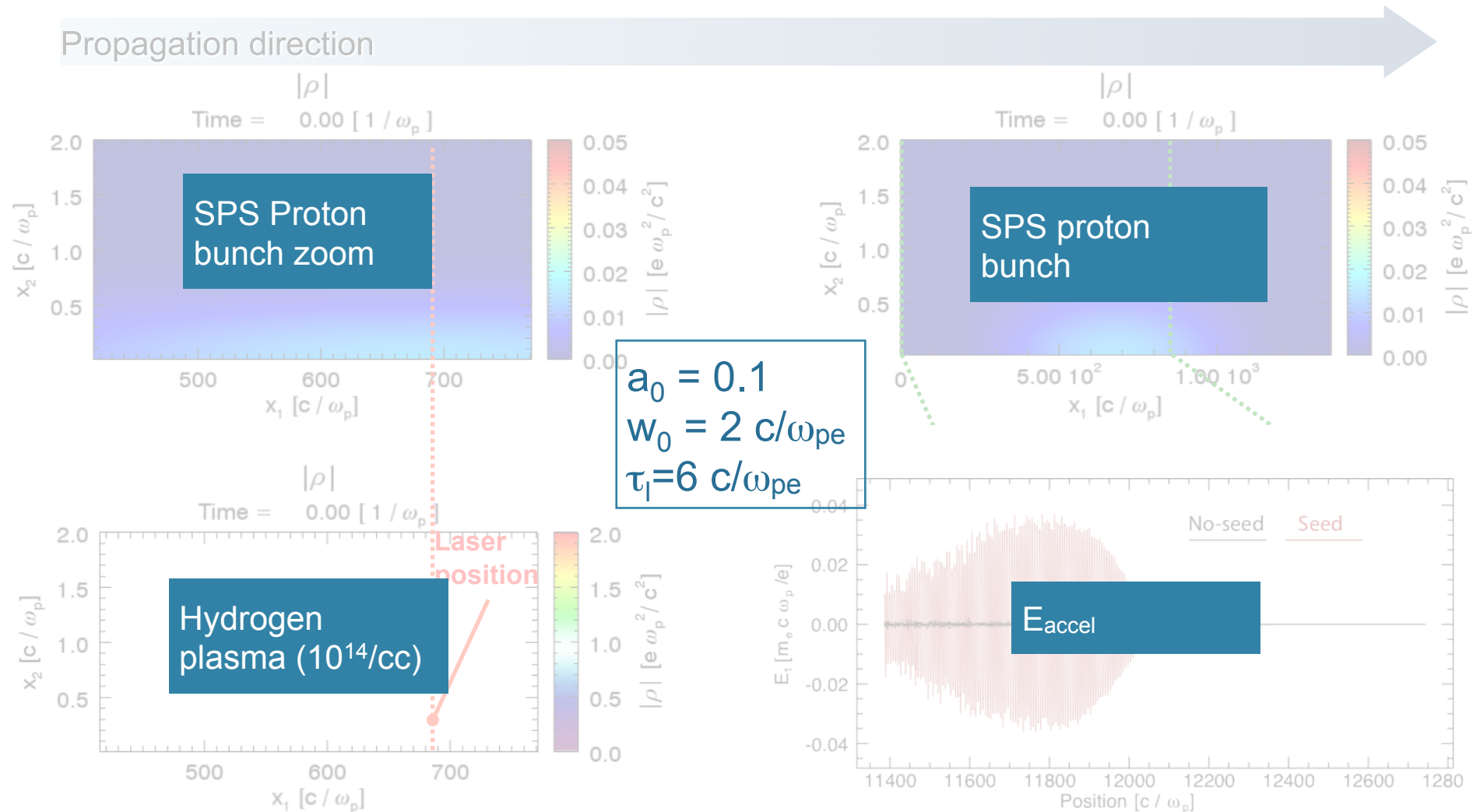
$$\partial_{\tau} a = \frac{1}{2i\omega_0} \left[ \left( 1 + \frac{1}{i\omega_0} \frac{\partial}{\partial \xi} + \nabla_{\perp}^2 \right) \right] a$$

$t=\tau$  (pointing to  $\partial_{\tau}$ )  
 laser frequency (pointing to  $\omega_0$ )  
 $\xi=x-ct$  (pointing to  $\frac{\partial}{\partial \xi}$ )  
 laser envelope (pointing to  $a$ )

D. Gordon, et al., IEEE-TPS, **28** 1135-1143 (2000).



# Creating plasma and cut proton bunch simultaneously Ionizing laser pulse



**Immobile ions are considered  
to avoid plasma ion motion**

J. Vieira et al, Phys. Rev. Lett. **109** 145005 (2012)



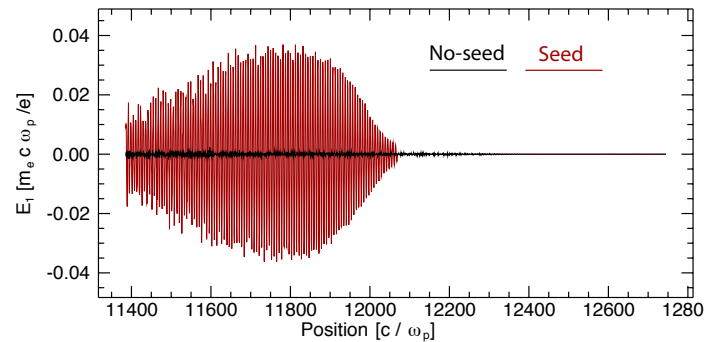


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# SMI SEEDING

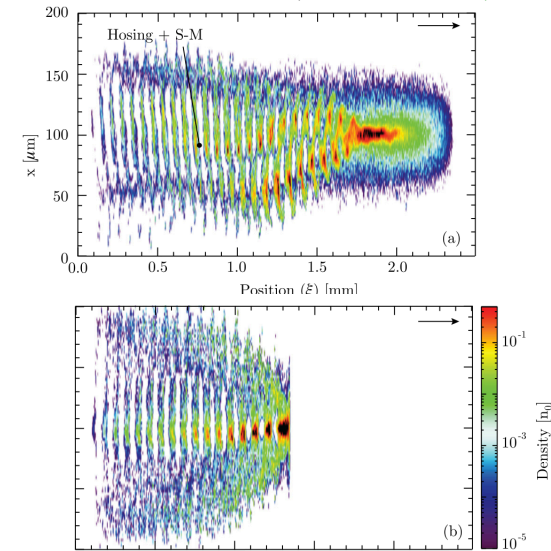


❑ Seeding of SMI is NECESSARY

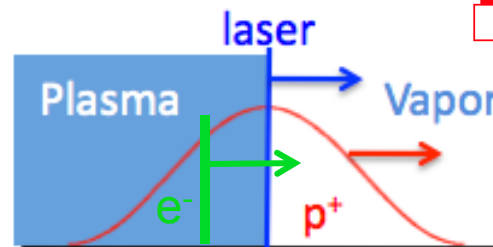


❑ No seed no SMI (over 10m)

SLAC  $e^-$  beam case, Vieira et al., PoP (2012)



❑ Hosing mitigation



❑ Deterministic  $e^-$  injection

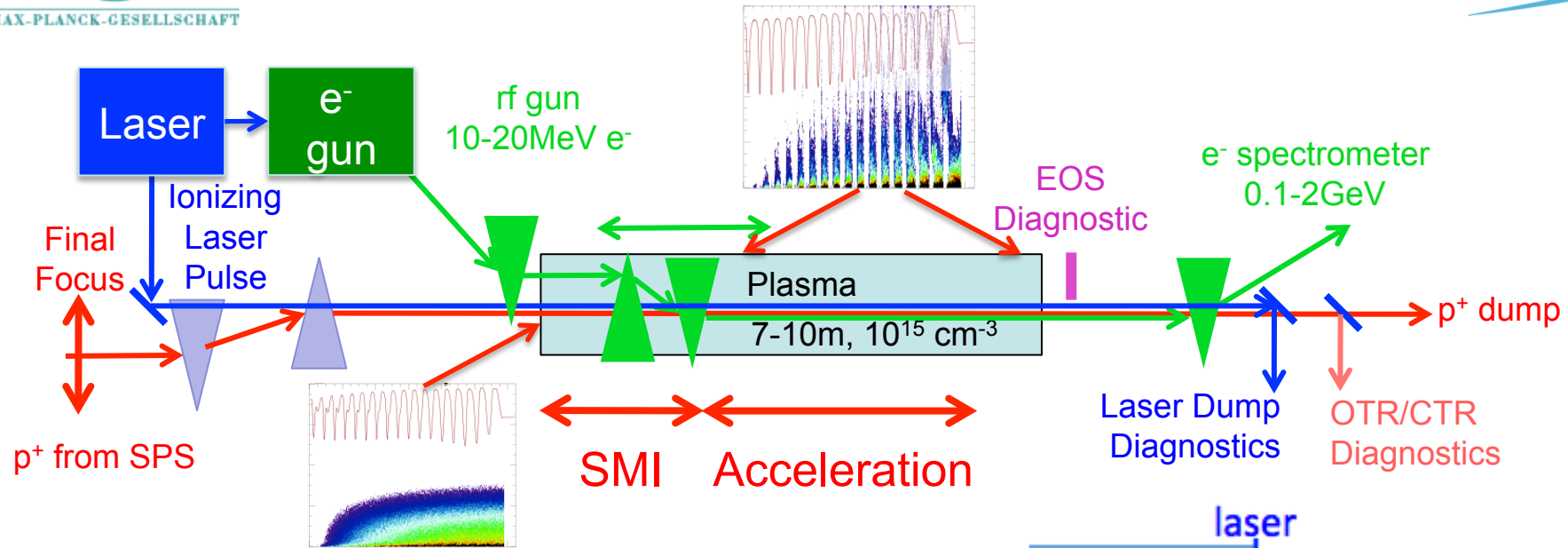
❑ Need to keep laser-ionized source for seeding



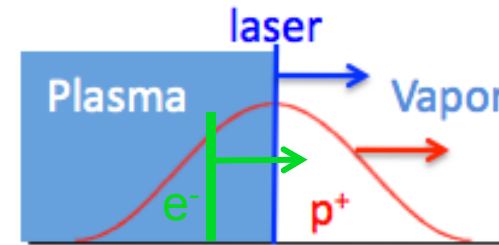


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# BASE-LINE EXPERIMENTAL SETUP



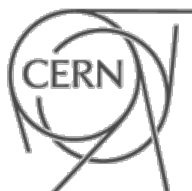
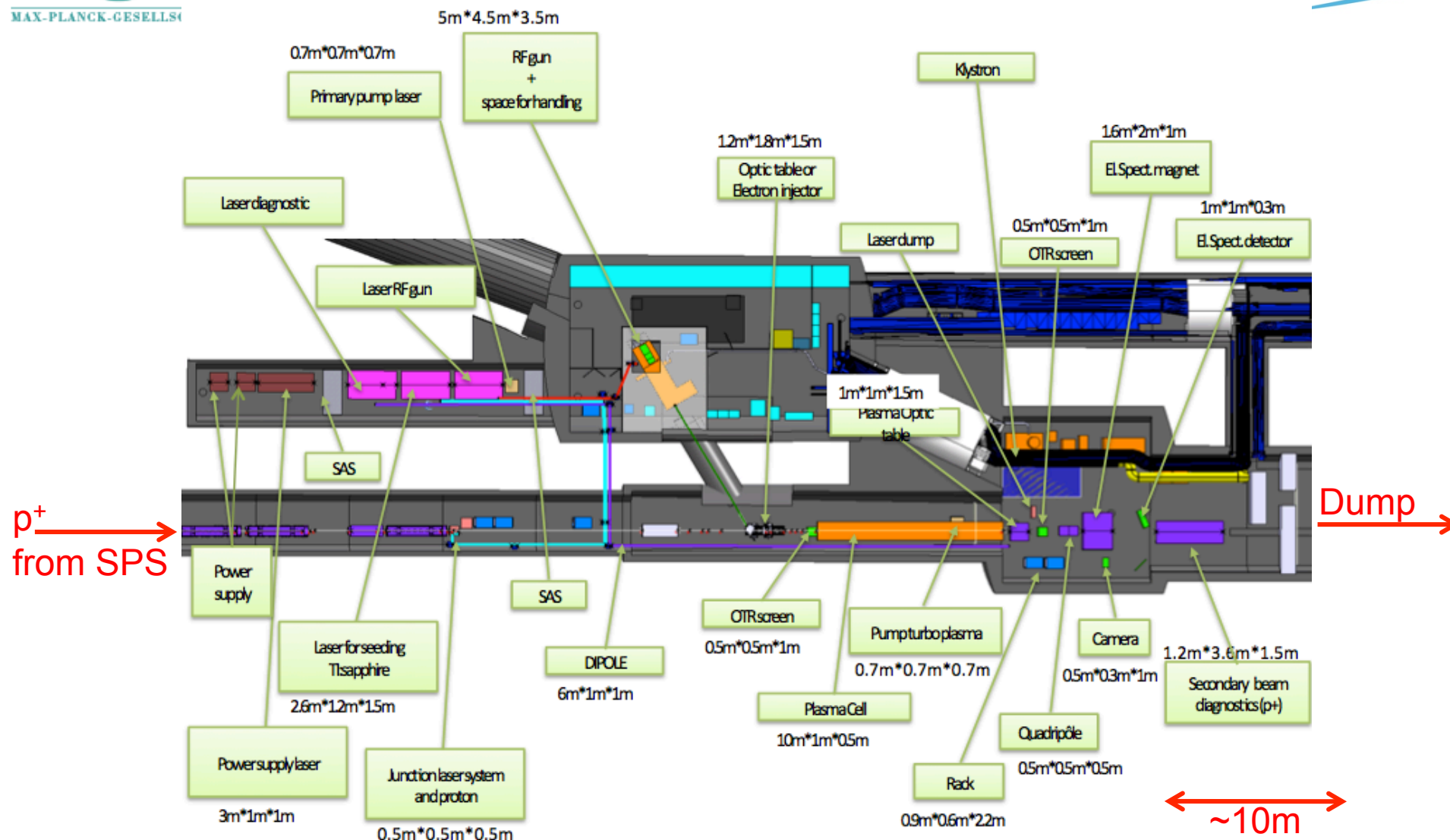
- ☐ Laser ionization of a Rb metal vapor, 7-10m plasma,  $n_e = 10^{14} - 10^{15} \text{ cm}^{-3}$
- ☐ Injection of 10-20MeV test e- at the 3m point (SMI saturated,  $v_\phi = v_{p+}$ )
- ☐ SMI-acceleration “separated”
- ☐ 0.1-5GeV electron spectrometer
- ☐ OTR + streak camera, electro-optic sampling for p<sup>+</sup>-bunch modulation diag.
- ☐ Additional optical diagnostics





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# CNGS EXPERIMENTAL AREA



Edda Gschwendtner CERN Project Manager  
Chiara Braco, Ans Pardon, ...





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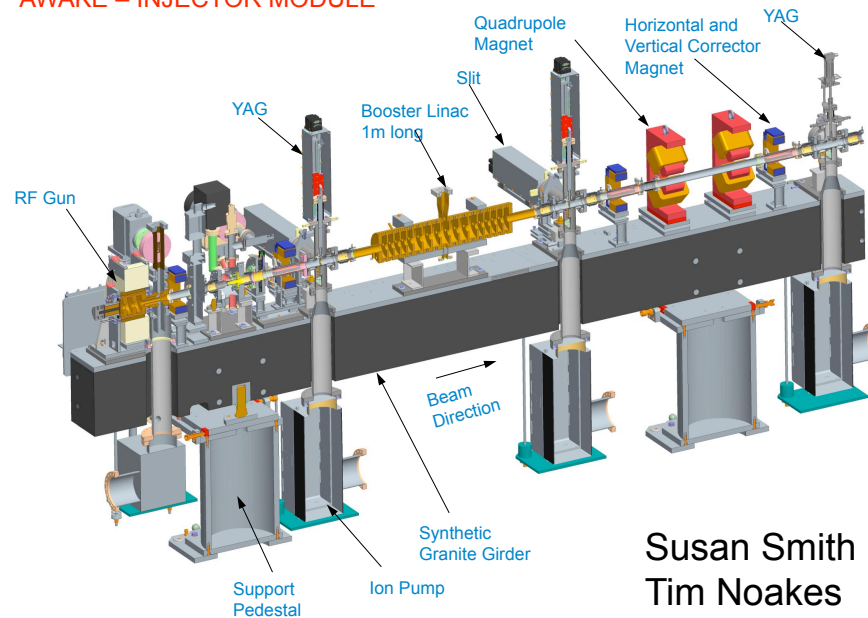
# e<sup>-</sup> GUN PHOTO INECTOR



❑ Two possible options:

❑ New gun from ASTeC Daresbury Laboratory

## AWAKE – INJECTOR MODULE



*Table 3: Design parameters for the electron bunch to be injected in the plasma wakefields.*

Parameter	Nominal Value
Beam Energy	5-20MeV
Energy Spread (rms)	<1%
Bunch Length	0.3-5ps
Laser/RF Synchronization	0.1ps
Synchronization to Experiment	0.1ps
Repetition Rate	10Hz
Focused Transverse Size	<250μm
Angular Divergence	<3 mrad
Normalized Emittance	0.5 mm-mrad
Charge	1-100pC

❑ PHIN gun from CERN-CLIC

❑ Must provide long (side injection, 1 plasma) and short (on axis, 2-plasma) bunches

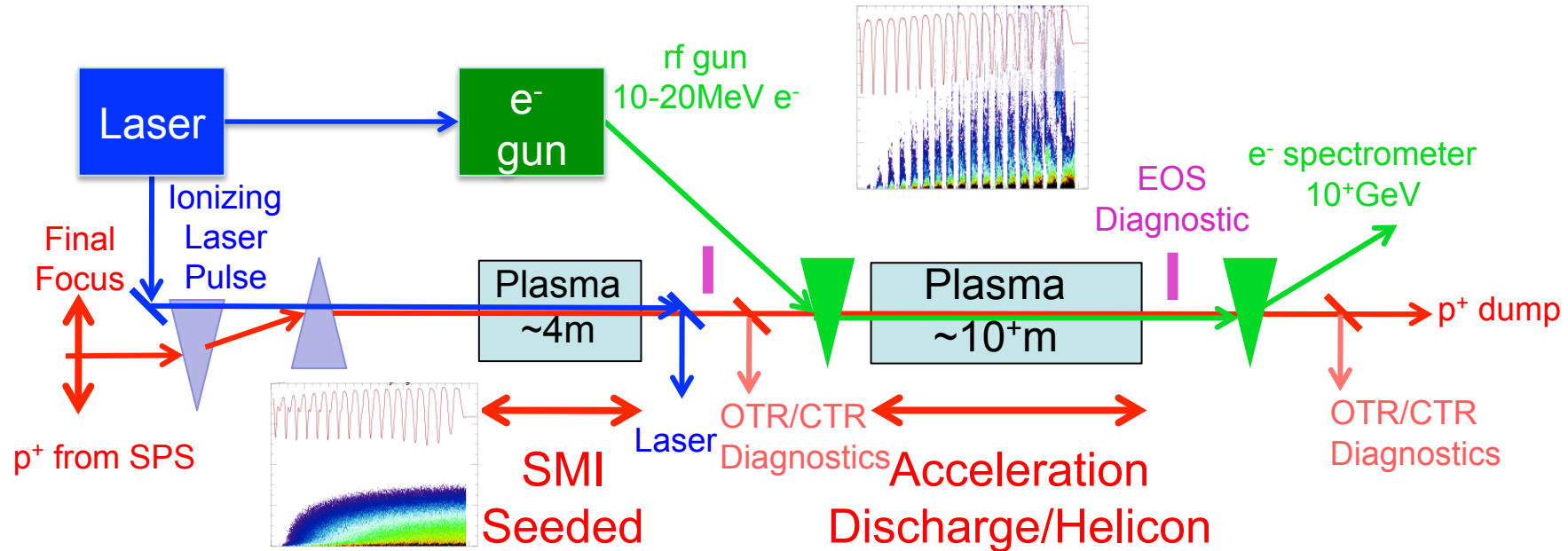
❑ Ionization laser will also be used for the pho-injector (synchronization!)





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# $p^+$ -PWFA ACCELERATOR PHYSICS



- ❑ Laser ionization of a metal vapor (Rb),  
3-4m plasma for  $p^+$  self-modulation only, SEEDING NECESSARY!
- ❑ ~10m discharge or helicon source for acceleration only
- ❑ Helicon plasma source scales well to very long plasmas (>100m)
- ❑ Maybe able to tune plasma densities to maintain accelerating gradient



P. Muggli, JAI 21/02/2013





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# PLASMA SOURCE FOR PWFA @ CERN



## ❑ Metal vapor source (Li, Cs) ~ SLAC experiments

- ❑ Very uniform, very well known
- ❑ Ionization? Scaling to long length?

## ❑ Long gas discharge

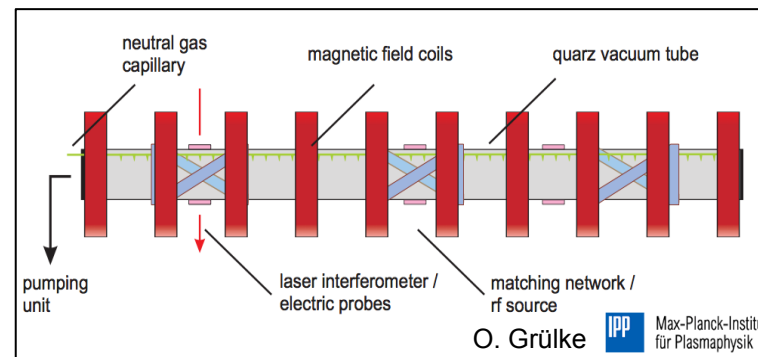
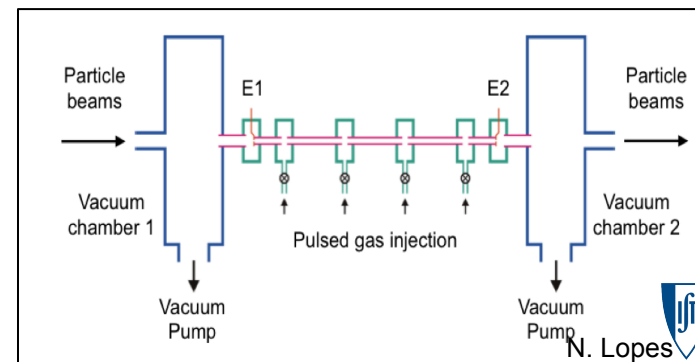
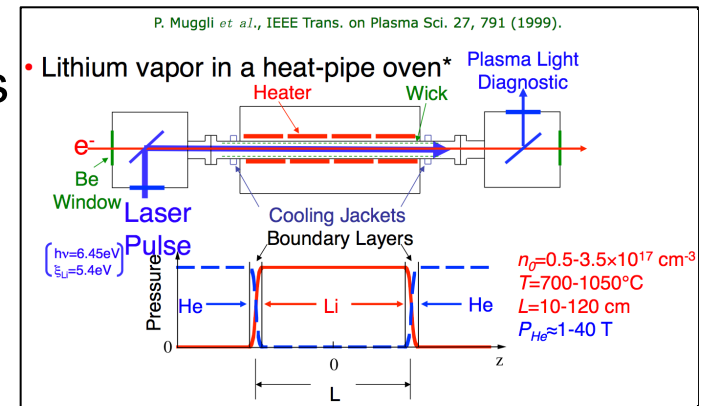
- ❑ Simple, scalable
- ❑ Density?

## ❑ Helicon source

- ❑ Scalable
- ❑ Density? Uniformity?

## ❑ Others?

## ❑ Choice to be made





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# PLASMA DENSITY REQUIREMENTS



❑ SMI-PWFA: **instability + resonantly** driven

❑ Requirements for SMI growth rate

For a linear gradient:  $\frac{n_e(z)}{n_{e0}} = 1 + \frac{z}{L}$

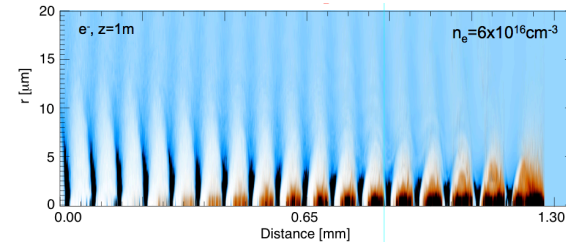
Instability suppressed if:  $L < \left( \frac{2\gamma n_{e0} m_p}{n_{b0} m_e} \right)^{1/3} \sigma_z^{2/3} L_p^{1/3}$

❑ Requirements witness bunch acceleration

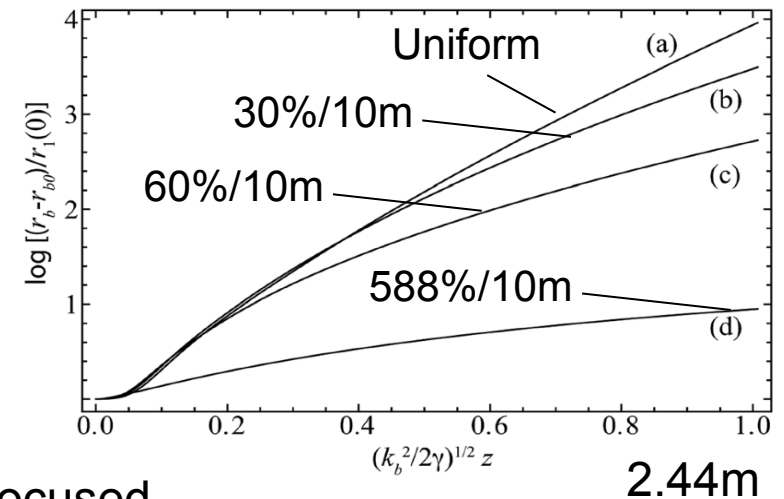
If  $\lambda_{pe}$  changes locally injected electron will be defocused

$$\Delta\phi = \frac{2\pi\xi}{\lambda_{pe0}} \frac{1}{2} \frac{\delta n_e}{n_{e0}} < \frac{\pi}{2} \Rightarrow \frac{\delta n_e}{n_{e0}} < \frac{\lambda_{pe0}}{4\xi} \equiv \frac{\lambda_{pe0}}{4\sigma_z} \equiv 0.25\%$$

❑ Tight requirement!



Schroeder, Phys. Plasmas 19, 010703 (2012)



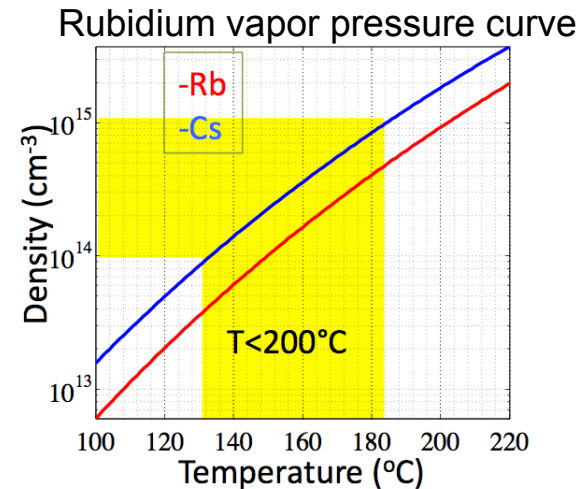
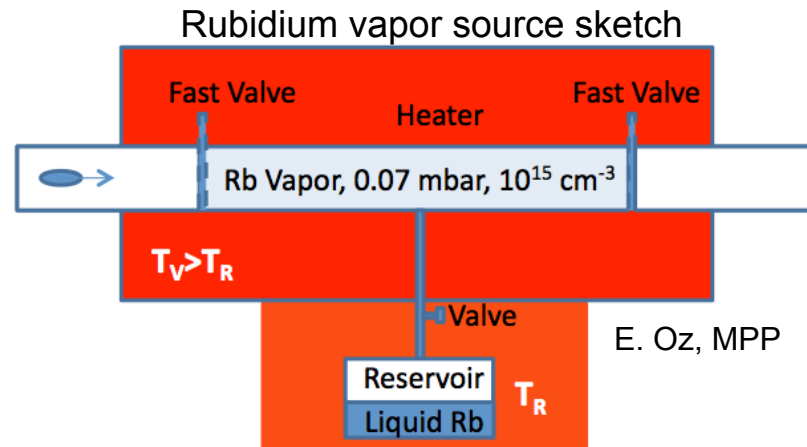
2.44m





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# PLASMA DENSITY REQUIREMENTS

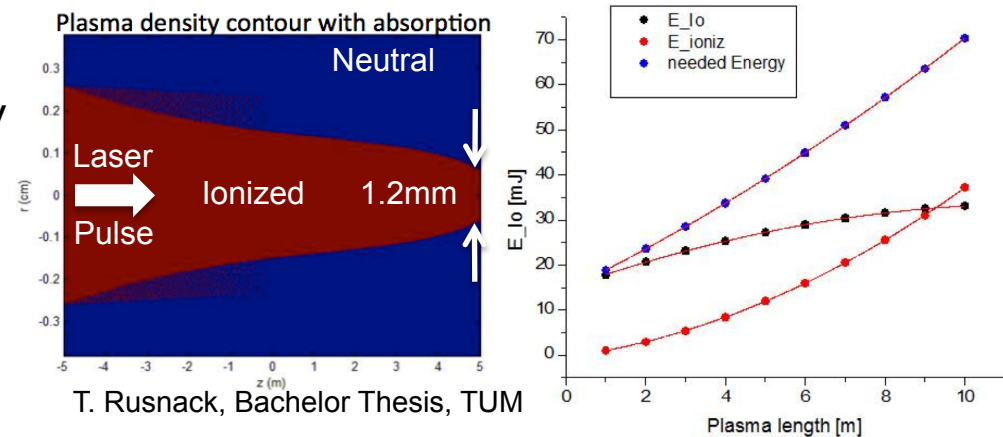
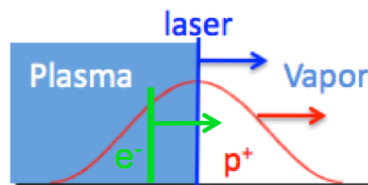


- Statistical temperature variations in a gas:  $\langle (\Delta T)^2 \rangle = \frac{k_B T}{C_V} \Rightarrow \frac{\sqrt{\langle (\Delta T)^2 \rangle}}{T} = \sqrt{\frac{k_B}{C_V T}} = \left| \frac{\delta n}{n} \right| \propto 10^{-14}$
- Tunnel Ionization, threshold process: Typically:  $C_V = 1000 \text{ J/kgK}$

$$I_{\text{Rb}} \approx (\phi_{\text{Rb}} / \phi_{\text{He}})^4 I_{\text{He}} \approx 1.7 \times 10^{12} \text{ Wcm}^{-2}$$

$$I_{\text{He}} \approx 1.54 \times 10^{14} \text{ Wcm}^{-2}, \phi_{\text{Rb}} = 4.2 \text{ eV}, \phi_{\text{He}} = 24.6 \text{ eV}$$

S. Augst et al., Phys. Rev. Lett. 63, 2212 (1989)



- Uniform neutral density (T) + threshold ionization + co-propagation





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# OUTLINE



- ❑ Introduction to Plasma Wakefield Accelerator (PWFA)
- ❑ Introduction to the self-modulation instability (SMI)
- ❑ SMI experiments at SLAC E209 with  $e^-/e^+$
- ❑ SMI PWFA experiments at CERN with  $p^+$ : AIAKE
- ❑ Summary



# 5/4 PLASMA ACCELERATORS\*



- **Plasma Wakefield Accelerator (PWFA)**

A high energy particle bunch ( $e^-$ ,  $e^+$ , ...)

P. Chen et al., Phys. Rev. Lett. 54, 693 (1985)

- **Laser Wakefield Accelerator (LWFA)**

A short laser pulse (photons)

- **Plasma Beat Wave Accelerator (PBWA)**

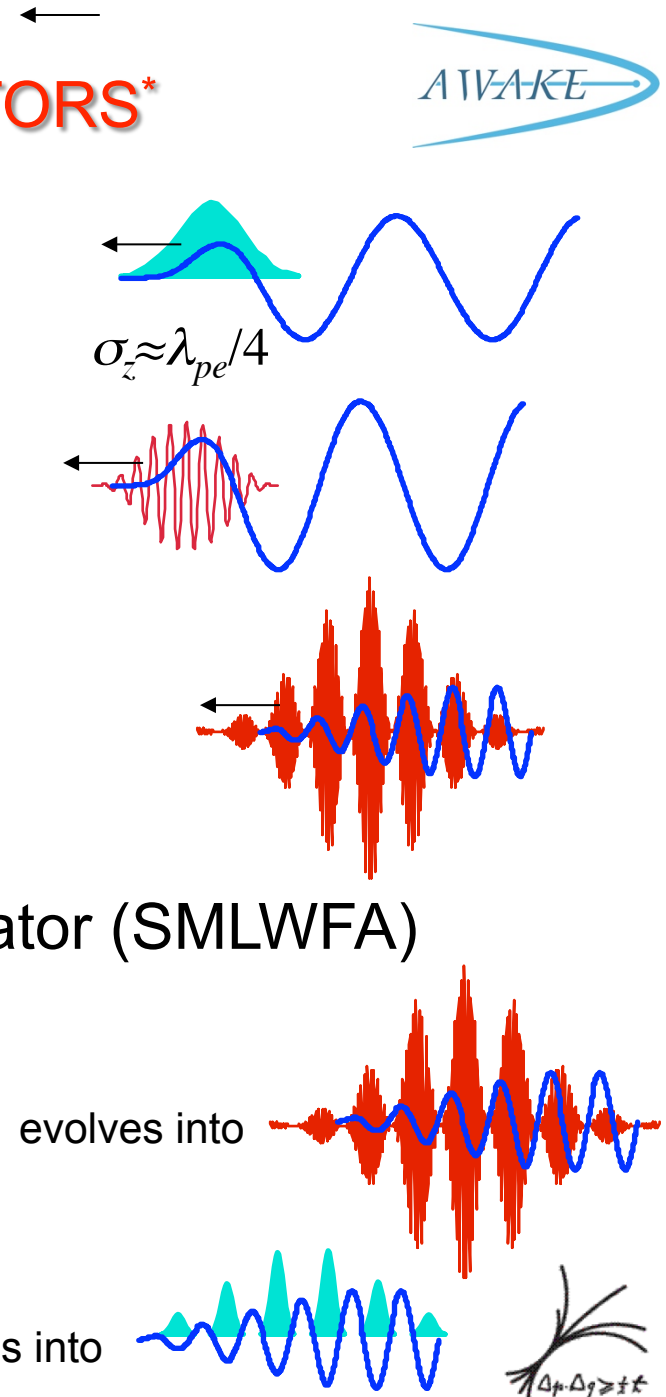
Two frequencies laser pulse, i.e., a train of pulses

- **Self-Modulated Laser Wakefield Accelerator (SMLWFA)**

Raman forward scattering instability  
in a long laser pulse

- **Self-Modulated PWFA (SMPP<sub>WFA</sub>)**

\*Pioneered by J.M. Dawson, Phys. Rev. Lett. 43, 267 (1979)







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# SUMMARY



- ❑ p<sup>+</sup> bunches are the only drivers with enough energy for PWFA to the energy frontier
- ❑ Observe self-modulation instability (SMI) of long particle bunches in plasma
- ❑ Signs of SMI seeding in ATF experiments
- ❑ SLAC E209 SMI physics experiment with e<sup>-</sup>/e<sup>+</sup> (2013)
  - Transverse modulation
  - Large wakefields (~10GV/m)
  - Seeding (cut bunch)
  - SMI/hosing competition
  - e<sup>-</sup>/e<sup>+</sup> differences
  - ...
- ❑ SMI PWFA experiments at CERN with p<sup>+</sup> (2015)
  - PWFA driven by p<sup>+</sup> bunch
  - SMI of p<sup>+</sup> bunch
  - Seeding (laser ionization)
  - ~GV/m over 10m
  - External injection of electrons
  - ...
  - Beginning of a long term program at CERN for p<sup>+</sup>-driven PWFA
- ❑ Other SMI experiments (DESY, UK, ...)

